

Surname						Other Names					
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General Certificate of Secondary Education
June 2006



MATHEMATICS (MODULAR) (SPECIFICATION B)
Module 5 Higher Tier
Paper 2 Calculator

33005/H2

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Monday 12 June 2006 9.00 am to 10.15 am

<p>For this paper you must have:</p> <ul style="list-style-type: none"> • a calculator • mathematical instruments 	
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For Examiner's Use	
Pages	Mark
3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16	
TOTAL	
Examiner's Initials	

Time allowed: 1 hour 15 minutes

Instructions

- Use blue or black ink or ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Answer the questions in the spaces provided.
- Use a calculator where appropriate.
- Do all rough work in this book.
- If your calculator does not have a π button, take the value of π to be 3.14 unless another value is given in the question.

Information

- The maximum mark for this paper is 70.
- The marks for questions are shown in brackets.
- You may ask for more answer paper, graph paper and tracing paper. This must be tagged securely to this answer book.

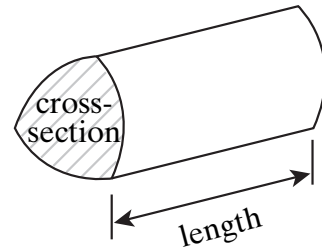
Advice

- In all calculations, show clearly how you work out your answer.

Formulae Sheet: Higher Tier

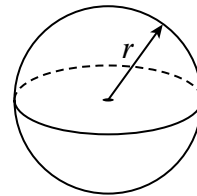
You may need to use the following formulae:

Volume of prism = area of cross-section \times length



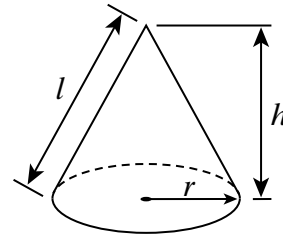
Volume of sphere = $\frac{4}{3} \pi r^3$

Surface area of sphere = $4 \pi r^2$



Volume of cone = $\frac{1}{3} \pi r^2 h$

Curved surface area of cone = $\pi r l$

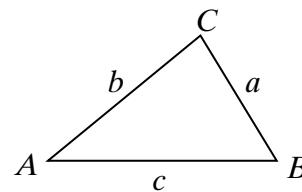


In any triangle ABC

Area of triangle = $\frac{1}{2} ab \sin C$

Sine rule $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$



The Quadratic Equation

The solutions of $ax^2 + bx + c = 0$, where $a \neq 0$, are given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Answer **all** questions in the spaces provided.

- 1 Liam is using trial and improvement to find a solution to the equation

$$x^3 + 4x = 72$$

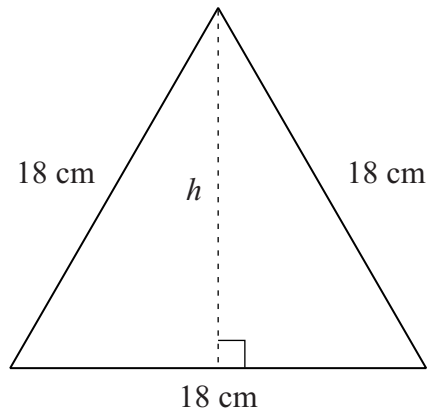
The table shows his first two trials.

x	$x^3 + 4x$	Comment
3	39	Too small
4	80	Too large

Continue the table to find a solution to the equation.
Give your answer to one decimal place.

Answer $x = \dots\dots\dots$ (3 marks)

- 2 The diagram shows an equilateral triangle of side 18 cm.



Not drawn accurately

Calculate the height of the triangle (marked h in the diagram).

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Answer cm (4 marks)

- 3 (a) Solve the inequality $5x + 3 < 18$

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Answer (2 marks)

- (b) y is an integer.

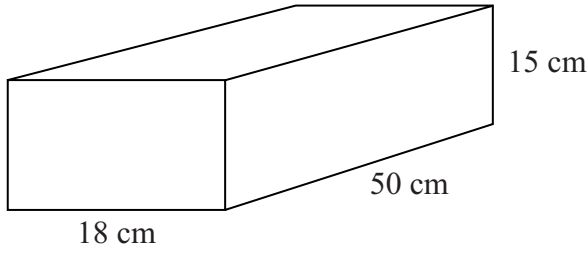
Write down all the solutions of the inequality $-6 \leq 2y < 0$

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Answer (3 marks)

- 4 A wooden cuboid is 18 cm wide, 15 cm high and 50 cm long.
It weighs 12 kg.



