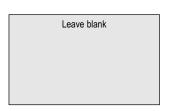
| Surname           |     |  | Other | Names   |            |  |  |
|-------------------|-----|--|-------|---------|------------|--|--|
| Centre Number     |     |  |       | Candida | ate Number |  |  |
| Candidate Signatu | ire |  |       |         |            |  |  |



ALIFICATIONS

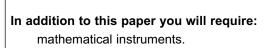
ALLIANCE

General Certificate of Secondary Education June 2004

## MATHEMATICS (SPECIFICATION A) 3301/1H Higher Tier Paper 1 Non-Calculator



Tuesday 8 June 2004 1.30 pm to 3.30 pm





Time allowed: 2 hours

You must not use a calculator.

### **Instructions**

- Use blue or black ink or ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions in the spaces provided.
- Do all rough work in this booklet.

### Information

- The maximum mark for this paper is 100.
- Mark allocations are shown in brackets.
- Additional answer paper, graph paper and tracing paper will be issued on request and must be tagged securely to this answer booklet.
- The use of a calculator is **not** permitted.

### **Advice**

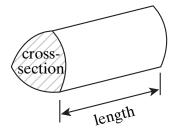
• In all calculations, show clearly how you work out your answer.

| For Exam            | iner's l | Jse  |
|---------------------|----------|------|
| Pages               |          | Mark |
| 3                   |          |      |
| 4 – 5               |          |      |
| 6 – 7               |          |      |
| 8 – 9               |          |      |
| 10 – 11             |          |      |
| 12 – 13             |          |      |
| 14 – 15             |          |      |
| 16 – 17             |          |      |
| 18 – 19             |          |      |
| 20 – 21             |          |      |
| 22                  |          |      |
| TOTAL               |          |      |
| Examiner's Initials |          |      |

### Formulae Sheet: Higher Tier

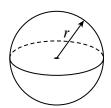
You may need to use the following formulae:

**Volume of prism** = area of cross-section  $\times$  length



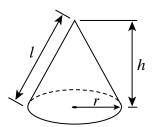
**Volume of sphere** = 
$$\frac{4}{3} \pi r^3$$

**Surface area of sphere** =  $4 \pi r^2$ 



**Volume of cone** = 
$$\frac{1}{3} \pi r^2 h$$

Curved surface area of cone =  $\pi r l$ 

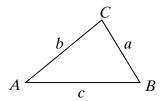


In any triangle ABC

**Area of triangle** = 
$$\frac{1}{2}ab \sin C$$

**Sine rule** 
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

**Cosine rule**  $a^2 = b^2 + c^2 - 2bc \cos A$ 



### The Quadratic Equation

The solutions of  $ax^2 + bx + c = 0$ , where  $a \ne 0$ , are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

# Answer all questions in the spaces provided.

3

| 1 | Tom, Sam and Matt are counting drum beats.   |
|---|--|
|   | Tom hits a snare drum every 2 beats.   |
|   | Sam hits a kettle drum every 5 beats.  |
|   | Matt hits a bass drum every 8 beats.   |
|   | Tom, Sam and Matt start by hitting their drums at the same time.  How many beats is it before Tom, Sam and Matt <b>next</b> hit their drums at the <b>same</b> time? |
|   |  |
|   |  |
|   |  |
|   |  |
|   |  |
|   |  |
|   | Answer beats (2 marks)   |
|   |  |
|   |  |
| 2 | Simplify   |
|   | (a) $w^6 \times w^2$   |
|   |  |
|   |  |
|   | Answer (1 mark)  |
|   | (b) $x^3 \div x^5$   |
|   | (b) $x - x$  |
|   |  |
|   | Answer (1 mark)  |
|   | 2.2  |
|   | (c) $(y^3)^2$  |
|   |  |

Answer .....



