ASSESSMENT and
OUALIFICATIONS

# General Certificate of Secondary Education 

## Mathematics 3301 Specification A

Paper 2 Higher Tier

## Mark Scheme <br> 2006 examination - November series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

## The following abbreviations are used on the mark scheme:

M Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
oe $\quad$ Or equivalent.
eeoo Each error or omission.

## Paper 2H

| $\mathbf{1}$ | S, A, N | B3 | -leeoo |
| :---: | :--- | :---: | :--- |


| $\boldsymbol{2}$ | $30 \div 20(=1.5)$ | M1 | oe |
| :---: | :--- | :---: | :--- |
|  | Their $\left(\frac{30}{20}\right) \times 2.78$ | M1dep | $2.78 \div 0.666 .$. oe M2 |
|  | 4.17 | A1 | 4.2 |


| 3 | Digits 5 or $52 \div(360-363)$ | M1 | $13774-14444$ M1 |
| :--- | :--- | :---: | :--- |
|  | 14000 | A1 | Accept 14300,14400 |


| 4(a) | $3 x-6 \leq 9$ | M1 | $x-2 \leq 3 \quad \text { M1 }$ <br> $3 x-6=9$ or $x-2=3$ is M0 unless inequality recovered <br> Allow one error in first or second answer |
| :---: | :---: | :---: | :---: |
|  | $3 x \leq 9+6(=15)$ | M1 | $x \leq 3+2(=5)$ |
|  | $x \leq 5$ | A1 | $\begin{aligned} & \mathrm{SC} x=5 \quad x \geq x>5 \mathrm{~B} 1 \\ & x=\leq 5 \text { is M2, A } 0 \\ & x=<5 \text { is M2, A } 0 \\ & x<5 \mathrm{M} 2, \mathrm{~A} 0 \end{aligned}$ <br> $x$ Must be on answer line <br> Embedded $3(5-2) \leq 9$ oe SC 1 |
| 4(b) | Left Boundary <br> $-3 \leq$ open circle $<-2 \quad$ or $-3<$ closed circle $\leq-2$ <br> Right Boundary <br> Closed circle on 3 or line beyond 3 with any termination (eg, arrow, circle, nothing) | B1 | Boundaries must be joined with a line Ignore any markings on intermediate points |


| $\mathbf{5}$ | Evidence of adding at least two <br> frequencies | M1 | $18,52, \ldots(92,100)$ |
| :---: | :--- | :---: | :--- |
|  | $40<m \leq 80$ | A1 | Answer only with no working or no <br> contradictory working M1, A1 |
| Answer from incorrect working |  |  |  |
| (eg, mean $\left.=75.2, \frac{160}{2}=80\right), \mathrm{M} 0, \mathrm{~A} 0$ |  |  |  |


| 6(a) | 40 | B1 | $150 \div 100(\times 100)=1.3636 \ldots(136.36)$ is <br> M0 unless 1 or $100 \%$ subtracted, then it is M2 |
| :---: | :---: | :---: | :---: |
|  | $40 \div 110 \times 100$ | M1 |  |
|  | 36.4, 36.36.... | A1 | $36 \frac{4}{11} \%$ accept $36 \%$ if M1 awarded |
| 6(b) | $120 \%=110$ | M1 | $110 \div 1.2$ is M2 |
|  | $1 \%=0.9166 \ldots$ | A1 |  |
|  | $100 \%=92,91.7,91.6 \ldots$ | A1 | $\begin{aligned} & \text { NB } 20 \times \frac{100}{110}=0.909 \ldots \\ & 0.909 \times 20=18.18 \\ & 110-18.18=92 \mathrm{M} 0 \end{aligned}$ <br> T \& I has to get 91.6-91.7 <br> $136.4 \%$ seen after 36.4 is 2 marks out of 3 |


