ASSESSMENT and
OUALIFICATIONS

# General Certificate of Secondary Education 

## Mathematics 3301 Specification A

## Paper 2 Intermediate Tier

## Mark Scheme <br> 2006 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

## The following abbreviations are used on the mark scheme:

M Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
oe $\quad$ Or equivalent.
eeoo Each error or omission.

## Paper 2I

| 1(a) | 12.5 | B1 |  |
| :---: | :---: | :---: | :---: |
| 1(b) | $36 \div 100 \times 420$ | M1 | oe Allow full method of $10 \%, 10 \%, 10 \%, 5 \%, 1 \%$ |
|  | £151.20 | A1 |  |
| 1(c) | $84 \div 240 \times 100$ | M1 | oe |
|  | 35 | A1 |  |
| 2 | $3 \times 52$ | M1 | 156 or $245-26(=219)$ |
|  | Their $156+26$ | M1dep | and $3 \times 52(=156)$ |
|  | 245 - their 182 | M1dep | and their 219 - their 156 |
|  | 63 | A1 | SC2 £167 |


| $\mathbf{3 ( a )}$ | 7,13 | B1 |  |
| :--- | :--- | :---: | :--- |
| $\mathbf{3 ( b )}$ | Correct plotting on ft to $\frac{1}{2} \mathrm{sq}$ | B1ft | Allow 1 error |
|  | Line from $(0,4)$ to $(5,19)$ to $\frac{1}{2} \mathrm{sq}$ | B1 |  |
| $\mathbf{3 ( c )}$ | Line at least 3cm long to $\frac{1}{2} \mathrm{sq}$ | B1 | Label not needed if correct |


| 4(a) | $72 \times \frac{5}{8}$ | M1 | $72 \times 0.625,72 \div 1.6$ |
| :---: | :---: | :---: | :---: |
|  | 45 | A1 |  |
| 4(b) | 3.5 | B1 | oe or 210 |
|  | $\frac{200}{\text { their3.5 }}$ | M1 | $\frac{200}{\text { their } 210} \times 60$ |
|  | 57.1(4) | A1 |  |
|  | Round their answer to 1 dp or 0dp | B1ft | 57 or 57.1 , or 60 with working |


| $\mathbf{5}$ | Prism with triangular cross <br> section | B2 | B1 for any prism <br> Allow free hand sketch |
| :---: | :--- | :--- | :--- |


| 6 | $\frac{(180-126)}{2}$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $x=27$ | A1 |  |
|  | 153 | B1ft | $126+$ their $x, 180-$ their $x$ |


| 7(a) | 1 | B 1 |  |
| :--- | :--- | :---: | :--- |
| 7 7(b) | $3 n$ | M 1 | $n+n+n, n \times 3$, but not $n 3$ |
|  | $3 n+7$ | A 1 | $\mathrm{SC} 1 n 3+7$ <br> $3 n+7=10 n$ is M1, A0 |


| $\mathbf{8 ( a )}$ | 58 | B1 |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{8 ( b )}$ | 13 | B1 |  |
| $\mathbf{8 ( c )}$ | 15 | B1 |  |
| $\mathbf{8 ( d )}$ | $\Sigma x$ at least 6 correct values | M1 |  |
|  | $\frac{\text { their } 288}{\text { their13 }}$ | M1dep |  |
|  | 22.2 | A1 | $22.1,22.15$ or 22 with working |


| 9 | Square any number between 0 <br> and 1 inclusive and show <br> answer | B2 | B1 square any number $>1$ and show answer <br> B1 (number in range) but not evaluated or <br> evaluated incorrectly |
| :---: | :--- | :---: | :---: |


| $\mathbf{1 0}$ | $-2,1,6$ | B2 | -1 each error or emission. <br> Ignore extra terms <br> $1^{2}-3,2^{2}-3,3^{2}-3$ is B1 |
| :---: | :--- | :--- | :--- |


| 11 | $20 \times 10 \times 20(=4000)$ | M1 | Must be volume calculation not surface area |
| :---: | :---: | :---: | :---: |
|  | $5 \times 5 \times 2(=50)$ | M1 | Must be volume calculation not surface area |
|  | $\frac{\text { their } 4000}{\text { their } 50}$ or 80 or $\frac{(20 \times 10 \times 20)-(70 \times 5 \times 5 \times 2)}{(5 \times 5 \times 2)}$ | M1 | M3 for $4 \times 2 \times 10$ <br> M2 for two of 2, 4 or 10 multiplied together and by another number |
|  | 10 | A1 |  |