(1 *mark*)

3 Use approximations to estimate the value of  $\frac{316 \times 4.03}{0.198}$ 

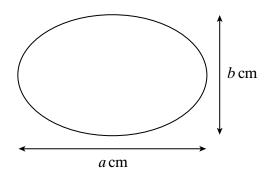
You **must** show your working.

| • | • | • | • | • | ••••• | • |
|---|---|---|---|---|-------|---|
|   |   |   |   |   |       |   |
|   |   |   |   |   |       |   |



| Answer | (3 marks) |
|--------|-----------|

4 The diagram shows an ellipse of width a cm and height b cm.



One of the following is a formula for the area of the ellipse.

Formula 1  $\pi(a+b)$ 

Formula 2  $\pi ab$ 

Formula 3  $\pi a^2 b^2$ 

(a) Which is the correct formula?

Answer ...... (1 mark)

(b) Explain how you can tell that this formula is correct.

(1 mark)

| 5 | Here are six numbers wr                            | tten in standard     | form.                |                    |                      |
|---|--|----------------------|----------------------|--------------------|----------------------|
|   | $2.6 \times 10^5$ $1.75 \times 10^6$               | $5.84 \times 10^{0}$ | $8.2 \times 10^{-3}$ | $3.5\times10^{-1}$ | $4.9 \times 10^{-2}$ |
|   | (a) Write down the large                           | gest number.         |                      |                    |                      |
|   |  | Answer               |                      |                    | (1 mark)             |
|   | (b) Write down the sm                              | allest number.       |                      |                    |                      |
|   |  | Answer               | •••••                | •••••              | (1 mark)             |
|   | (c) Write $4.9 \times 10^{-2}$ as                  | an ordinary num      | ber.                 |                    |                      |
|   |  | Answer               |                      |                    | (1 mark)             |
|   | (d) Work out $2.6 \times 10^5$ Give your answer is |                      |                      |                    |                      |
|   |  |                      | ••••••               | •••••              |                      |
|   |  | Answer               |                      |                    | (1 mark)             |
| 6 | Make $p$ the subject of the                        | ne formula u         | t = 5p + 40          |                    |                      |
|   |  |                      |                      |                    |                      |
|   |  |                      |                      |                    |                      |
|   | 1  | Answer $p = \dots$   |                      |                    | (2 marks)            |

5

# TURN OVER FOR THE NEXT QUESTION



7 (a) Complete the table of values for  $y = 2x^2 - 4x - 1$ 

| х | -2 | -1 | 0  | 1 | 2  | 3 |
|---|----|----|----|---|----|---|
| У | 15 |    | -1 |   | -1 | 5 |

| <br>   |          | •• |
|--------|----------|----|
| <br>   |          | •• |
|        |          |    |
| •••••• |          | •• |
| <br>   | (2 marks |    |

(b) On the grid opposite, draw the graph of  $y = 2x^2 - 4x - 1$  for values of x from -2 to +3.

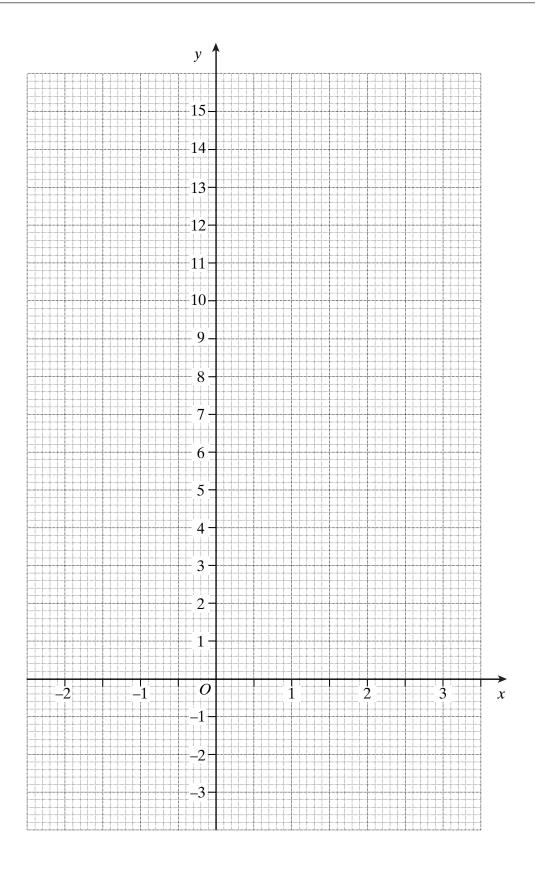
(2 marks)

(c) An approximate solution of the equation  $2x^2 - 4x - 1 = 0$  is x = 2.2

| (1) | Explain how you can find this from the graph. |          |
|-----|---|----------|
|     |   |          |
|     |   |          |
|     |   | (1 mark) |

(ii) Use your graph to write down another solution of this equation.

