# AQA 

ASSESSMENT and
OUALIFICATIONS

## General Certificate of Secondary Education

## Mathematics 3301 Specification A

Paper 2 Intermediate Tier

## Mark Scheme

2005 examination - November series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available to download from the AQA Website: www.aqa.org.uk
Copyright © 2005 AQA and its licensors. All rights reserved.

## COPYRIGHT

AQA retains the copyright on all its publications. However, registered centres for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to centres to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Set and published by the Assessment and Qualifications Alliance.

## AQA GCSE Mathematics Specifications A \& B

## Notes for Examiners

In general if a response is fully correct then it is sufficient to tick the final answer and put the mark for that part in the margin. Parts not attempted or totally incorrect must have 0 for that part in the margin. Negative marks must not be used.

Errors must be underlined or ringed.
Responses that are partly correct will generally be awarded marks for method or partial working. In that case the following should appear in the margin to indicate what the mark(s) has been awarded for. These are detailed in the mark scheme.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
M dep A method mark dependent on a previous method mark being or DM awarded.

B dep A mark that can only be awarded if a previous independent mark or DB has been awarded.

Ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.

Within the script the following notations can be used to explain the decision further. These should appear next to the place in the script where the error or omission is made.

| ft | Follow through marks. Wrong working should not be penalised <br> more than once so that positive achievement later in the question <br> can be recognised. |
| :--- | :--- |
| or |  |$\quad$| An answer that does not follow through from previous working. |
| :--- |


| Fw | Further work. Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer. |
| :---: | :---: |
| Choice | When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost. |
| Wnr | Work not replaced. Erased or crossed out work that is still legible can be marked. |
| Wr | Work replaced. Erased or crossed out work that has been replaced is not awarded marks. |
| 入 | Work incomplete or method missing. |
| Allow | In general decisions should support the candidate. If an examiner feels that work is worthy of a mark then it can be allowed. |
| BOD | Benefit of the doubt should only be given in cases where evidence is not secure. For example overwriting numbers. It should not be used to avoid making a decision. Examiners are expected to make decisions based on the scheme. |
| $\begin{aligned} & \text { seen } \\ & \text { or } \end{aligned}$ | Every page containing working should be annotated to show it has been considered. |
| From page $23 】$ | Marks transferred from another part of the paper. Candidates often make a mistake in their original work and do the question on the back page or another page with some space. The part marks should be credited there within the script and the marks transferred to the margin by the printed question. |
| Wrong method | Candidates sometimes obtain the correct answer via a completely wrong method. If an examiner is sure that this is the case then the Method mark should not be awarded and subsequently the accuracy mark cannot be awarded. This notation should also be used when candidates 'fiddle' algebra to demonstrate a given result. |
| Pa | Premature approximation. Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise in the standardising meeting. |

## Unusual responses

Very occasionally situations may occur which are not covered by the above notations. In these rare cases examiners should write brief comments in the script to explain their decision, such as ignore, irrelevant etc.

## Blank answer spaces and blank pages

Blank answer spaces should be crossed through to show that they have been seen. Blank pages at the end of a paper should also be crossed through to indicate that they have been seen. Any working on these pages must be marked.

## Diagrams

Diagrams that have working on them should be treated like normal responses and marked with same notations as above. If the diagram is written on but the correct response is within the answer space the work within the answer space should be marked and the diagram ticked to indicate that the examiner has seen it. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised as directed at the standardising meeting.

## Questions which ask candidates to show working

Instructions on marking will be given at the standardising meeting but usually marks are not awarded to candidates who show no working.

## Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

## Probability

Answers should be written as fractions, decimals or percentages. If a candidate uses an incorrect notation such as " 1 out of 4 " for $1 / 4$ consistently through the paper, then penalise the first occurrence but allow any following answers. Ratio is not acceptable as incorrect notation.

## Recording Marks

Part marks for a question should be shown in the margin at the side of the work. The totals should be shown in the oval either at the end of each question or after each double page. These marks should be transferred to the appropriate box on the front of the paper. The grand total for the paper should also be shown in the appropriate box on the front of the paper. This total should agree with the total of the part marks within the paper.

