

# General Certificate of Secondary Education 

## Mathematics 3301 Specification A

## Paper 1 Intermediate

## Mark Scheme

2007 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Mdep A method mark dependent on a previous method mark being awarded.
B dep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$

## Paper 1I

| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 1(a) | Line drawn from $3 x-x$ to $2 x$ | B1 |  |
| :---: | :--- | :--- | :--- |
|  | Line drawn from $3 x \times x$ to $3 x^{2}$ | B1 |  |
|  | Line drawn from $3(x+1)$ to <br> $3 x+3$ | B1 |  |
|  | Line drawn from $x \times x \times x$ to $x^{3}$ | B1 |  |
| $\mathbf{1 ( b ) ~}$ | $4 p+3 q$ | B2 | B1 For $4 p$ or $3 q$ <br> fw eg, $7 p q$ deduct 1 mark |


| $\mathbf{2 ( a )}$ | $400-(137+128)$ | M1 | oe |
| :---: | :--- | :---: | :--- |
|  | 135 | A1 | oe |
| $\mathbf{2 ( b )}$ | (Their 420$) \div 3$ | M1 | or $(137-128)$ and $(137-$ Their 135$)$ or 11 <br> oe |
|  | (Their 140$)-128$ | M1 | $(20-$ Their 11$) \div 3+9$ oe |
|  | 12 | A1 |  |


| 3 | $5-2.72$ | M1 | or 2.28 or 228 |
| :---: | :--- | :---: | :--- |
|  | (Their 228$) \div 6$ or <br> $($ Their 2.28$) \div 6$ | M1 | oe |
|  | 38 | A1 | or $£ 0.38$ |


| $\mathbf{4 ( a )}$ | $180-(90+36)$ or $90-36$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | 54 | A1 |  |
|  | $180-115$ or 65 | M1 |  |
|  | $180-(75+$ Their 65$)$ | M1dep | M2 For $115-75$ |
|  | 40 | A1 |  |
| $\mathbf{4}(\mathbf{c})$ | $r=72$ | B1 |  |
|  | $s=55$ | B1 |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{5}$ | 5 | B1 |  |
| :--- | :--- | :---: | :--- |
|  | 20 | B2 | B1 for $z=4$ |


| 6 | $\frac{60}{80} \times 100$ or $\frac{3}{4}$ | M1 | or Two fractions with same denominators and one correct numerator, eg, <br> eg, $\frac{15}{20}, \frac{14}{20}$ or $\frac{300}{400}, \frac{280}{400}$ oe |
| :---: | :---: | :---: | :---: |
|  | 75(\%) or 0.75 | M1 | or $\frac{15}{20}$ and $\frac{14}{20}$ or $\frac{300}{400}$ and $\frac{280}{400}$ oe |
|  | 75(\%) and 70(\%) and Test 1 0.75 and $0.7(0)$ and Test 1 | A1 | Correct fractions and Test 1 |


| 7 7(a) | $15 \div 3 \times 9$ | M1 | oe eg, $60-15$ |
| :--- | :--- | :---: | :--- |
|  | 45 | A1 | Can be recovered in (b) if missing in (a) |
| 7 (b) | 45 (boys pass) | B1ft |  |
|  | 35 (girls pass) and 25 (girls fail) | B1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 8(a) | $2 \times 3 \times 4$ | M1 | oe |
| :---: | :---: | :---: | :---: |
|  | 24 | A1 | oe |
|  | $\mathrm{m}^{3}$ | B1 | Units mark for consistent units |
| 8(b) | $2 \times 3$ or $2 \times 4$ or $3 \times 4$ | M1 | or 6,8 and 12 |
|  | $2 \times(2 \times 3+2 \times 4)+3 \times 4$ | M1 | $\text { oe eg, } \begin{aligned} & 2 \times(6+8)+12 \\ & 2 \times(2 \times 3+2 \times 4)+3 \times 4 \end{aligned}$ |
|  | (Their 40) $\div 6$ | M1dep | $(6 \div 6)+(6 \div 6)+(8 \div 6)+(8 \div 6)+(12 \div 6)$ |
|  | 7 | A1 | SC3 5 from 28 or 9 from 52 or 6 from 32 or 34 <br> or 5 from $1+1+1 .(\ldots)+1 .(\ldots)$ <br> or 6 from $1+1+1 .(\ldots)+2$ <br> or 6 from $1+1 .(\ldots)+1 .(\ldots)+2$ <br> or $\quad 9$ from $1+1+1 .(\ldots)+1 .(\ldots)+2+2$ <br> SC2 7 with no working <br> SC1 28 or 52 or 32 or 34 or 40 from 4 walls |