Not drawn accurately

Calculate the density of the wood.
Give your answer in g/cm^3 .

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Answer g/cm^3 (3 marks)

Turn over for the next question

5 (a) Multiply out $(2p^2q^3) \times (3p^5q)$

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Answer (2 marks)

(b) Expand and simplify $(p + 7)(p + 2)$

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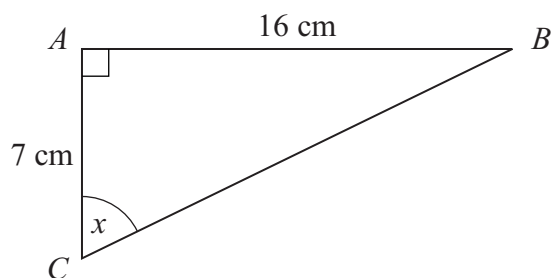
Answer (2 marks)

(c) Solve the equation $\frac{x + 1}{3} = 5 - 2x$

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Answer $x =$ (3 marks)

- 6 (a) In triangle ABC , angle $A = 90^\circ$, $AB = 16$ cm and $AC = 7$ cm



Not drawn accurately

Calculate the value of x .

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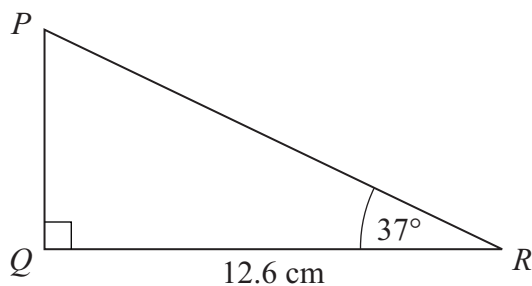
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Answer degrees (3 marks)

- (b) In triangle PQR , angle $Q = 90^\circ$, angle $R = 37^\circ$ and $QR = 12.6$ cm



Not drawn accurately

Calculate the length of PR .

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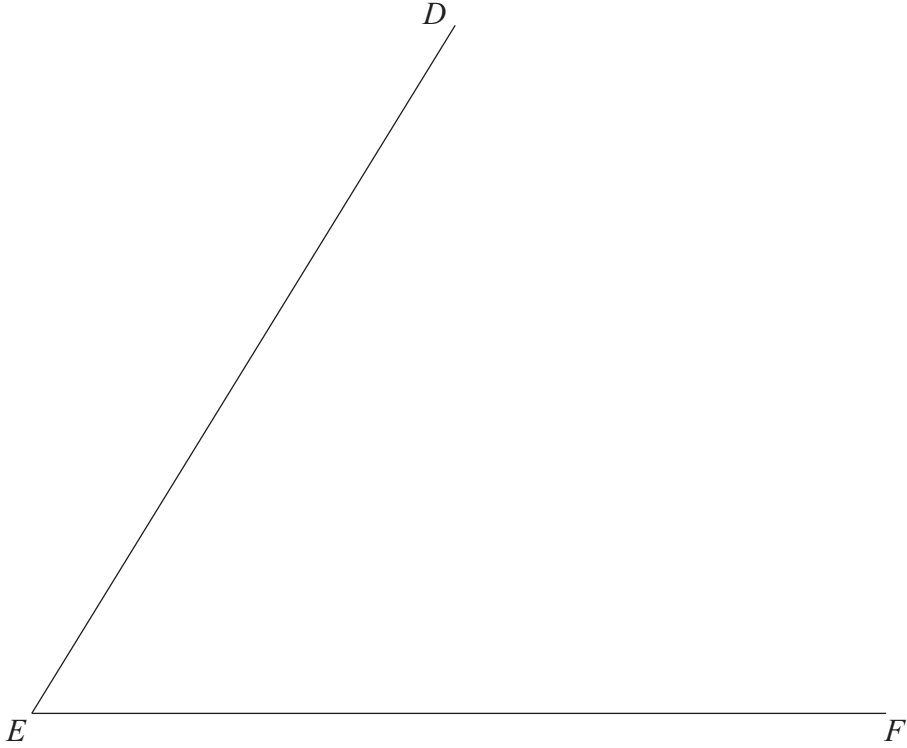
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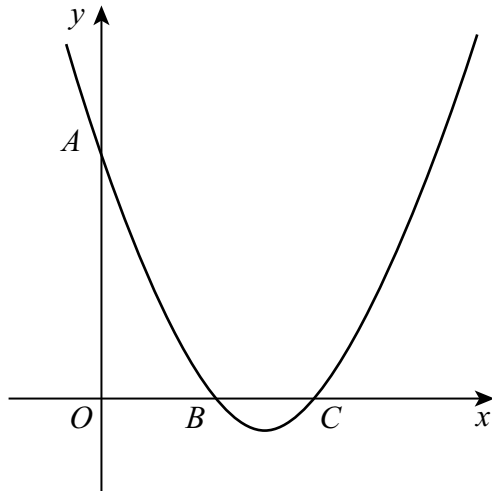
Answer cm (3 marks)

