

General Certificate of Secondary Education

Mathematics 3302 Specification B

Module 3 Tier H 33003H

Mark Scheme

2005 examination - November series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

The following abbreviations are used on the mark scheme:

M Method marks awarded for a correct method.

A Accuracy marks awarded when following on from a correct method.

It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.

M dep A method mark which is dependent on a previous method mark being

awarded.

ft Follow through marks. Marks awarded for correct working following a

mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has

some mathematical worth.

oe Or equivalent.

eeoo Each error or omission.

MODULE 3 HIGHER TIER

33003H

1(a)	i) 1.7583799	B1	Accept 1.75838(0) and 1.75837
1(a)	ii) 1.76	B1 ft	1
1(b)	390 625	B1	Condone 390,625 and 390.625
	3.90625×10^5	B1 ft	ft at least 5 digits Accept 3.91×10^5 or 3.906×10^5 or 3.9×10^5 [or 3.90×10^5] or 3.9062×10^5 or 3.9063×10^5 (all for 2 marks)
2(a)	Increase is 7.2 kg	B1	M1 $\frac{10.9}{3.7}$ × 100 and subtract 100
	Percentage increase is $\frac{7.2}{3.7} \times 100$	M1	B1 = 295 [-100]
	= 195%	A1	Accept 194.6, 194.59 190 SC2 194 SC2 1.95 ⇒ B1
3	In 2001, number is 70 000 × 1.06 = 74 200		
	In 2002, number is 74 200 × 1.06 = 78 652	M1	
	In 2003, number is 78 652 × 1.06 = 83 371		
	In 2004, number is 83 371 × 1.06 = 88 373		
	In 2005, number is 88 373 × 1.06	M1	M2 for $70\ 000 \times 1.06^5$
	= 93 676	A1	Accept 93675 or 93675
	= 94 000	A1	Accept 93 700, 93 600 Accept 90 000 if 93676 or 93 700 seen Note: 91000 No marks
			T
4	3140 ≈ 0.8%	B1	or $3140 \approx 0.008$ Not for $3140 \approx 0.8$
	Area = $\frac{3140}{0.8} \times 100$	M1	Area = $\frac{3140}{0.008}$
	= 392 500	A1	= 392 500
			SC2 Misplaced point

5(a)	9	B1	
5(b)	Plot points	B1 ft	Tolerance $\pm \frac{1}{2}$ square
	Smooth curve	B1 ft	Tolerance $\pm \frac{1}{2}$ square Must not cross x axis
5(c)	$(3x^2-2x+1)-(3x^2-6x+2)$	M1	Accept $\pm 4x \pm 1$ for M1
	=4x-1		
	$\overline{\text{Draw } y = 4x - 1}$	B1 ft	
	x = 0.42, 1.58	A1	Accept 0.35 to 0.5, 1.5 to 1.65 [inclusive] Delete 1 mark for co-ordinates
6(a)	$A \propto d^2 \text{ or } A = kd^2$	M1	
0(a)		IVII	
	When $d = 200$, $A = 20000$ $20000 = k(200)^2$		
		N/1	
	$k = \frac{20000}{200^2}$	M1	
	$k = \frac{20000}{40000}$		or $k = 0.5$ or $\frac{1}{2}$
	$A = 0.5 d^2$	A1	May be seen in (b) or accept $A = kd^2$ and $k = \frac{1}{2}$ oe
6(b)	$A = 0.5 (1400)^2$	M1	
	= 980 000	A1	
7	x = 0.342		$x = 0.\dot{4}\dot{2}$
	100x = 34.242	M1	100x = 42.42
	99x = 33.9	A1	Needs subtraction also $99x = 42$
)), 33.)	711	
	$x = \frac{33.9}{99}$		$x = \frac{42}{99}$
	99		$0.3\dot{4}\dot{2} = \frac{3}{10} + \frac{42}{990} = \frac{297 + 42}{990}$
	$x = \frac{339}{990}$		$=\frac{339}{990}$
	$=\frac{113}{330}$	A1	$= \frac{113}{330}$ Needs a previous fraction correct