Answer  $x = \dots (1 mark)$ 



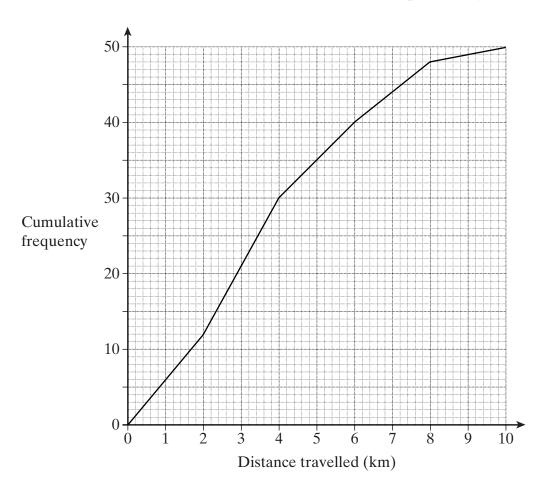


**8** The table shows the distances travelled to school by 50 pupils living in a town.

| Distance travelled, d (km) | Frequency |
|----------------------------|-----------|
| $0 < d \le 2$              | 12        |
| 2 < d ≤ 4                  | 18        |
| 4 < <i>d</i> ≤ 6           | 10        |
| 6 < d ≤ 8                  | 8         |
| 8 < d ≤ 10                 | 2         |

| (a) | Calculate an estimate of the mean distance travelled to school by these pupils. |
|-----|---|
|     |   |
|     |   |
|     |   |
|     |   |
|     |   |
|     |   |
|     | Answer $(5 \text{ marks})$  |

(b) The distances travelled are shown on the cumulative frequency diagram.



Use the cumulative frequency diagram to estimate

| (i) | the | median |
|-----|-----|--------|
| (1) | the | meanan |

Answer ...... km (1 mark)

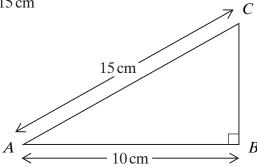
(ii) the interquartile range.

Answer ...... km (2 marks)



9 (a) The diagram shows a right-angled triangle ABC.

 $AB = 10 \,\mathrm{cm}$  and  $AC = 15 \,\mathrm{cm}$ 



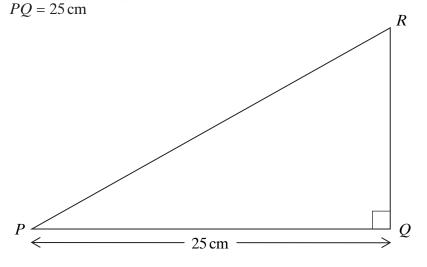
Not drawn accurately

Calculate the length of BC.

Leave your answer as a square root.

| ••••• |      | • |
|-------|------|---|
|       |      |   |
|       |      | •••••                                   |
|       |      |   |
| ••••• |      |   |
|       |      |   |
| Answe | r cm | (3 marks)                               |

(b) Triangle PQR is similar to triangle ABC. Angle CAB = angle RPQ.

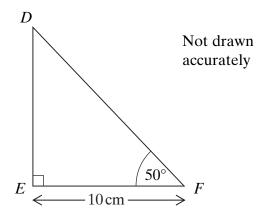


Not to scale

Work out the length of PR.