| 7 | $20=\frac{15}{v}$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $v=0.75$ | A 1 |  |
|  | Their ' 0.75 ' $=0.6 \times$ length | M1 | Must be calculated value <br> eg, $\frac{20}{15}=1.33 \ldots, 1.33 \div 0.6=2.22 \ldots$ <br> or $300 \div 0.6=500$ are M0, A0, M1 A0 |
|  | 1.25 | A 1 |  |


| 8(a) | $\left(x^{2}=\right) 45^{2}+40^{2}$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $\sqrt{ } 3625$ | M1dep | Mark is for squaring, adding and square rooting $\sqrt{ }\left(45^{2}+40^{2}\right)$ is M2 <br> M2 for $45 \div \sin 48.366$ oe |
|  | 60.2... | A1 | 60 with working |
|  | 60 | B1ft | For rounding Their answer to an integer |
| 8(b) | $\begin{aligned} & \operatorname{Tan} y=\frac{45}{40} \\ & \operatorname{Sin} y=\frac{45}{\operatorname{Their}(\mathrm{a})} \\ & \operatorname{Cos} y=\frac{40}{\text { Their(a) }} \end{aligned}$ | M2 | M1 for fraction wrong way round <br> M1 for other angle using correct trigonometry. then M1 for subtract from $90^{\circ}$ |
|  | $48.1^{\circ}$ to $48.6^{\circ}$ | A1 | $48^{\circ}$ or $49^{\circ}$ with working <br> Grads 53.74, Rads 0.844 both M2, A0 |


| 9(a)(i) | C | B3 | -1eeoo |
| :---: | :---: | :---: | :---: |
| 9(a)(ii) | F |  |  |
| 9(a)(iii) | D |  |  |
| 9(b) | $830 \div 10(\times 11)$ | M1 | oe 83 |
|  | 913 | A1 |  |


| $\mathbf{1 0 ( a )}$ | Lowest 'whisker' 8 <br> Lower quartile 18 <br> Median 25 <br> Upper quartile 32 <br> Highest 'whisker' 57 | -leeoo plotted to half square <br> Failure to draw box is 1 error <br> Failure to draw 'whisker' is 1 error |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 0 ( b )}$ | $25 \%$ | B1 |  |


| 11(a) | $4 p+4 r=7 r+11$ | M1 | Allow one error eg, $4 p+r=7 r+11$ $p+r=\frac{7 r+11}{4} \text { is } \mathrm{M} 1, \mathrm{~A} 1$ |
| :---: | :---: | :---: | :---: |
|  | $4 p=3 r+11$ | A1 |  |
|  | $p=\frac{3 r+11}{4}$ or $\frac{1}{4}(3 r+11)$ | A1ft | Dividing by 4 must be done correctly eg, $3 r+11 \div 4$ is A0 but $(3 r+11) \div 4$ is A1 ft if M1 awarded ie, $p=(6 r+11) \div 4$ oe eg, $p=\frac{7 r+11}{4-r}$ A2 |
| 11(b) | $\begin{array}{ll} (3 x+5 y=4) & 6 x+10 y=8 \\ 30 x+5 y=130 & (6 x+y=26) \end{array}$ | M1 | oe Allow error in 1 term <br> M1 for substituting one equation into the other |
|  | $27 x=126 \quad 9 y=-18$ | M1dep | oe Elimination from Their equations at least one term correct |
|  | $x=4 \frac{2}{3} \quad$ and $\quad y=-2$ | A1 | oe $(4.66,-2)(4.67,-2)$ <br> SC1 for correct answer with no working or using trial and improvement. |


| 12(a) | Convincing algebra | B1 | Must see $(p+q)(p+q)=p(p+q)+q(p+q)$ or box method and $p^{2}+p q+p q(q p)+q^{2}$ |
| :---: | :---: | :---: | :---: |
| 12(b) | $(2 x+3+x-1)^{2}$ | M1 | $4 x^{2}+12 x+9+2\left(2 x^{2}+x-3\right)+x^{2}-2 x+1$ <br> Allow one sign or coefficient error <br> For middle term accept $(4 x+6)(x-1)$ or $(2 x+3)(2 x-2)$ |
|  | $(3 x+2)^{2}$ | A1 | $4 x^{2}+12 x+9+4 x^{2}+2 x-6+x^{2}-2 x+1$ |
|  | $9 x^{2}+12 x+4$ | A1ft | ft if M1 awarded and no further errors |


