

General Certificate of Secondary Education

Mathematics 3301 Specification A

Paper 2 Intermediate Tier

Mark Scheme

2006 examination - November series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

The following abbreviations are used on the mark scheme:

| Μ | Method marks awarded for a correct method. |
|-----------------------|---|
| Α | Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied. |
| В | Marks awarded independent of method. |
| M dep awarded. | A method mark which is dependent on a previous method mark being |
| ft | Follow through marks. Marks awarded for correct working following a mistake in an earlier step. |
| SC | Special Case. Marks awarded for a common misinterpretation which has some mathematical worth. |
| oe | Or equivalent. |
| eeoo | Each error or omission. |

Paper 2I

| 1(a) | 125 | B1 | 125.0 |
|----------|-----------|------|--|
| 1(b)(i) | 0.7407407 | B1 | $\frac{20}{27}$ is B1 7.4 ⁻⁰¹ is B0 |
| 1(b)(ii) | 1 | B1ft | 1.0 is B0 |

| 2(a) | 8 × 4.55 | M1 | |
|------|-----------|----|--|
| | 36.4 | A1 | 36.40 |
| 2(b) | 40 ÷ 4.55 | M1 | |
| | 8.79(12) | A1 | 8.79, 8.8, 8.7 is A0 9 × 4.55 = 40.95 T & I M0 A0 |

| 3(a) | 8 and 12 | B2 | Either order |
|------|---------------------------------------|----|---|
| | | | B1 for one correct |
| 3(b) | Rectangle at | В3 | B2 Rectangle at $(2, -2)$ $(5, -2)$ $(5, -4)$ $(2, -4)$ |
| | (-2, 2) $(-5, 2)$ $(-5, 4)$ $(-2, 4)$ | | B1 Any rotation centre $(0, 0)$ |

| 4 | £60 | B1 | 6000 6000 mins is B0 |
|---|------------------------|------|------------------------|
| | 150 - 30 | M1 | 150 × 0.1 – 30 is M0 |
| | Their 120×0.1 | Alft | 1200 |
| | 26 and Contract | A1 | 2600 or cheaper by £34 |

| 5(a) | 21 – 10 | M1 | 21 + -10 |
|------|--------------|----|---------------------------|
| | 11 | A1 | |
| 5(b) | 4×9 | M1 | 4×3^2 only is M0 |
| | 31 | A1 | |

| 6 | Graph through (0, 5) | B1 | 1 correct point plotted or worked eg, (0, 5), (1, 7), (2, 9), (3, 11), (4, 13), (5, 15) |
|---|---|----|--|
| | Line gradient 2 | B1 | B1 for further 2 points plotted or worked |
| | Drawn line from (0, 5) to (5, 15) to $\frac{1}{2}$ sq accuracy | B1 | |

| 7 | A = 19, B = 4 | B2 | B1 for each |
|---|------------------|------|-------------|
| | C = 7 - Their B | B1ft | 3 |
| | D = 15 + Their C | B1ft | 18 |

| 8 | Fully correct triangle to 2 mm | В3 | B2 for 2 sides correct to 2 mm |
|---|--------------------------------|----|--------------------------------|
| | accuracy | | B1 for 1 side correct to 2 mm |

| 9 | 20 × 20 × 15 (6000) | M1 | $\frac{1000}{(20 \times 20)}$ or $\frac{15}{6}$ |
|---|-----------------------------|-------|---|
| | Their 6000 + 1000 | Alft | 2.5 |
| | Their 7000 \div (20 × 20) | M1dep | 15 + Their 2.5 |
| | 17.5 | A1 | T & I can get all 4 marks |

Only penalise once for notation error eg, 13 out of 28

Ratio never allowed

| 10(a)(i) | $\frac{13}{28}$ | B1 | oe 0.46(4) $\frac{6.5}{14}$ is B0 notation error |
|------------|---|----|---|
| 10(a)(ii) | $\frac{7}{28}$ | B1 | oe $\frac{1}{4}$ |
| 10(a)(iii) | $\frac{16}{28}$ | B1 | oe 0.57(1) |
| 10(b) | Double count blue eyed girls or Should be $\frac{20}{28}$ or 8 other children with brown or green eyes or There are 8 people left not 1 or Not taken off the girls who have blue eyes | B1 | B0 The 12 children may not all be girls Not all the girls have blue eyes He has added girls and blue eyed children Statement must have no incorrect part |

| 11Correct shadingB2B1 for just 3 corners | or just 3 mid-points |
|--|----------------------|
|--|----------------------|