Checkers at the board will first check that the part marks agree with the ringed totals, either at the end of each question or after each double page. They will then check that these marks have been transferred correctly and finally that the total on the front cover is correct. Papers that contain clerical errors may be returned to examiners.

## Paper 2I

| $\mathbf{1 ( a ) ( i ) ~}$ | 11 | B1 |  |
| :---: | :--- | :--- | :--- |
| $\mathbf{1 ( a ) ( i i ) ~}$ | 8 | B1 |  |
| $\mathbf{1 ( b )}$ | 200 | B2 | B1 for 8 or 25 |


| 2(a) | $\frac{5}{20}, 1 / 4,0.25,25 \%$ | B2 | B1 for $5 /$ total $\quad$ B1 for $? / 20$ must be a prob. |
| :--- | :--- | :--- | :--- |
| 2(b) | $0.6,60 \%, 3 / 5$ | B1 | oe |


| 3(a)(i) | 5,9 | B1 |  |
| :---: | :--- | :---: | :--- |
| 3(a)(ii) | Correct plots on ft | M1 | At least 3 correct on ft |
|  | Straight line between 1 and 5 <br> All plots correct | A1 | allow freehand sketch to $1 / 2 \mathrm{sq}$ accuracy <br> ignore $(0,0)$ |
| $\mathbf{3 ( b )}$ | Correct line at least 2 cm long | B1 | allow freehand sketch to $1 / 2$ sq accuracy |


| 4(a) | 2 on bottom row right hand side | B1 |  |
| :--- | :--- | :---: | :--- |
| 4(b) | 2 correct and none wrong | B1 |  |
|  | 3 correct and none additional | B1 | see diagrams below |


|  |  | e | d |  |  |  | a |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | f | c |  |  | b |  |  |  |  |  |
| e | f | a | b |  | c |  |  |  |  | a |  |
| d | c | b | a | d |  |  |  |  |  |  |  |


| $\mathbf{5}$ | $200 / 1.82$ | M1 | M2 20370x1.82/194 or $200 \times 194 / 1.82$ |
| :--- | :--- | :---: | :--- |
|  | $20370 / 194$ | M1 |  |
|  | their $£ 109.89-$ their $£ 105$ | DM1 | $200-$ their $191.1(0)$ or 20370 - their <br> $21318 .(68)$ |
|  | Japan and $£ 4.89$ | A1 | $8.9(0)$ dollars or 948.(68) yen |


| $\mathbf{6}$ | $180-52-90$ | M1 | $90-52$ |
| :--- | :--- | :--- | :--- |
|  | 38 | A1 |  |


| 7(a) | Draws any rhombus | B1 | Accuracy of 3 mm. <br> Angle between sides must not be 90 |
| :--- | :--- | :---: | :--- |
| 7(b) | Rhombus | B1ft | Not square, diamond, oblong |


| $\mathbf{8 ( a )}$ | Both points plotted | B1 | $1 / 2$ sq accuracy |
| :---: | :--- | :---: | :--- |
|  | Line drawn | B1ft | One plot must be correct |
| $\mathbf{8 ( b )}$ | Any value between 11 and 12 <br> inclusive | B1 |  |


| 9(a) | $520 \times 3 \div 4$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $£ 390$ | A1 |  |
| 9(b) | Their(a)/520 $\times 100$ | M1 | $\frac{3}{4} \times 100$ |
|  | 75 | A1ft |  |