Price in March 2005 is $\frac{80}{100}$ of 2004 price Price in June 2005 is $\frac{80}{100} \times \frac{5}{6}$ of 2004 price = $\frac{2}{3}$ of 2004 price A1 Percentage discount is $\frac{1}{3} \times 100$ M1 = $33\frac{1}{3}$ A1 If final result 33.3 or 33.33 M2A2 or Assume price in 2004 was '£600' Price is now £480 $\times \frac{5}{6}$ M1 = £400 A1 Percentage discount is $\frac{200}{600} \times 100$ M1 = $33\frac{1}{3}$ A1 $66\frac{2}{3} \text{ SC2}$ $0r \frac{1}{6} \times \frac{80}{100}$ $13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ \therefore Discount is $20 + 13\frac{1}{3}$ M1 = $33\frac{1}{3}$ M1 = $33\frac{1}{3}$ M1 = $33\frac{1}{3}$ M1			I	
Price in June 2005 is $\frac{80}{100} \times \frac{5}{6}$ of 2004 price = $\frac{2}{3}$ of 2004 price A1 Percentage discount is $\frac{1}{3} \times 100$ M1 = $33\frac{1}{3}$ A1 If final result 33.3 or 33.33 M2A2 or Assume price in 2004 was '£600' Price is now £480 $\times \frac{5}{6}$ M1 = £400 A1 Percentage discount is $\frac{200}{600} \times 100$ M1 = $33\frac{1}{3}$ A1 $\frac{66\frac{2}{3} \text{ SC2}}{\text{or } \frac{1}{6} \times \frac{80}{100}}$ or $\frac{1}{3}\frac{1}{3}$ M1 = $13\frac{1}{3}$ % A1 [13.3 \Rightarrow M1 only] \therefore Discount is $\frac{20 \times 100}{100}$ M1	8	Price in March 2005 is $\frac{80}{100}$ of		
2004 price $= \frac{2}{3} \text{ of 2004 price}$ $= \frac{2}{3} \text{ of 2004 price}$ A1 Percentage discount is $\frac{1}{3} \times 100$ M1 $= 33\frac{1}{3}$ A1 If final result 33.3 or 33.33 M2A2 or Assume price in 2004 was '£600' Price is now £480 $\times \frac{5}{6}$ M1 $= £400$ A1 Percentage discount is $\frac{200}{600} \times 100$ M1 $= 33\frac{1}{3}$ A1 $\frac{66\frac{2}{3} \text{ SC2}}{\text{or } \frac{1}{6} \times \frac{80}{100}}$ M1 $= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is}$ $20 + 13\frac{1}{3}$ M1		2004 price		
			M1	
$= 33\frac{1}{3}$ A1 If final result 33.3 or 33.33 M2A2 or Assume price in 2004 was '£600' Price is now £480 × $\frac{5}{6}$ M1 $= £400$ A1 Percentage discount is $\frac{200}{600} \times 100$ M1 $= 33\frac{1}{3}$ A1 $\frac{66\frac{2}{3} \text{ SC2}}{\text{or } \frac{1}{6} \times \frac{80}{100}}$ M1 $= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is}$ $20 + 13\frac{1}{3}$ M1			A1	
or Assume price in 2004 was '£600' Price is now £480 $\times \frac{5}{6}$ M1 $= £400 \qquad A1$ Percentage discount is $\frac{200}{600} \times 100$ M1 $= 33\frac{1}{3} \qquad A1$ $\frac{66\frac{2}{3} \text{ SC2}}{\text{or } \frac{1}{6} \times \frac{80}{100} \qquad M1}$ $= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is }$ $20 + 13\frac{1}{3} \qquad M1$		Percentage discount is $\frac{1}{3} \times 100$	M1	
Assume price in 2004 was '£600' Price is now £480 × $\frac{5}{6}$ M1 = £400 A1 Percentage discount is $\frac{200}{600}$ × 100 M1 = $33\frac{1}{3}$ A1 $66\frac{2}{3}$ SC2 or $\frac{1}{6}$ × $\frac{80}{100}$ M1 = $13\frac{1}{3}$ % A1 [13.3 \Rightarrow M1 only] \therefore Discount is $20 + 13\frac{1}{3}$ M1		$=33\frac{1}{3}$	A1	If final result 33.3 or 33.33 M2A2
$= £400 \qquad \qquad A1$ Percentage discount is $\frac{200}{600} \times 100$ $= 33\frac{1}{3} \qquad \qquad A1$ $= 33\frac{1}{3} \qquad \qquad A1$ $\frac{66\frac{2}{3} \text{ SC2}}{\text{or } \frac{1}{6} \times \frac{80}{100}} \qquad \qquad M1$ $= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is}$ $20 + 13\frac{1}{3} \qquad \qquad M1$				1 ~ -
Percentage discount is $\frac{200}{600} \times 100$ M1 $= 33\frac{1}{3} \qquad \qquad A1$ $66\frac{2}{3} \text{ SC2}$ $\text{or } \frac{1}{6} \times \frac{80}{100} \qquad \qquad M1$ $= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is}$ $20 + 13\frac{1}{3} \qquad \qquad M1$				Price is now £480 $\times \frac{5}{6}$ M1
$= 33\frac{1}{3}$ $= 66\frac{2}{3} \text{ SC2}$ $\text{or } \frac{1}{6} \times \frac{80}{100}$ $= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is}$ $20 + 13\frac{1}{3}$ M1				= £400 A1
$= 33\frac{1}{3}$ $66\frac{2}{3} \text{ SC2}$ $\text{or } \frac{1}{6} \times \frac{80}{100}$ $= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is}$ $20 + 13\frac{1}{3}$ M1				Percentage discount is $\frac{200}{600} \times 100$
$66\frac{2}{3} \text{ SC2}$ $\text{or } \frac{1}{6} \times \frac{80}{100} \qquad \text{M1}$ $= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is}$ $20 + 13\frac{1}{3} \qquad \text{M1}$				M1
or $\frac{1}{6} \times \frac{80}{100}$ M1 $= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is}$ $20 + 13\frac{1}{3} \qquad \text{M1}$				$=33\frac{1}{3}$ A1
$= 13\frac{1}{3}\% \text{ A1 } [13.3 \Rightarrow \text{M1 only}]$ $\therefore \text{ Discount is}$ $20 + 13\frac{1}{3} \qquad \qquad \text{M1}$				$66\frac{2}{3}$ SC2
$\therefore \text{ Discount is} \\ 20 + 13\frac{1}{3} \qquad \qquad \text{M1}$				or $\frac{1}{6} \times \frac{80}{100}$ M1
$20 + 13\frac{1}{3}$ M1				$= 13\frac{1}{3}\%$ A1 [13.3 \Rightarrow M1 only]
				∴ Discount is
$= 33\frac{1}{3}\%$ A1				$20 + 13\frac{1}{3}$ M1
				$=33\frac{1}{3}\%$ A1
			T	