| 13 | $[(2 x-1)(2 x+1)]=4 x^{2}-1$ | M1, A1 | or $(4 x y-2 y)(2 x+1) \quad$ M1 Allow one error <br> Lack of brackets is 1 error but no ft possible <br> $8 x^{2} y-4 x y+4 x y-2 y$ |
| :---: | :--- | :---: | :--- |
|  |  | A1ft | ft if M1 awarded no further errors <br> $\mathrm{SC} 216 y^{2} x^{2}-4 y^{2}$ |


| $\mathbf{1 4 ( a )}$ | $A B C=65$ | B 1 |  |
| :---: | :--- | :---: | :--- |
|  | $A D C=115$ | B 1 ft | $180-(A B C)$ |
|  | $A C O=90-56(=34)$ and <br> $B A C=65$ or $A B C=56$ | B 1 | Many different methods |
|  | $O B A=360-65-230-34$ | M1 | Complete method <br> Angles must be identified or marked on diagram <br> (Allow incorrect angles for M1) |
|  | $(O B A)=31$ | A1 |  |


| 15(a) | $\sum(\mathrm{fd} \times$ width | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $6,26,19,17,32$ | A1 | Allow 4 out of 5 |
|  | $=100$ | A1 |  |
| $\mathbf{1 5 ( b ) ~}$ | $\sum(\mathrm{fm})$ | M1 | Use of incorrect $m$ <br> eg, ucb or lcb consistently allow M1 |
|  | $10 \times 6+30 \times 26+45 \times 19+55 \times$ <br> $17+80 \times 32$ <br> $60,780,855,935,2560$ | A1ft | A1 for correct combination (allow one error) <br> or identifying at least 4 out of 5 values <br> ft Their values from (a) |
|  | 5190 | A1ft | A1ft |
|  | 51.9 | ft Their $\sum \mathrm{f}$ if M1 awarded in (a) and also $\sum \mathrm{mf}$ <br> if M1 awarded in (b) |  |


| 16(a) | $x^{2}=8^{2}+7^{2}-2 \times 7 \times 8 \times \cos 48^{\circ}$ | M1 | $1 \times \cos 48$ implied M1 |
| :---: | :---: | :---: | :---: |
|  | $x^{2}=38 .(\ldots \ldots)$ | A1 | Grads $x^{2}=31.355$ |
|  | $(x)=$ root any value 38.1 or better <br> eg, 6.168..., 6.169..., 6.17, 6.2 | A1ft | Grads $x=5.6$ is 2 marks out of 3 Allow ft on one arithmetical error |
| 16(b) | $\frac{\sin x}{7}=\frac{\sin 48}{6.17}$ | M1 | ft Their ' 6.17 ' from (a) $7^{2}={ }^{\prime} 6.17^{\prime 2}+8^{2}-2 \times{ }^{\prime} 6.17 ’ \times 8 \times \cos x$ |
|  | $\sin x=\frac{7 \times \sin 48}{6.17}(=0.8432)$ | M1dep | Grads 0.8557 $\operatorname{Cos} x=\frac{{ }^{\prime} 6.17^{\prime 2}+8^{2}-7^{2}}{2 \times^{\prime} 6.17^{\prime} \times 8}(=0.5374)$ |
|  | $x=57.5^{\circ}$ | A1ft | ft Their value from (a) <br> Grads $x=65.4 \frac{3}{3}$ <br> Answer to nearest degree after working is OK |