## Allow embedded answers unless contradicted when M marks only

| 12(a) | $4 v=9+1$ (or 10) | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $v=2.5$ | A1 | oe |
| 12(b) | $3 w+2 w=19-4$ | M1 | oe Allow one sign error |
|  | $5 w=15$ | M1dep | Gathering terms |
|  | $w=3$ | A1 |  |
| 12(c) | $x=5 \times(11+2)$ | M1 | $x=5 \times 11+10$ |
|  | 65 | A1 |  |
| 12(d) | $4 y+12=9 y-18$ | M1 | Allow one error |
|  | $30=5 y,-5 y=-30$ | A1ft | ft if M1 awarded and equation in form $a y=b$ with no further errors |
|  | 6 | A1ft | ft only if M1, A0 previously and their equation of form $a y=b$ is solved correctly |


| 13 | $5 x>10-3(=7)$ |  | Accept $5 x \geq 7,5 x \geq 10-3$ |
| :--- | :--- | :--- | :--- |
|  | $x>\frac{7}{5}$ |  | oe |
|  |  | eg accept $x>1.4$ or $x>1 \frac{2}{5}, \frac{7}{5}<x, 1.4<x$ <br> SC1 $x>2.6$ oe <br> $x=1.4$ on answer line after $x>1.4$ is M1, A0 |  |


| 14 | Line 4cm, arcs 6 cm (above) | B1 | All $\pm 2 \mathrm{~mm}$ |
| :---: | :---: | :---: | :---: |
|  | Complete correct triangle | B1 |  |
|  | Arcs 6cm (below) | B1 |  |
|  | Complete correct rhombus | B1 |  |
|  | or line 6 cm , arcs 4 cm and 6 cm | B1 | or line 2 cm , construction $90^{\circ}$ with arcs |
|  | Complete correct triangle | B1 | Hypotenuse of length 6cm |
|  | Arcs 6 cm from 4cm line | B1 | Repeat below |
|  | Complete correct rhombus | B1 | Complete correct rhombus |


| 15 | Angle bisector to $\pm 2^{\circ}$ | B1 | See overlay. <br> Just points plotted is B0 |
| :---: | :--- | :---: | :--- |
|  | Circles of arcs 4 cm and 7 cm <br> from A to $\pm 2 \mathrm{~mm}$ | B1 | See overlay. <br> Accept crosses on their angle bisector |
|  | Correct line segment indicated | B1 |  |

$\left.\begin{array}{|l|l|c|l|}\hline \mathbf{1 6 ( a )} & \text { Plot }(50,0.4) & \text { B1 } & 1 \mathrm{~mm} \text { tolerance } \\ \hline \mathbf{1 6 ( b )} & 27 & \text { B1 } & \\ \hline \mathbf{1 6 ( c )} & \begin{array}{l}\text { Yes + reason with numbers } \\ \text { eg Yes if fair expect } 15 \mathrm{As} \\ \text { Yes if fair prob }=0.25\end{array} & \text { B2 } & \text { B1 Yes + reason that must have some sense } \\ \text { eg Yes As A comes up nearly half the time } \\ \text { Yes There are 4 sections and A is } \\ \text { winning an unfair amount of spins }\end{array}\right\}$

| $\mathbf{1 7}$ | Fruity bar $17.4 \times \frac{62.6}{100}$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $10.9,10.89 \ldots$ | A1 | 11 with working |
|  | Sports bar $3.4 \times \frac{100}{10.3}$ | M1 |  |
|  | $33 .(\ldots \ldots)$ | A1 |  |