9(a)	2×30 or 3×20	M1	First prime factor correct		
	= 2 (x) 2 (x) 3 (x) 5	A1	Condone × 1		
	$=2^2\times3\times5$	A1			
9(b)	HCF is 8	B2	$32 = 2^5 120 = 2^3 \times 3 \times 5$		
			B1 for HCF = 4		

	10(a)	$\approx \frac{400 \times 3}{0.6}$	M1	
			A1	Needs $\frac{1200}{0.6}$ or equivalent [or $\frac{1170}{0.6}$]
10(c) $8 \times \frac{1}{9}$ B1 B1B1 for 8; B1 for $\frac{1}{9}$; × not required $= \frac{8}{9}$ B111Sum is three times the middle numberB2or use of $x-1$, x , $x+1$ B1 $= 3x$ oeB1SC1 for two correct examples12(a) 11.5×10^{12} B1or correct answer, not in correct standard form, could be normal numbers $= 1.15 \times 10^{13}$ B112(b) 0.46×10^{-2} B1B1 for digits 46 4.6×10^{-3} B113Minimum length left is minimum started minus maximum used Minimum started is 99.5 m Maximum used per house isM1			A1	[or 1950] [Check not from $\frac{400 \times 5}{1}$]
11Sum is three times the middle numberB2or use of $x-1$, x , $x+1$ B1 $=3x$ oeB1 $=3x$ oeB1 $=5x$ or correct examples $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct standard form, could be normal numbers $=5x$ or correct answer, not in correct answer, no	10(b)	2.4×10^{-6}	B1	
Sum is three times the middle B2 or use of $x - 1$, x , $x + 1$ B1 $= 3x$ oe B1 SC1 for two correct examples	10(c)	$8 \times \frac{1}{9}$	B1 B1	B1 for 8; B1 for $\frac{1}{9}$; × not required
number B2 Or use of $x - 1$, x , $x + 1$ B1 = $3x$ oe B1 SC1 for two correct examples 12(a) 11.5×10^{12} B1 or correct answer, not in correct standard form, could be normal numbers = 1.15×10^{13} B1 12(b) 0.46×10^{-2} B1 B1 for digits 46 4.6 \times 10 ⁻³ B1 Minimum length left is minimum started minus maximum used M1 Minimum started is 99.5 m B1 Maximum used per house is B1		$=\frac{8}{9}$	B1	
number B2 Or use of $x - 1$, x , $x + 1$ B1 = $3x$ oe B1 SC1 for two correct examples 12(a) 11.5×10^{12} B1 or correct answer, not in correct standard form, could be normal numbers = 1.15×10^{13} B1 12(b) 0.46×10^{-2} B1 B1 for digits 46 4.6 \times 10 ⁻³ B1 Minimum length left is minimum started minus maximum used M1 Minimum started is 99.5 m B1 Maximum used per house is B1				,
SC1 for two correct examples 12(a) 11.5×10^{12} B1 or correct answer, not in correct standard form, could be normal numbers = 1.15×10^{13} B1 12(b) 0.46×10^{-2} B1 B1 for digits 46 4.6 $\times 10^{-3}$ B1 Minimum length left is minimum started minus maximum used M1 Minimum started is 99.5 m B1 Maximum used per house is B1	11		B2	or use of $x - 1$, x , $x + 1$ B1