Answer ...... cm (3 marks)

(c) The diagram shows a right-angled triangle DEF.  $EF = 10 \, \mathrm{cm}$  Angle  $F = 50^{\circ}$ 



| Angle | Sine  | Cosine | Tangent |
|-------|-------|--------|---------|
| 40°   | 0.643 | 0.766  | 0.839   |
| 50°   | 0.766 | 0.643  | 1.192   |

| Use the table of data to work out the length of $DE$ . |  |
|--|--|
|  |  |
|  |  |
|  |  |
| Answer   |  |

## TURN OVER FOR THE NEXT QUESTION



10 Each of the graphs represents one of the following equations.

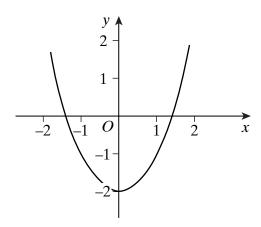
$$A \quad y = 3x + 4$$

$$B \quad 2x + 3y = 12$$

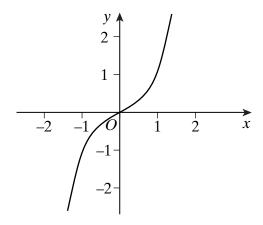
$$C \quad y = x^2 - 2$$

$$D \quad y = x^3$$

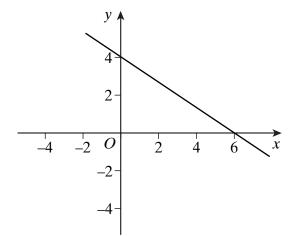
Write down the letter of the equation represented by each graph.



Equation ..... (1 mark)



Equation ..... (1 mark)



Equation ..... (1 mark)

11 Find the equation of the straight line passing through the point (0,5) which is perpendicular to the line

$$y = \frac{2}{3}x + 3$$

**12** (a) Prove that  $0.\dot{5}\dot{8} = \frac{58}{99}$ 

(2 marks)

(b) Hence, or otherwise, express 0.158 as a fraction.

.....

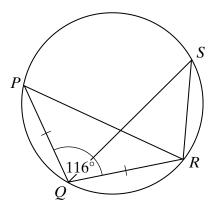
Answer ...... (2 marks)



13 (a) Points P, Q, R and S lie on a circle.

$$PQ = QR$$

$$\widetilde{\text{Angle }PQR} = 116^{\circ}$$



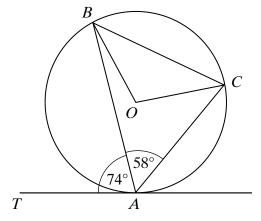
Not drawn accurately

| Explain why angle $QSR = 32^{\circ}$ . |
|--|
|--|

| ••••• | •••••                                   | •••••                                   | •••••                                   |
|-------|---|---|---|
|       |   |   |   |
|       | •••••                                   | •••••                                   | •••••                                   |
|       |   |   |   |
|       | • | • | •••••                                   |
|       |   |   |   |
|       |   |   |   |
| ••••• | • | • | • |

(2 marks)

(b) The diagram shows a circle, centre O. TA is a tangent to the circle at A. Angle  $BAC = 58^{\circ}$  and angle  $BAT = 74^{\circ}$ .



Not drawn accurately

| (1 | i) | Calcu | late | angle | BO | C. |
|----|----|-------|------|-------|----|----|
|----|----|-------|------|-------|----|----|

| ••••• | ••••• | ••••• | ••••• |
|-------|-------|-------|-------|
|       |       |       |       |

Answer Angle  $BOC = \dots$  degrees (1 mark)

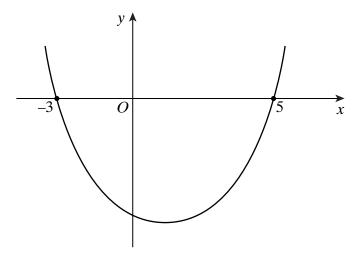
(ii) Calculate angle OCA.

| • • • • |
|---------|
|         |

| <br> | <br> |  |
|------|------|--|
|      |      |  |

| <br> | <br> | <br> |  |
|------|------|------|--|
|      |      |      |  |
|      |      |      |  |
|      |      |      |  |