| $\mathbf{9 ( a )}$ | 3 | B1 |  |
| :--- | :--- | :---: | :--- |
| $\mathbf{9 ( b )}$ | 2 | B1 |  |
| $\mathbf{9 ( c )}$ | 40 | B1 |  |
| $\mathbf{9 ( d )}$ | $10 \div 0.5$ | M1 | oe eg, Allow $10 \div 30$ or $0.33(3 \ldots)$ |
|  | 20 | A1 |  |


| $\mathbf{1 0 ( a )}$ | $50 \times 2+120$ | M1 | or Better, eg, $100+120$ |
| :--- | :--- | :---: | :--- |
|  | 220 | A1 |  |
|  | $5 \times 200=m+750$ | M1 | or $200=\frac{m}{5}+150$ |
|  | 250 | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 11 | $(64=) 8 \times 8$ | B1 | or $8^{2}$ or $\sqrt{ } 64=8$ or " 8 times itself" |
| :---: | :--- | :---: | :--- |
|  | $(64=) 4 \times 4 \times 4$ | B1 | or $4^{3}$ or $\sqrt[3]{ } 64=4$ |


| 12 | Correct rotation $( \pm 2 \mathrm{~mm})$ | B2 | B1 for $90^{\circ}$ any clockwise rotation $( \pm 2 \mathrm{~mm})$ <br> or $180^{\circ}$ rotation about $C( \pm 2 \mathrm{~mm})$ <br> or $90^{\circ}$ anticlockwise rotation about $C$ <br> $( \pm 2 \mathrm{~mm})$ |
| :---: | :--- | :--- | :--- |


| $\mathbf{1 3 ( a )}$ | 55 | B1 |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 3 ( b )}$ | $45:$ Their 55 | M1 | oe or $11: 9$ |
|  | $9: 11$ | A1 |  |
|  | $18 \div($ Their 9$) \times($ Their 11$)$ | M1 | or $18 \div 45 \times 55$ oe |
|  | 22 | A1 |  |


| $\mathbf{1 4 ( a )}$ | $\frac{3}{8}$ | B2 | oe <br> B1 3 as numerator or 8 as denominator |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 4 ( b ) ( i ) ~}$ | $\frac{7}{20}$ | B2 | B1 7 as numerator or 20 as denominator |
| $\mathbf{1 4 ( b ) ( i i ) ~}$ | (Results are) random or occur by <br> chance | B1 | or Too few spins oe |
| $\mathbf{1 4 ( c )}$ | $\frac{1}{4} \times 1000$ | M1 | oe |
|  | or $\frac{250}{1000}$ |  |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 15(a) | Complete explanation <br> eg, Quadrilateral can be divided into 2 triangles and $2 \times 180$ <br> Use of $(n-2) \times 180$ with $n=4$ | B2 | or Using $\Sigma$ external angles $=360^{\circ}$ <br> eg, $\Sigma$ (Internal angles + external angles) <br> $=4 \times 180$ <br> $\Sigma$ Internal angles $=4 \times 180-360$ <br> B1 Partial explanation <br> B0 $2 \times 180$ only |
| :---: | :---: | :---: | :---: |
| 15(b)(i) | $3 x-12+x-6+2 x+90=360$ <br> or Better eg, $6 x+72=360$ | B1 | B0 $3 x-12+x-6+2 x+90=180$ |
| 15(b)(ii) | $6 x=288$ or $6 x=360-72$ or (Their 288) $\div 6$ | M1 | M1ft $6 x=108$ or $6 x=180-72$ or (Their 108) $\div 6$ |
|  | $x=48$ | A1 | A1ft $x=18$ |
|  | 132 | B1ft | $3 \times$ (Their $x$ ) - 12 for $35 \leq x \leq 63$ <br> SC1 48 no working or T \& I <br> SC2 48 and 132 no working or T \& I |