Allow embedded answers unless contradicted when M marks only

| 12(a) | 4x = 21 - 7 | M1 | $x = \frac{21}{4} - \frac{7}{4}$ |
|-------|---------------------------------|----|---|
| | $\frac{14}{4}$, 3.5 | A1 | $3\frac{1}{2}, 3\frac{2}{4}$ oe |
| 12(b) | 7 = 14y - 6y or $-7 = 6y - 14y$ | M1 | $\frac{7}{6} = \frac{14}{6} y - y, \frac{7}{14} = y - \frac{6}{14}y, -8y = 7, 8y = -7$ |
| | $\frac{7}{8}$ | A1 | 0.875 oe |

| 13 S, A | ., N | В3 | -1eeoo |
|---------|------|----|--------|
|---------|------|----|--------|

| 14 | Digits 52 or 5 ÷ (360 to 363) | M1 | 13774 to 14444 |
|----|-------------------------------|----|---------------------|
| | 14000 | A1 | Accept 14300, 14400 |

| 15 | \sum fx (187) | M1 | At least 3 additions 0 + 16 + 70 + 45 + 56 |
|----|-----------------|----|--|
| | Their 187 ÷ 90 | M1 | |
| | 2.1, 2.08, 2.07 | A1 | Accept 2 with workings Beware $\frac{10}{5} = 2$ |

| 16 | 30 ÷ 20 | M1 | oe |
|----|-------------------------------------|-------|--|
| | Their $(\frac{30}{20}) \times 2.78$ | M1dep | 2.78 ÷ 0.667 M2 but M0 if time = $\frac{20}{30}$ |
| | 4.17 | Al | 4.2 |

| 17 | Evidence of adding at least two frequencies | M1 | 18, 52, 92, 100 |
|----|---|----|---|
| | $40 < m \le 80$ | A1 | Answer only with no working or no contradictory working M1, A1 Answer from incorrect working eg, mean = 75.2, $\frac{160}{2}$ = 80 M0, A0 |

| 18(a) | $3x - 6 \le 9$ | M1 | $x - 2 \le 3$ is M1 |
|-------|---|-------|---|
| | | | 3x - 6 = 9 or $x - 2 = 3$ is M0 unless inequality recovered |
| | | | Allow 1 error in 1 st or 2 nd line |
| | $3x \le 6 + 9 (= 15)$ | M1 | $x \le 3 + 2 (= 5)$ |
| | $x \le 5$ | A1 | $x = 5, x \ge 5, x > 5 \text{ or } 3(5-2) \le 9 \text{ SC1}$ |
| | | | $x = <5 x, \le 5, x < 5$ M2, A0 |
| 18(b) | Left Boundary | | |
| | $-3 \le$ open circle < -2 or $-3 <$ closed circle ≤ -2 | | |
| | Right Boundary | B1 | Boundaries must be joined by a line, ignore any markings on intermediate points |
| | closed circle on 3 or line beyond 3 with termination (arrow, circle, nothing) | | |
| | | | |
| 19(a) | $\frac{26}{100} \times 150$ | M1 | 39 |
| | 150 + Their 39 | M1dep | M2 for 1.26 × 150 |
| | 189 | A1 | 190 is A0 |
| 19(b) | 40 | B1 | 150 - 110 |
| | $40 \div 110 \times 100$ | M1 | 150 ÷ 100 (×100) = 1.3636 (136.36) is M0 |
| | | | unless 1 or 100% subtracted, then it is M2 |
| | 36.4, 36.36 | A1 | 36 if M1 awarded 36 from T & I is M0 |
| 19(c) | 120% = 110 | M1 | 110 ÷ 1.2 is M2 |
| | 1% = 0.9166 | Al | |
| | | A1 | T & I must get 91.6 to 91.7 |
| | 100% = 92, 91.7, 91.6 | | Beware $20 \times \frac{100}{110} = 18.18, 110 - 18.18 = 92$ M0 |