- Answer Angle  $OCA = \dots$  degrees (3 marks)
- 14 The diagram shows the graph of an equation of the form  $y = x^2 + bx + c$



Not drawn accurately

| Find | the | Vä | alues | of | b | and | С. |
|------|-----|----|-------|----|---|-----|----|
|      |     |    |       |    |   |     |    |

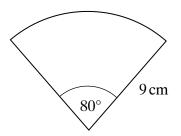
You **must** show your method.

| • | • | ••••• | ••••• | ••••• | ••••• |
|---|---|-------|-------|-------|-------|
|   |   |       |       |       |       |
|   |   |       |       |       |       |
|   |   |       |       |       |       |

Answer  $b = \dots, c = \dots (3 \text{ marks})$ 

marks)

15 The diagram shows a sector of a circle of radius 9 centimetres.



Not drawn accurately

|   |       | the perimeter of the sector. your answer in terms of $\pi$ .        |           |
|---|-------|---|-----------|
|   | ••••• |   |           |
|   | ••••• |   |           |
|   | ••••• |   |           |
|   | ••••• |   | •••••     |
|   | ••••• |   |           |
|   | ••••• |   |           |
|   |       | Answer cm   | (3 marks) |
| 6 | (a)   | Factorise $2n^2 + 5n + 3$   |           |
|   |       |   |           |
|   |       |   |           |
|   |       |   |           |
|   |       | Answer  | (2 marks) |
|   | (b)   | Hence, or otherwise, write 253 as the product of two prime factors. |           |
|   |       |   | •••••     |
|   |       |   |           |
|   |       |   | •••••     |
|   |       | Answer  | (1 mark)  |

|  | be satisf  | ied when col | lecting data for | r a stratified |  |  |
|--|--|--------------|------------------|----------------|--|--|
| (b) A small village has a population The population is classified by a  Age (years)  O-12  Number of people  35  A stratified sample of 50 is plan | •••••  |              |                  |                |  |  |
| (b) A small village has a population The population is classified by a  Age (years) 0-12  Number of people 35  A stratified sample of 50 is plan   | •••••  |              |                  | (1 mark)       |  |  |
| Age (years)  O-12  Number of people  A stratified sample of 50 is plan   |  |              |                  |                |  |  |
| Age (years)  O-12  Number of people  A stratified sample of 50 is plan   | •••••  |              |                  | (1 mark)       |  |  |
| Number of people 35  A stratified sample of 50 is plan   | A small village has a population of 400.  The population is classified by age as shown in the table below. |              |                  |                |  |  |
| A stratified sample of 50 is plan  | 13-24  | 25-40        | 41-60            | 61+            |  |  |
| A stratified sample of 50 is plan  | 58   | 125          | 103              | 79             |  |  |
|  |  |              |                  |                |  |  |
|  | •••••  |              |                  |                |  |  |
|  |  |              |                  |                |  |  |
|  |  |              |                  |                |  |  |
|  | Answer   | 0-12 years   |                  |                |  |  |
|  |  |              |                  |                |  |  |
|  |  |              |                  |                |  |  |
|  |  |              |                  |                |  |  |



| 18 | (a) | (i)   | Factorise $x^2 - 10x + 25$              |
|----|-----|-------|---|
|    |     |       |   |
|    |     |       | Answer                                  |
|    |     | (ii)  | Hence, or otherwise, solve the equation |
|    |     |       | $(y-3)^2 - 10(y-3) + 25 = 0$            |
|    |     |       |   |
|    |     |       |   |
|    |     |       | Answer $y = \dots (2 \text{ marks})$    |
|    | (b) | Simp  | polify $\frac{x^2 - 9}{x^2 + 3x}$       |
|    |     | ••••• |   |
|    |     | ••••• |   |
|    |     | ••••• |   |
|    |     | ••••• |   |
|    |     | ••••• |   |
|    |     | ••••• |   |
|    |     | ••••• |   |
|    |     |       | Answer (3 marks)                        |