7 Using ruler and compasses only, construct the bisector of angle DEF .



(2 marks)

8 The sketch shows the graph of $y = (x - 2)(2x - 7)$



Not drawn accurately

(a) The graph crosses the y -axis at A .

Write down the coordinates of A .

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Answer A (..... ,) (1 mark)

(b) The graph crosses the x -axis at B and C .

Write down the coordinates of B and C .

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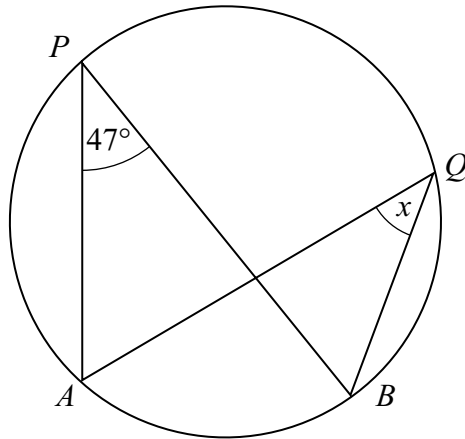
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Answer B (..... ,)

C (..... ,) (2 marks)

Turn over

- 9 In the diagram, A, P, Q and B are points on the circumference of the circle.
Angle $APB = 47^\circ$



Not drawn accurately

Find the value of x .
Give a reason for your answer.

Answer $x = \dots\dots\dots$ degrees

Reason $\dots\dots\dots$
 $\dots\dots\dots$
(2 marks)

- 10 Solve the equation $y^2 - 3y - 14 = 0$
Give your answers to two decimal places.
You **must** show your working.

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Answer $\dots\dots\dots$ (3 marks)

11 (a) The equations of four lines are given below.

Line *P* $y = 3x + 5$

Line *Q* $y = 4 - 3x$

Line *R* $y + 3x = 8$

Line *S* $y - 3x = 1$

(i) Name the lines that are parallel to the line $y = 3x$

Answer (1 mark)

(ii) Which line goes through the point (2, 7)?

Answer (1 mark)

(b) Write down the gradient of the line $y + 2x = 7$

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Answer (1 mark)

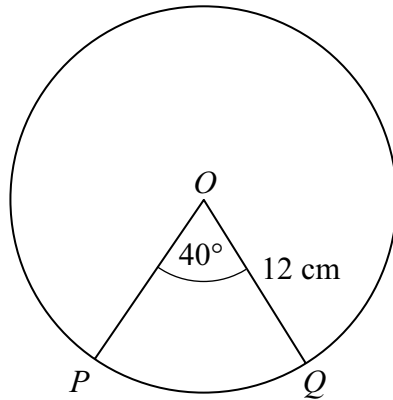
(c) Explain why the line $y = \frac{1}{2}x$ is perpendicular to the line $y + 2x = 7$

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(2 marks)

Turn over for the next question

- 12 PQ is an arc of a circle of radius 12 cm.
The centre of the circle is at O .
Angle $POQ = 40^\circ$



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Calculate the length of the minor arc PQ .