| 20(a) | $(x^2 =) 45^2 + 40^2$ | M1 | |
|-------|--|-------|--|
| | √3625 | M1dep | Mark is for squaring, adding and square rooting, |
| | | | $\sqrt{(45^2 + 40^2)}$ is M2 oe eg, $\frac{45}{\sin 48.366}$ |
| | 60.2 | A1 | 60 with working |
| | 60 | B1ft | For rounding Their answer to an integer |
| 20(b) | $Tany = -\frac{45}{40}$ | M2 | M1 for fraction wrong way M1 for other angle using correct trig. then M1 for subtract from 90° |
| | $Siny = \frac{10}{Their(a)}$ | | Cannot be scored in (a) |
| | $Cosy = \frac{40}{Their(a)}$ | | |
| | 48.1° to 48.6° | A1 | 48°, 49° with working Grads = 53.74, Rads = 0.844 M2, A0 |
| | | I | |
| 21 | $\pi r^2 = 8$ | M1 | |
| | Radius of circle $\sqrt{(8 \div \pi)}$ | M1 | √2.546 |
| | <i>r</i> = 1.59 | A1 | 1.6 |
| | Side square = 3 so No | A1 | oe $d = 3.19, 3.2$ so No |
| | | | |
| 22(a) | Lowest 'whisker' 8 | | |
| | Lower quartile 18 | | -1eeoo plotted to half square |
| | Median 25 | B3 | Failure to draw box is 1 error |
| | Upper quartile 32 | | Failure to draw 'whisker' is 1 error |
| | Highest 'whisker' 57 | | |
| 22(b) | 25% | B1 | |

| 23(a) | 4p + 4r = 7r + 11 | M1 | $p + r = \frac{(7r + 11)}{4}$ Allow one error eg, $4p + r = 7r + 11$ |
|-------|---|------------|--|
| | 4p = 3r + 11 | A1 | |
| | 2 . 11 1 | Alft | Dividing by 4 must be done correctly eg, $3r + 11 \div 4$ is A0 but |
| | $p = \frac{3r+11}{4}$ or $\frac{1}{4}(3r+11)$ | | eg, $(3r + 11) \div 4$ is A1 ft if M1 awarded eg, $p = \frac{(6r + 11)}{4} \frac{(7r + 11)}{4 - r}$ A2 |
| 23(b) | (x-9)(x+9) | B1 | |
| 23(c) | 3x + 5y = 4 $6x + 10y = 8$ | M1 | oe Allow error in 1 term |
| | 30x + 5y = 130 $6x + y = 26$ | | Sub one equation into other |
| | 27x = 126 $9y = -18$ | M1dep | oe Elimination from Their equation, at least one term correct eg, $27x = -126$, $9y = 18$ |
| | $x = 4\frac{2}{3}$ and $y = -2$ | A1 | oe (4.66, -2), (4.67, -2) SC1 for correct answer with no working or using trial and improvement. |
| 24(2) | 4.22 × 10.14 | D 2 | 4 222 × 10 ¹⁴ |
| 24(a) | 4.33×10^{-1} | B2 | 4.328×10^{14} P1 for 4.32^{14} or 4.3×10^{14} |
| | | | Only penalise once for calc. notation or 2 significant figures 4.3^{14} is B0 |
| 24(b) | 2.78×10^{16} | B2 | 2.783 × 10 ¹⁶ B1 for 2.78 ¹⁶ or 2.8×10^{16} |

| 25 | $20 = \frac{15}{v}$ | M1 | |
|----|---|----|--|
| | <i>v</i> = 0.75 | A1 | $\frac{15}{20}$ |
| | Their $0.75 = 0.6 \times \text{length}$ | M1 | Their 0.75 must be calculated value eg, $20 \div 6$ is M0, $300 \div 0.6$ is M1 |
| | 1.25 | A1 | |