| 18(a) | $(m-7)(m+7)$ | B1 | oe |
| :---: | :---: | :---: | :---: |
| 18(b) | Attempt to rearrange one equation and substitute into another <br> or <br> Attempt to balance $x$ or $y$ and eliminate | M1 | $\text { eg } \quad \begin{aligned} & 15 x+9 y=18 \\ & \\ & 15 x-35 y=95 \end{aligned}$ <br> followed by an attempt to subtract <br> eg $\quad 44 y=-77$ $\begin{aligned} & 35 x+21 y=42 \\ & 9 x-21 y=57 \end{aligned}$ <br> followed by an attempt to add <br> eg $\quad 44 x=99$ |
|  | Solving resultant equation to find $x=2.25$ or $y=-1.75$ | A1 |  |
|  | Attempt to eliminate other variable or substitution of found value into one of their equations | M1 | eg $\quad 11.25+3 y=6,5 x-5.25=6$ |
|  | Solving to find another value $y=-1.75$ or $x=2.25$ | A1 |  |


| 19 | Total reduction $£ 6+£ 1(=£ 7)$ <br> or cost is $£ 3$ | M1 | $25 \%$ of $£ 4=£ 1$ <br> $25 \%$ of $40 \%=10 \%$ |
| :---: | :--- | :---: | :--- |
|  | Hence Jill plus justification <br> eg $£ 7$ is $70 \%$ of $£ 10$ | A1 | $60 \%+10 \%=70 \%$ <br> $85 \%$ off $£ 10=£ 1.50$ |


| $\mathbf{2 0 ( a )}$ | 0.007 | B1 |  |
| :---: | :--- | :--- | :--- |
| $\mathbf{2 0 ( b ) ( i )}$ | $0.9119215(052)$ | B1 |  |
| $\mathbf{2 0 ( b ) ( i i ) ~}$ | $9.12 \times 10^{-1}$ | B1 |  |
| $\mathbf{2 0 ( c )}$ | 0.00805 or $8.05 \times 10^{-3}$ | B1 | oe |


| 21 | Identifying -2 as constant term <br> in equation $y=m x+c$ | B1 |  |
| :---: | :--- | :--- | :--- |
|  | Gradient $=\frac{20}{4}$ | M1 | Attempt to find gradient $\frac{ \pm 20}{ \pm 4}, \frac{ \pm 16}{ \pm 4}$ |
|  | $y=5 x-2$ | A1 | oe |


| 22 | $400-2 \times 80$ | M1 | 240 |
| :---: | :--- | :--- | :--- |
|  | $\pi d$ or $\pi r$ or $2 \pi r=$ anything | M1 | Anything but not 400 |
|  | $240 \div \pi$ | M1 | $240 \div(2 \pi) \quad(=38.2)$ |
|  | 76.4 | A1 | 76 with working or 80 with working |


| 23(a) | $10^{2}-5^{2}=Q R^{2}$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $Q R=\sqrt{ } 75$ | M1dep |  |
|  | $8.66(0 \ldots)$ or $5 \sqrt{3}$ or 8.7 | A1 | 9 with working |
| 23(b) | $\begin{aligned} & \cos P=\frac{5}{10} \\ & \sin P=\text { their } \sqrt{ } \frac{75}{10} \\ & \tan P=\operatorname{their} \sqrt{ } \frac{75}{5} \end{aligned}$ | M2 | Finding R then subtract from 90 |
|  | 60 | A1 |  |


| 24 | Sight of 1.072 | B1 | or 144 |
| :---: | :---: | :---: | :---: |
|  | $(2000) \times(\text { their } 1.072)^{10}$ | M1, A1 | Calculating at least 5 intermediate values correctly using their values M1 $\begin{aligned} & 2144,2298.37(.368), 2463.85(0496), \\ & 2641.25(.2477732), 2831.42(.417568) \\ & 3035.28(.279633), 3253.82(.819767), \\ & 3488.09(.09479), 3739.24(.237615), \\ & 4008.46(.462723) \end{aligned}$ <br> All 10 correct A1 <br> No penalty for rounding or truncating to nearest pound or 1 decimal place <br> Truncated values 2144, 2298, 2463, 2640, 2830, 3033, 3251, 3485, 3735, 4004 <br> Rounded values 2144, 2298, 2463, 2640, 2830, 3034, 3252, 3486, 3737, 4006 <br> No penalty for incorrect money notation eg $\quad 4008.5>2 \times 2000$ |
|  | Yes. 4008.(46) or 2.004(2..) | A1ft | ft if only one error made and correct conclusion drawn <br> Accept $1.072^{10}>2$ for 3 marks <br> SC2 for $2000 \times$ their $1.072^{9}$ |