Allow embedded unless contradicted when M marks only

| $\mathbf{1 0}(\mathbf{a})$ | 35 | B 1 |  |
| :--- | :--- | :---: | :--- |
| $\mathbf{1 0 ( b )}$ | $4 x=5+7$ | M 1 |  |
|  | 3 | A 1 |  |
| $\mathbf{1 0 ( c )}$ | $5 y+11=3 y+21$ | M 1 | $5 y / 3+11 / 3=y+7,1.6 y+3.6=y+7$ <br> $1.7 y+3.7=y+7$ <br> allow 1 error on $1^{\text {st }}$ or $2^{\text {nd }}$ line |
|  | $5 y-3 y=21-11$ | DM 1 | $\frac{5}{3} y-y=7-\frac{11}{3}$ |
|  | 5 | A 1 |  |


| $\mathbf{1 1 ( a )}$ | rotation | B1 | B0 for turned |
| :--- | :--- | :---: | :--- |
|  | $90^{\circ}$ clockwise or $270^{\circ}$ or $-90^{\circ}$ | B1 | B0 for $90^{\circ}$ right |
|  | Centre $(0,0)$ | B1 | About $(0,0)$ |
| $\mathbf{1 1 ( b )}$ | any reflection of shaded triangle | M1 |  |
|  | correct triangle | A1 | corners $(-3,1)(-4,1)(-3,3)$ |


| $\mathbf{1 2 ( a )}$ | More healthy eaters at gym | B1 | Biased results oe |
| :--- | :--- | :---: | :--- |
| $\mathbf{1 2 ( b )}$ | Cannot distinguish between | B1 | Should only ask 1 question not 2 at once oe <br> no indication what is a fruit or a sweet <br> no indication of amounts eaten to qualify |
| $\mathbf{1 2 ( c )}$ | Too few | B1 | it may be biased oe |


| $\mathbf{1 3 ( a )}$ | $3.2 \times 12500 / 100$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $12500+$ their 400 | DM1 | $103.2 \times 12500 / 100$ gets M2 |
|  | 12900 | A1 |  |
| $\mathbf{1 3 ( b )}$ | $12198-11400(=798)$ | M1 | $12198 / 11400(=1.07)$ |
|  | Their $798 / 11400 \times 100$ | DM1 | $(1.07-1) \times 100$ |
|  | 7 | A1 |  |


| $\mathbf{1 4}$ | $x=7$ | B1 |  |
| :--- | :--- | :---: | :--- |
|  | $2 y+1+8=17$ | M1 |  |
|  | $y=4$ | A1 |  |
|  | $z=17-2 y-x$ or 2 | B1ft |  |


| $\mathbf{1 5}$ | $360 / 5$ | M1 | $540 / 5$ |
| :--- | :--- | :---: | :--- |
|  | 72 or 108 seen | A1 |  |
|  | $(180-$ their108 $) / 2$ | M1 | $108-72$ or $180-72-72$ |
|  | 36 | A1 |  |


| $\mathbf{1 6}$ | Stays the same |  |  |
| :---: | :--- | :---: | :--- |
|  | Shows ability to find median as <br> middle value | M1 | This can be shown for 20 pieces or 21 pieces <br> of data |
|  | Identifying median as 19 from <br> 20 pieces of data | A1 | 19 quoted or implied as median M1A1 |
|  | Identifying 19 as the median <br> from 21 pieces of data | A1 |  |


| $\mathbf{1 7 ( a )}$ | $1 / 2$ п $1.4^{2}$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | 3.077 to 3.079 penalise incorrect <br> working if seen 3.08 | A1 | 6.15 to 6.16 SC 1 |
|  | 3 or 3.1 | B1ft | Their answer rounded to 1sf or 2sf <br> Allow 3 only if M1 awarded <br> $0.5 \pi 1.4^{2}=3$ gets 3 marks |
| $\mathbf{1 7 ( b )}$ | Their(a) x 0.5 | M1 | x50 after attempt to convert to cm ${ }^{2}$ <br> eg, 300x50 |
|  | $1.5(\ldots)$ | A1ft |  |


| $\mathbf{1 8}$ | Trial above 2.8796 | M1 | 2 gives 6, 3 gives 24 |
| :---: | :--- | :---: | :--- |
|  | Trial below 2.8796 | M1 | 2.9 gives 21.489, all values to at least 1dp <br> rounded or truncated |
|  | Testing a value that justifies 2.9 <br> as answer | DM1 | $2.5 \rightarrow 13.125,2.6 \rightarrow 14.976,2.7 \rightarrow 16.983$ <br> $2.8 \rightarrow 19.152,2.85$ gives 20.299 |
|  | $x=2.9$ | A1 | Dep on any M mark |


