ASSESSMENT and
OUALIFICATIONS

# General Certificate of Secondary Education 

## Mathematics 3302 Specification B

Module 3 Tier H 33003H

## Mark Scheme

## 2006 examination - March series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

## The following abbreviations are used on the mark scheme:

M Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
oe $\quad$ Or equivalent.
eeoo Each error or omission.

MODULE 3 HIGHER TIER

| 1(a) | $0.0428669(\ldots)$ | B1 | Allow 0.042867 |
| :---: | :--- | :---: | :--- |
| 1(b) | 0.0429 | B1 ft | ft from value $>3$ sf seen |


| 2(a) | $572 \div 13(=44)$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | their $44 \times 25$ | M1 dep | their $44 \times 12+572$ |
|  | 1100 | A1 | SC1 Answer 528 |
| 2(b) | It depends upon the actual <br> numbers of girls and boys in the <br> year <br> or <br> Gives a number of girls and boys <br> for Year 10 that is not in the ratio <br> $13: 12$ <br> or <br> Gives a ratio for girls to boys that <br> is not 13:12 | B1 | There may be more boys (than girls) <br> There may be fewer girls (than boys) <br> There may be the same number of <br> each gender |


| 3(a) | 3.2 | B1 |  |
| :---: | :---: | :---: | :---: |
| 3(b)(i) | their $3.2 \times 0.8$ evaluated correctly | B1 ft | 2.56 if (a) correct |
| 3(b)(ii) | their (b)(i) $\times 0.8 \times 0.8$ | M1 | 1.6(384) if correct Could be seen in stages ie their $(\mathrm{b})(\mathrm{i}) \times 0.8$ their calculated value $\times 0.8$ <br> If starts again must see $4 \times 0.8^{4}$ |
|  | 3 | A1 | 3 with no working scores M0A0 Do not award A1 for an answer of 3 if there were numerical errors previously <br> SC2 2.0(48) and answer 3 |
| 3(c) | Sight of 0.7(0) | M1 | $70(\%)=1.82$ |
|  | $1.82 \div 0.7$ | M1 | $\begin{aligned} & 1(\%)=1.82 \div 70 \quad(=0.026) \\ & 100(\%)=\text { their } 0.026 \times 100 \\ & \hline \end{aligned}$ |
|  | 2.6 | A1 | SC2 Answer 2.275 SC1 Digits 26 |


| 4(a) | $1.153 \times 10^{6}$ | B1 | Allow $1.153000 \times 10^{6}$ |
| :---: | :--- | :---: | :--- |
| 4(b) | Attempt to add 1 153 000, <br> $4.07 \times 10^{5}$ and 4.6 million | M1 | Numbers all in same form with at <br> least two correct |
|  | $6160000(\mathrm{oe})$ and Yes | A1 | Must have both |


| 5 (a) | $y=\frac{k}{x} \quad$ or $\quad y \alpha \frac{1}{x}$ | M1 | oe |
| :---: | :--- | :--- | :--- |
|  | $\left(16.5=\frac{k}{20}\right)$ | M1 |  |
|  | $k=330 \quad\left(y=\frac{330}{x}\right.$ oe $)$ | A1 | Only need the equation if have not <br> seen $y=\frac{k}{x}$ earlier |
| $5(\mathrm{~b})$ | $x=\frac{\text { (their } k)}{75}$ | M1 |  |
|  | 4.4 | A1 |  |


| 6 | 315 <br> (Allow 314.999...) | B1 | Ignore 305 if seen as well |
| :---: | :--- | :---: | :--- |
| 49.5 | B1 | Ignore 50.5 if seen as well |  |
|  | $\frac{\text { their max miles }}{\text { their min litres }}$ | M1 | $\frac{315}{49.5}$ if correct |
| $6.3636363636 \ldots$ | Allow 6.3, 6.4, 6.363, 6.36, 6.364 <br> etc provided there is evidence to <br> support these answers <br> (B2 M1 awarded) <br> Always check the working <br> eg $\frac{314.9}{49.5}=6.36(2$ dp) <br> scoring B0B1M1A0 |  |  |