| 19 | (a) | n is a positive integer.  |              |
|----|-----|---|--------------|
|    |     | (i) Explain why $n(n + 1)$ must be an even number.                          |              |
|    |     |   |              |
|    |     |   | (1 mark)     |
|    |     | (ii) Explain why $2n + 1$ must be an odd number.                            |              |
|    |     |   | (1 mark)     |
|    | (b) | Expand and simplify $(2n+1)^2$  |              |
|    |     |   |              |
|    |     | Answer(2  | 2 marks)     |
|    | (c) | Prove that the square of any odd number is always 1 more than a multiple of | of 8.        |
|    |     |   | •••••        |
|    |     |   | •••••        |
|    |     |   | •••••        |
|    |     |   | •••••        |
|    |     |   | •••••        |
|    |     | (2  | <br>3 marks) |



| 20 | (a) | Find the values of a and b such that            |
|----|-----|---|
|    |     | $x^2 + 6x - 3 = (x + a)^2 + b$                  |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     | Answer $a = \dots, b = \dots (2 \text{ marks})$ |
|    | (b) | Hence, or otherwise, solve the equation         |
|    | (0) | $x^2 + 6x - 3 = 0$                              |
|    |     | giving your answers in surd form.               |
|    |     | giving your answers in surd form.               |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     |   |
|    |     | Answer  |

21 A crane has a cable with a breaking strain of 5300 kg measured to 2 significant figures.

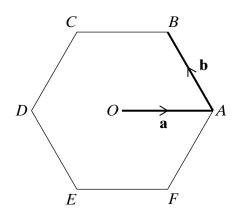
| not break?                         | test number of crates that can be lifted at one time so                    | that the cable do  |
|------------------------------------|--|--------------------|
|                                    |  |                    |
|                                    |  |                    |
|                                    |  |                    |
|                                    |  |                    |
|                                    |  |                    |
|                                    |  |                    |
|                                    |  |                    |
|                                    |  |                    |
|                                    | Answer   | (4 mar             |
|                                    | obability of a 17 year old passing the driving test at the                 |                    |
| Three people are about to take the | chosen at random from the population of 17 year old                        | s in Britain who   |
| Three people are about to take the | e chosen at random from the population of 17 year old<br>eir driving test. | s in Britain who a |
| Three people are about to take the | e chosen at random from the population of 17 year old<br>eir driving test. | s in Britain who a |
| Three people are about to take the | e chosen at random from the population of 17 year old<br>eir driving test. | s in Britain who a |
| Three people are about to take the | e chosen at random from the population of 17 year old<br>eir driving test. | s in Britain who a |
| Three people are about to take the | e chosen at random from the population of 17 year old<br>eir driving test. | s in Britain who a |
| Three people are about to take the | e chosen at random from the population of 17 year old<br>eir driving test. | s in Britain who a |
| Three people are about to take the | e chosen at random from the population of 17 year old<br>eir driving test. | s in Britain who a |



23 ABCDEF is a regular hexagon with centre O.

 $\overrightarrow{OA} = \mathbf{a} \text{ and } \overrightarrow{AB} = \mathbf{b}$ 

Diagram drawn accurately



- (a) Find expressions, in terms of **a** and **b**, for
  - (i)  $\overrightarrow{OB}$

Answer ...... (1 mark)

(ii)  $\overrightarrow{AC}$ 

Answer ...... (1 mark)

(iii)  $\overrightarrow{EC}$ 

Answer ...... (1 mark)

(b) The positions of points P and Q are given by the vectors

$$\overrightarrow{OP} = \mathbf{a} - \mathbf{b}$$
  $\overrightarrow{OQ} = \mathbf{a} + 2\mathbf{b}$ 

(i) Draw and label the positions of points P and Q on the diagram.

(2 marks)

(ii) Hence, or otherwise, deduce an expression for  $\overrightarrow{PQ}$ .

.....

Answer ...... (1 mark)

**END OF QUESTIONS** 

## THERE ARE NO QUESTIONS PRINTED ON THIS PAGE

## THERE ARE NO QUESTIONS PRINTED ON THIS PAGE