| $\mathbf{1 9}$ | Trying any cube root | B1 | Must be accurate to at least 1dp |
| :---: | :--- | :---: | :--- |
|  | Number $\leq-1$ or $0 \leq$ number $\leq 1$ | B1 | Cube root must be seen |


| 20(a) | Min 341.5 | B1 | SC1 for 3415 and 3425, transposed SC1 |
| :--- | :--- | :---: | :--- |
|  | Max 342.5 | B1 | $342.49 \ldots$ any indication of recurring |
| 20(b) | $12 \times$ their min | B1ft | 4098 |
|  | $12 \times$ their max | B1ft | 4110 |


|  | trial and improvement is 0 |  |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{2 1}$ | 1 st $-2^{\text {nd }}$ | M1 | $6 y=-3$ allow 1 error eg, $1.2 y=-36 y=3$ <br> $2-3.6 y=5+2.4 y$ allow 1 error or <br> $2.4 \mathrm{equation(1)+3.6equation(2)}$ |
|  | $y=-0.5$ or $x=3.8$ | A1 |  |
| $y=-0.5$ and $x=3.8$ | A1ft | Must have both. <br> Allow reversed if both seen correct in <br> working <br> ft if M1 awarded |  |


| 22(a) | line and arc any radius | B1 |  |
| :---: | :--- | :---: | :--- |
|  | 2nd arc same radius and 2nd <br> line | B1 | $\pm 2^{\circ}$ accuracy |
| 22(b) | Both arcs intersecting <br> Correct radius and region <br> shaded or indicated | B2 | B1 for either arc, correct radius $\pm 2 \mathrm{~mm}$ |


| $\mathbf{2 3}$ | Attempt to find gradient | M1 | Accept $2,-2$ or $1 / 2$ for M1 |
| :--- | :--- | :---: | :--- |
|  | Correct gradient $(-1 / 2)$ | A1 |  |
|  | Line of form $y=m x+1 / 2$ | B1 | Accept $2 y+a x=1$ for SC1 <br> $2 y+x=1$ gets all 3 marks |


| $\mathbf{2 4}$ | sight of 0.55 or 55 | B1 | $55 \%=31.9 \mathrm{M} 1$ |
| :--- | :--- | :---: | :--- |
|  | $31.90 \div 0.55$ | M1 | $1 \%=0.58 \mathrm{~A} 1$ |
|  | $58(.00)$ | A1 |  |


| 25(a) | Sight of tan unless alternative <br> method used | M1 |  |
| :--- | :--- | :---: | :---: |
|  | $\operatorname{Tan}^{-1}(5.59 / 1.5)$ | DM1 | $90^{\circ}-\tan ^{-1}(1.5 / 5.59), 1.5 \tan 70$ and $1.5 \tan 80$ |
|  | $74 .(98)$ or $75^{\circ}$ so safe | A1 | $4.1(2)$ and $8.5(1)$ |
| $\mathbf{2 5 ( b )}$ | Sight of cos | M1 |  |
|  | $4 \times \cos 80$ | DM1 |  |
|  | 0.69 | A1 | 0.7 with working |


| $\mathbf{2 6}$ | $(2$ or $1.998(\ldots)) \times 10^{10}$ | B2 | B1 for $10^{10}$ B1 for 1.9 or 1.99 |
| :---: | :--- | :--- | :--- |


| 27(a) | $(48+30+81) \div 3$ | M1 | $159 / 3$ |
| :--- | :--- | :--- | :--- |
|  | 53 | A1 | 53 with incorrect or no working no marks |
| $\mathbf{2 7 ( b ) ( i ) ~}$ | 88 | B1 | Answer in table unless contradicted on <br> answer line |
| $\mathbf{2 7 ( b ) ( i i ) ~}$ | $(93+114+57) / 3=88$ | B1 | $3 \times$ (their88) $-(114+57)$ |