| 7 | $2 \sqrt{ } 3 \sqrt{ } 3(+) 2 \sqrt{ } 3 \sqrt{ } 8$ | M1 | $2 \sqrt{9}(+) 2 \sqrt{ } 3 \sqrt{ } 8$ or <br> $2 \sqrt{9}(+) 2 \sqrt{24}$ or <br> $2 \sqrt{9}(+) 2 \sqrt{3} \times 2 \sqrt{2}$ |
| :---: | :--- | :---: | :--- |
|  | $6(+) 2 \sqrt{ } 24$ | A1 | $6(+) 2 \sqrt{ } 3 \times 2 \sqrt{ } 2$ |
|  | $6+4 \sqrt{ } 6$ | A1 | SC1 6 or $4 \sqrt{ } 6$ seen |


| 8 | Sight of 0.85 or 1.224 | M1 | $85 \%$ or $122.4 \%$ |
| :---: | :--- | :---: | :--- |
|  | $1.224 \div 0.85$ | M1 dep | $(=1.44)$ |
|  | $\sqrt{ }$ their 1.44 | M1 dep | $(=1.2)$ |
|  | 20 | A1 | SC3 Answer 2 <br> SC2 Answer 44 |


| Alt 8 | Chooses a 2003 pay value <br> eg 1000 <br> $(1000) \times 0.85$ <br> $(1000) \times 1.224$ | M1 | or finds $15 \%$ then subtracts or <br> finds $22.4 \%$ then adds |
| :--- | :--- | :---: | :--- |
| $(1224) \div(850)$ | M1 dep | $(=1.44)$ |  |
| $\sqrt{(122 e i r ~} 1.44$ | M1 dep | $(=1.2)$ |  |
| 20 | A1 | SC3 Answer 2 <br> SC2 Answer 44 |  |


| 9 | $2(\times) 54$ or $3(\times) 36$ | M1 | Using 2 or 3 in valid method <br> eg factor tree <br> Do not award for a list of all factors <br> even if in product pairs |
| :---: | :--- | :---: | :--- |
|  | $2(\times) 2(\times) 3(\times) 3(\times) 3$ | A1 | Condone use of 1 |
|  | $2^{2} \times 3^{3}$ | A1 | Do not allow factor of 1 |


| $10(\mathrm{a})$ | $3.97 \times 10^{-7}$ | B1 |  |
| :--- | :--- | :---: | :--- |
| $10(\mathrm{~b})$ | $15000 \times 10^{8}$ | B1 | or correct answer in any form |
|  | $1.5 \times 10^{12}$ | B1 ft | ft from value seen |
| $10(\mathrm{c})$ | Sight of 0.75 or $10^{-4}$ or correct <br> answer in any form | B1 | eg 0.000075 |
|  | $7.5 \times 10^{-5}$ | B1 | SC1 Answer $7.5^{-5}$ |


| 11 | $\frac{7}{4}(\div) \frac{15}{11}$ | M1 | Conversion of both to improper <br> fractions (one fraction correct) |
| :---: | :--- | :---: | :--- |
|  | their $\frac{7}{4} \times$ their $\frac{11}{15}$ | M1 dep | Change to multiplication and <br> inversion of second fraction |
| $\frac{77}{60}$ | A1 | $1 \frac{17}{60}$ | If correct answer converted <br> to mixed number <br> incorrectly regard as <br> further work |


| 12(a) | -5 <br> 4 | B1 <br> B1 |  |
| :--- | :--- | :---: | :--- |
| 12(b) | Points plotted accurately | B1 ft | ft their table of values $\pm \frac{1}{2}$ square <br> vertically \& horizontally |
| Smooth curve | B1 ft | ft their plotted points $\left( \pm \frac{1}{2}\right.$ square <br> diagonally) but curve must look like <br> a parabola |  |
| 12(c) | -2 and (1.5) | B1 ft | Must have -2 <br> $\mathrm{ft} \mathrm{their} \mathrm{graph} \mathrm{for} \mathrm{other} \mathrm{value} \mathrm{(which}$ <br> must not be an integer) <br> Must have exactly 2 solutions |
| 12(d) | Draws $y=2 x+1$ correctly | B1 | Must have 2 values <br> Coordinates given B0 <br> Dependent on first B1 |
|  | $2 \leq x \leq 2.3$ and $-1.8 \leq x \leq-1.5$ | B1 dep |  |