| 16 Arcs on $B A$ and $B C$ and <br> intersecting arcs M1  <br>  Bisector from $B \pm 2^{\circ}$ A 1 SC 1 Angle bisector based on arcs from $A$ and $C$ <br> $\mathbf{1 7 ( a )}$ A and D B 1  <br> $\mathbf{1 7 ( b )}$ All angles equal and 7 cm length <br> in corresponding $/$ matching/the <br> same position B1dep oe eg, ASA <br> $\triangle \mathrm{A} \leftrightarrow \triangle \mathrm{D}$ by rotation and reflection    |
| :--- |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{1 8 ( a )}$ | $\frac{2}{3}$ of 300 | B2 | B1 $\frac{1}{3}$ of 300 |
| :--- | :--- | :--- | :--- |
|  | or $300 \div 3 \times 2$ | or $300 \div 3$ |  |
|  | or $\frac{2}{3} \times 300$ |  |  |
|  | or $300-\frac{1}{3}$ of 300 | $\frac{200}{300}$ | M1 |
| $\mathbf{1 8 ( b )}$ | $100 \div 5$ or 20 | oe $\frac{1}{3} \times \frac{1}{5}$ |  |
|  | $80 \div 2$ or 40 | M1 | $\frac{1}{3} \times \frac{4}{5} \times \frac{1}{2}$ |
|  | 60 | A1 |  |


| 19(a) | $x^{8}$ | B1 |  |
| :--- | :--- | :--- | :--- |
| 19(b) | $y^{8}$ | B1 |  |


| 20(a) | $B$ : Volume, $C$ : None, $D$ : Area | B2 | B1 For one or two correct |
| :---: | :--- | :---: | :--- |
| 20(b) | Mixed dimensions | B1dep | oe Dependent on $C$ correct |


| 21 | $5 x+6 y=28$ $5 x+6 y=28$ <br> $2 x+6 y=4$ $5 x+15 y=10$ | M1 | Allow error in one term |  |
| :---: | :--- | :--- | :--- | :--- |
|  | $3 x=24$ | $-9 y=18$ | M1 | Correct elimination from Their equations |
|  | $x=8$ and $y=-2$ | A1 | SC1 Correct answers with no working or using <br> T \& I |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 22(a) | Jupiter | B1 |  |
| :---: | :--- | :---: | :--- |
| 22(b) | Pluto | B1 |  |
| 22(c) | Saturn | B1 |  |
| 22(d) | 4880000 | B1 |  |
| $\mathbf{2 2 ( e ) ~}$ | $\left(2.39 \times 10^{6}\right) \div 1000$ | M1 | or 2390 oe |
|  | $2.39 \times 10^{3}$ | A1 |  |


| $\mathbf{2 3}$ | Straight line <br> $(-2,-5)$ to $(-1,-2)$ or <br> $(-1,-2)$ to $(0,1)$ | B2 | B1 Line with constant positive gradient through <br> $(-1,-2)$ or <br> Any line with gradient 3 |
| :---: | :--- | :---: | :---: |


| 24(a) | 6 | B1 |  |
| :---: | :---: | :---: | :---: |
| 24(b) | (Girls) average (length is different to boys) | B1 | oe or <br> B1 Precise difference not related to average or spread <br> eg, (A boy jumped) the longest length, (The girls) LQ (is different to the boys) <br> For average allow: <br> eg, On the whole, on average, in general, overall, median, (not mean or mode),.. <br> For spread allow: <br> eg, Range, IQR, consistency, variability,... |
|  | (Girls jump greater) spread (of lengths) | B1 |  |
|  |  |  |  |


| 25 | $\pi \times 15^{2}$ or $\pi \times 10^{2}(\div 2)$ | M1 | Allow use of 3.(14...) |
| :---: | :---: | :---: | :---: |
|  | $225 \pi-50 \pi$ | M1 | or $\pi \times 225(-) \frac{1}{2} \times \pi \times 100$ <br> or $3 .(14 \ldots) \times 175$ <br> or 525 to 550 |
|  | $175 \pi$ | A1 | or $\pi \times 175$ or $175 \times \pi$ SC1 for $700 \pi$ |