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| $C \alpha d^{2}$ or $C=k d^{2}$ | M 1 |  |
| :--- | :---: | :--- |
| $k=50 \div 3600=(0.013888 \ldots)$ | A 1 | $50 \div 60^{2} \times 90^{2} \mathrm{M} 2$ |
| $(C)=£ 112.50$ | A 1 | 112.5 is A0 |


| 18 | Mid point (5, 8) | B1 |  |
| :---: | :---: | :---: | :---: |
|  | Gradient $A B=-\frac{1}{3}$ | B1 | Accept any indication eg, 6 across, 2 down |
|  | Attempt to find gradient $M C$ or 'stepping' from $M$ to $C$ | M1 | M1 for using 'Their gradient' |
|  | Valid conclusion with justification. eg, No because gradient $M C$ not 3 | A1 | Accept any indication $\text { eg, }(5,8) \text { plus }(3,9)=(8,17), m m^{\prime} \neq-1$ |
| 18 Alt | Mid point (5, 8) | B1 |  |
|  | Use of Pythagoras | M1 |  |
|  | Three correct lengths $\sqrt{109}, 11, \sqrt{10}$ | A1 |  |
|  | Correct conclusion at least 2 correct values | A1 |  |

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| $3 y x+2 x=x+3$ | M1 | $3 y+2=1+\frac{3}{x}$ |
| :--- | :--- | :--- |
| $3 y x+x=3$ | A1 | $3 y+1=\frac{3}{x}$ |
| $x(3 y+1)=3$ | M1 | $\frac{1}{(3 y+1)}=\frac{x}{3} \quad x(3 y-1)=1$ |
| $x=\frac{3}{3 y+1}$ | A1ft | oe $x$ must be seen <br> eg, $x=1 \div(3 y-1)$ |


| 20 | $55 \leq($ speed $<65)$ | B1 | 55 alone gets B1 <br> Ignore incorrect upper limit |
| :---: | :---: | :---: | :---: |
|  | $14500 \leq$ file $<15500$ (15499.9) | B1 | 15500 (15499.9) alone gets B1 Ignore incorrect upper limit |
|  | Their 'greatest file' $\div$ Their 'minimum speed' | M1 | Attempts at limits must be made |
|  | 282, 281.8... | A1ft | ft if M1 awarded and attempt to find lower speed and upper file made and one correct <br> NB check answer comes form correct work ft answer must be at least 3 sf |

$\left.\begin{array}{|c|l|c|c|}\hline 21 & \text { (area base) }=\frac{1}{2} \times 5 \times 5 \times \sin 60 & \text { M1 } & \text { oe eg, Use of trigonometry or } \\ \text { Pythagoras but must give full method } \\ \text { to find area of a triangle } \\ \text { Height of triangle }=4.33\end{array}\right]$

| 22(a) | $x^{2}+4$ | B1 |  |
| :--- | :--- | :--- | :--- |
| 22(b) | $2 x^{2}$ | B1 |  |
| 22(c) | $(x-1)^{2}$ | B1 | oe |


| 23(a)(i) | $-3 \mathbf{a}+1 \frac{1}{2} \mathbf{b}$ | B1 | oe |
| :---: | :---: | :---: | :---: |
| 23(a)(ii) | $\mathrm{OX}=\mathrm{OA}+\mathrm{AX}$ | M1 | oe |
|  | $1 \frac{1}{2} \mathbf{a}+1 \frac{1}{2} \mathbf{b}$ | A1 | oe |
| 23(a)(iii) | $\mathrm{AZ}=\mathrm{AO}+\mathrm{OZ}$ | M1 | oe M1 for $-3 \mathbf{a}+\frac{2}{3}$ (Their OX) |
|  | b-2a | A1 | oe |
| 23(b) | $\mathrm{ZY}=\frac{1}{2} \mathbf{b}-\mathbf{a}$ | M1 | Their 'AY' - Their 'AZ' |
|  | 2:1 | A1ft |  |