12(a) 11.5×10^{12} B1or correct answer, not in correct standard form, could be normal numbers $= 1.15 \times 10^{13}$ B112(b) 0.46×10^{-2} B1B1 for digits 46 4.6×10^{-3} B1 Minimum length left is minimum started minus maximum used Minimum started is 99.5 m Maximum used per house is				=3x oe B1
12(a) 11.5×10^{12} B1standard form, could be normal numbers $= 1.15 \times 10^{13}$ B112(b) 0.46×10^{-2} B1B1 for digits 46 4.6×10^{-3} B1 13Minimum length left is minimum started minus maximum used Minimum started is 99.5 mM1Maximum used per house isB1				SC1 for two correct examples
12(a) 11.5×10^{12} B1standard form, could be normal numbers $= 1.15 \times 10^{13}$ B112(b) 0.46×10^{-2} B1B1 for digits 46 4.6×10^{-3} B1 13Minimum length left is minimum started minus maximum used Minimum started is 99.5 mM1Maximum used per house isB1				
12(b) 0.46×10^{-2} B1 B1 for digits 46 4.6×10^{-3} B1 13 Minimum length left is minimum started minus maximum used M1 Minimum started is 99.5 m B1 Maximum used per house is B1	12(a)	11.5×10^{12}	B1	standard form, could be normal
4.6 × 10 ⁻³ B1 Minimum length left is minimum started minus maximum used Minimum started is 99.5 m Maximum used per house is		$=1.15\times10^{13}$	B1	
13 Minimum length left is minimum started minus maximum used Minimum started is 99.5 m Maximum used per house is	12(b)	0.46×10^{-2}	B1	B1 for digits 46
Started minus maximum used Minimum started is 99.5 m Maximum used per house is		4.6×10^{-3}	B1	
started minus maximum used Minimum started is 99.5 m Maximum used per house is		,		
Maximum used per house is D1	13	Minimum length left is minimum started minus maximum used	M1	
Maximum used per house is P1		Minimum started is 99.5 m	B1	
10.25 m		Maximum used per house is 10.25 m	B1	
Maximum used for nine houses is 92.25 m M1 ft $9 \times \text{max}$ [max must be between 10 and 10.5 not inclusive]			M1 ft	[max must be between 10 and 10.5,
Minimum left is 7.25 m A1		Minimum left is 7.25 m	A1	

14(a)	5	B1	
14(b)	$162 = 2 \times 3^b$		
	$81 = 3^b$	M1	
	b = 4 Hence $162 = 2 \times 3^4$	A1	
14(c)	$\frac{1}{32^{\frac{3}{5}}}$	B1	or B1 for $32^{\frac{3}{5}} = 8$ or 2^3
	$=\frac{1}{8}$	B1	

		l		
15	$\sqrt{150} = 5\sqrt{6}$	B1		
	$\sqrt{150} - \sqrt{6} = 4\sqrt{6}$	B1		
	$\frac{\sqrt{150} - \sqrt{6}}{\sqrt{12}} = \frac{4\sqrt{6}}{2\sqrt{3}} \text{ or } \frac{4\sqrt{6}}{\sqrt{2}\sqrt{6}}$	M1	M1 for $\sqrt{12} = 2\sqrt{3}$	
	$=2\sqrt{2}$	A1	SC3 $\frac{4}{\sqrt{2}}$	
			OR $\frac{\sqrt{1800} - \sqrt{72}}{12}$	M1
			$=\frac{30\sqrt{2}-6\sqrt{2}}{12}$	B1
			$=\frac{24\sqrt{2}}{12}$	B1
			$=2\sqrt{2}$	A1
			or $\frac{5\sqrt{6} - \sqrt{6}}{\sqrt{2}\sqrt{6}}$ $= \frac{4}{\sqrt{2}}$	M1M1
			$=\frac{4}{\sqrt{2}}$	A1
			$=2\sqrt{2}$	A1