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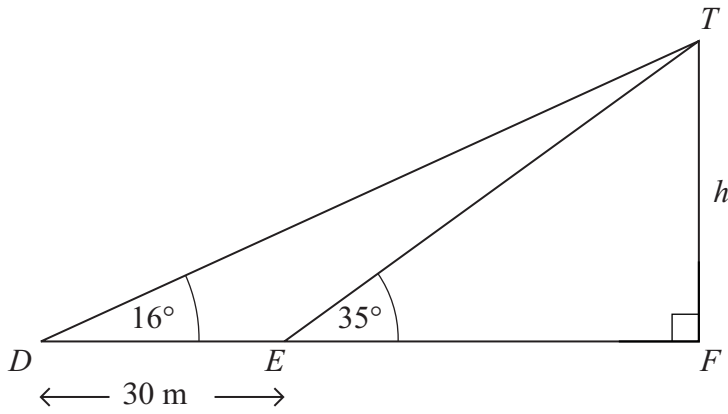
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Answer cm (3 marks)

- 13 D, E and F are three points on level ground.
 TF is the vertical side of a building.
 The angle of elevation of the top of the building from D is 16° .
 The angle of elevation of the top of the building from E is 35° .
 The distance $DE = 30$ m



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accurately

Calculate the height of the building, marked h on the diagram.

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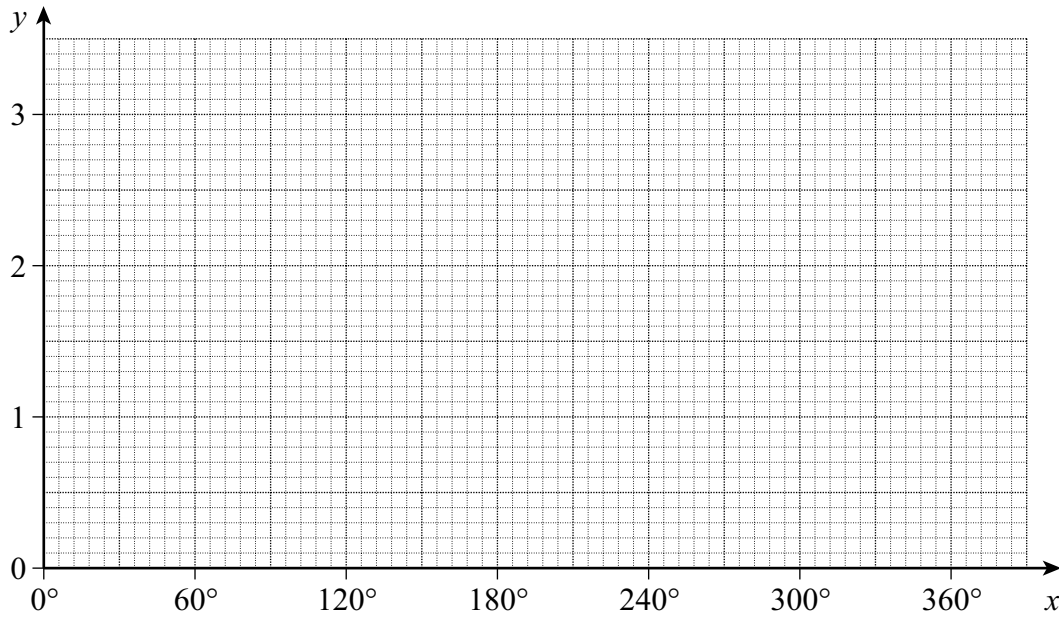
Answer m (5 marks)

- 14 (a) Complete the table of values for $y = 2 - \cos x$

x	0°	30°	60°	90°	120°	150°	180°
y	1	1.13	1.5	2	2.5		3

(1 mark)

- (b) On the grid, draw the graph of $y = 2 - \cos x$ for values of x from 0° to 180° .



(2 marks)

- (c) Describe how you could transform your graph from 0° to 180° to produce the graph from 180° to 360° .

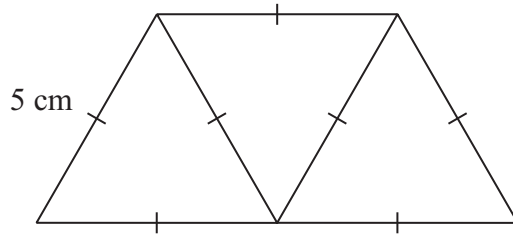
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(2 marks)

15 A trapezium is made from three equilateral triangles of side 5 cm.



Not drawn accurately

Calculate the area of the trapezium.

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Answer cm² (4 marks)

16 The surface area of a sphere is 1380 cm².

Calculate the volume of the sphere.
State the units of your answer.

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Answer (5 marks)

Turn over for the next question

Turn over ►

17 Solve the equation $\frac{3}{y+7} - \frac{1}{y+6} = \frac{1}{2}$

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Answer (5 marks)

END OF QUESTIONS