| 13 | $5 \sqrt{ } 2(-\sqrt{ } 2=4 \sqrt{ } 2)$ | B1 | If attempts to square the bracket |
| :---: | :--- | :---: | :---: |
|  | $\sqrt{2} 2500 \pm \sqrt{ } 50 \sqrt{ } 2 \pm \sqrt{ } 50 \sqrt{ } 2 \pm \sqrt{4}$ M1 |  |  |
|  | 32 | B1 |  |
| 32 | A1 |  |  |


| 14(a) | $2(\times) \frac{1}{25}(\times) 1$ | B3 | 1 mark for each value Allow 0.04 for $5^{-2}$ <br> Do not allow $\frac{1}{5^{2}}$ |
| :---: | :---: | :---: | :---: |
|  | $\frac{2}{25}$ | B1 | oe |
| 14(b) | $\frac{1}{64^{\frac{2}{3}}} \text { or }\left(4^{3}\right)^{-\frac{2}{3}} \text { or } \frac{1}{\left(4^{3}\right)^{\frac{2}{3}}}$ | M1 | $\begin{aligned} & 4^{-2} \text { or } \frac{1}{4^{2}} \\ & \text { or } \frac{1}{\left(64^{\frac{1}{3}}\right)^{2}} \text { or }\left(64^{\frac{1}{3}}\right)^{-2} \end{aligned}$ |
|  | $\frac{1}{16}$ | A1 |  |


| 15 | $100 n=21.6161 \ldots$ <br> $n=0.21616 \ldots$ | M1 | $1000 n=216.1616 \ldots$ <br> $10 n=2.1616 \ldots$ |
| :---: | :--- | :---: | :--- |
| and subtracts |  |  |  |$\quad$ A1 | $990 n=214$ |
| :--- |


| Alt 15 | $\begin{aligned} & 0.2+0.01616 \ldots \\ & 100 n=1.61616 \ldots \\ & \quad n=0.01616 \ldots \\ & \text { and subtracts } \\ & \\ & \text { (or uses } 1000 n \text { and } 10 n \text { and } \\ & \text { subtracts) } \\ & \hline \end{aligned}$ | M1 | $\begin{aligned} & 0.2+0.01616 \ldots \\ & 100 n=16.1616 \ldots \\ & \quad n=0.1616 \ldots \\ & \text { and subtracts } \\ & \\ & \text { (or uses } 1000 n \text { and } 10 n \text { and } \\ & \text { subtracts) } \end{aligned}$ |
| :---: | :---: | :---: | :---: |
|  | $99 n=1.6$ | A1 | $99 n=16$ and obtains $\frac{16}{990}$ |
|  | $\frac{2}{10}+\frac{1.6}{99}=\frac{198+16}{990}=\frac{214}{990}=\frac{107}{495}$ <br> Must see $\frac{214}{990}$ as well as $\frac{107}{495}$ | A1 | $\frac{2}{10}+\frac{16}{990}=\frac{198+16}{990}=\frac{214}{990}=\frac{107}{495}$ <br> Must see $\frac{214}{990}$ as well as $\frac{107}{495}$ |
|  |  |  | SC2 $0.2+\frac{16}{990}$ and fully correct subsequent working |


| 16 | $\begin{aligned} & x^{2}+x-7 \pm 3 x \pm 2 \text { or } \\ & 3 x-2 \pm x^{2} \pm x \pm 7 \end{aligned}$ | M1 | $x^{2}+x-7= \pm 3 x \pm 2$ or $3 x-2= \pm x^{2} \pm x \pm 7$ |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & x^{2}+4 x-9 \\ & -x^{2}+2 x+5 \end{aligned}$ <br> or | A1 |  |
|  | $\begin{aligned} & y=x^{2}+4 x-9 \\ & y=-x^{2}+2 x+5 \end{aligned}$ | A1 | SC 1 $\begin{array}{r} x^{2}-2 x-5 \\ x^{2}-2 x-9 \\ x^{2}+4 x-5 \\ x^{2}+4 x+5 \\ x^{2}+2 x+5 \\ x^{2}+2 x-9 \\ -x^{2}+4 x+5 \\ -x^{2}+4 x-9 \\ -x^{2}+2 x-9 \end{array}$ <br> SC2 $y=$ any of the above |

