ASSESSMENT and
OUALIFICATIONS

# General Certificate of Secondary Education 

## Mathematics 3302 Specification B

Module 5 Paper 1 Tier H 33005H1

## Mark Scheme

## 2005 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

M Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
oe Or equivalent.
eeoo Each error or omission.

MODULE 5 Paper 1 HIGHER TIER

| 1(a) | $-12-4-3$ | B2 | -1 eeoo |
| :---: | :--- | :---: | :--- |
| (b) | Five points plotted | B1 ft | $\pm \frac{1}{2}$ square |
|  | Smooth curve | B1 ft | Through all five points $\pm \frac{1}{2}$ square |


| 2(a) | $3 x \leq 11$ | M1 | $(x=) \frac{11}{3}$ <br> $11 \div 3$ <br> $x \leq \frac{16-5}{3}$ <br> $x<\frac{16-5}{3}$ |
| :--- | :--- | :--- | :--- |
|  | $x \leq \frac{11}{3}$ or $3.66 \ldots$ or 3.67 | A1 | oe |
|  | $\frac{5}{2}<x<\frac{7}{2}$ <br> or $2 x=6$ | M1 | oe |
| 3 | A1 | $5<2 \times 3<7$ |  |


| 3(a) | $r^{4}\left(r^{2}-3\right)$ | B1 |  |
| :---: | :--- | :---: | :--- |
| (b) | i) $(x+a)(x+b)$ | M1 | $a b= \pm 14$ |
|  | $(x+7)(x-2)$ | A1 |  |
|  | ii) $-7,2$ | B1 ft | ft from two linear brackets |


| 4 (a) | 9.4 cm | B1 |  |
| :--- | :--- | :---: | :--- |
| (b) | Valid reason | B1 | Accept: <br> Angles opposite to side 5.6 cm <br> In the same position <br> Smallest angles (in the triangle) <br> Angles between 9.4 and 10.3 <br> Corresponding (angles) |
| Not accept: <br> Rotation <br> Reflection (unless clarified) |  |  |  |


| 5(a) | $y=5 x+c$ <br> $c \neq 0$ | B1 | oe |
| :---: | :--- | :---: | :--- |
| (b) | $y=-2 x+6$ | M1 | $-2 x$ scores M1A0 <br> $m=-2$ and $c=6$ scores M1A0 |
|  | $(m=)-2$ | A1 |  |


| 6(a) | $\pi(\times) 5^{2}$ | M1 | Condone $3.1 \ldots \times 5^{2}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \pi(\times) 5^{2} \times 10 \\ & \text { or their area } \times 10 \end{aligned}$ | M1 | Condone $3.1 \ldots \times 5^{2} \times 10$ <br> Their area must contain $\pi$ (or 3.1...) |  |
|  | $250 \pi$ or $250 \times \pi$ or $\pi \times 250$ | A1 | 775 to 790 implies M2A0 <br> Do not accept $\pi 250$ <br> Ignore fw <br> $250 \pi$ can be recovered in (b) |  |
| (b) | $40 \times 50$ | M1 | $10 \times 10 \times 10$ | $40 \times 50$ |
|  | their $2000 \times 10$ | M1 | $\begin{aligned} & \text { their } 1000 \text { - their } \\ & 250 \pi \end{aligned}$ | $\begin{aligned} & 20 \times \text { their } \\ & \pi(\times) 5^{2} \end{aligned}$ |
|  | $20 \times$ their $250 \pi$ | M1 | $\begin{aligned} & 20 \times \text { their } \\ & (1000-250 \pi) \end{aligned}$ | $\begin{aligned} & \text { their } 2000 \text { - their } \\ & 500 \pi \end{aligned}$ |
|  | $20000-5000 \pi$ | A1 | oe <br> 4290 - 4500 implies M3A0 Ignore fw except $15000 \pi$ |  |


| 7 (a) | 45 | B1 |  |
| :---: | :--- | :--- | :--- |
| (b) | 53 | B1 |  |
| (c) | 90 | B1 |  |
| (d) | 80 | B1 |  |


| 8(a) | $\begin{aligned} & \frac{1}{2} \times 4 \times 4 \\ & \text { or } \frac{1}{2} \times 8 \times 4 \\ & \text { or } 4 \times 4 \end{aligned}$ <br> or $x^{2}+x^{2}=64$ <br> or $4^{2}+4^{2}=y^{2}$ | M1 | Correct attempt at one area |
| :---: | :---: | :---: | :---: |
|  | $\frac{1}{2} \times 4 \times 4 \times 4$ <br> or $\frac{1}{2} \times 8 \times 4 \times 2$ <br> or $4 \times 4 \times 2$ <br> or $8 \times 4$ <br> or $8 \times 8=64$ and $64 \div 2$ <br> or $2 x^{2}=64$ or $x=\sqrt{32}$ <br> or $\sqrt{\text { their } y^{2}}$ | M1 dep | Correct attempt at total area |
|  | 32 | A1 | Notes: <br> Penalise if clearly using perimeter $8 \times 8=64$ and $64 \div 4=16$ <br> scores M0 |
| (b) | $\begin{aligned} & \text { i) } 2 \times 25 \\ & \text { or } 100-50 \\ & \hline \end{aligned}$ | M1 | oe |
|  | 50 | A1 |  |
|  | ii) Attempt to use patterns of areas or lengths <br> or stating or implying that 29.7 cm is redundant data | M1 | Area 50, 100, 200, 400, (800) <br> Pattern 1 ( 5 cm ) <br> Pattern 3 ( 10 cm ) <br> Pattern $5(20 \mathrm{~cm})$ |
|  | Pattern 5 | A1 |  |


| 9 | $(x-2) y=m+x$ | M1 | Condone missing brackets for this <br> mark only unless recovered |
| :---: | :--- | :---: | :--- |
| $x y-2 y=m+x$ A1 | oe |  |  |
| $x y-x=m+2 y$ <br> or $x(y-1)=m+2 y$ <br> $x=\frac{m+2 y}{y-1}$ | M1 dep | Allow one sign error |  |


| 10(a) | $(-1,0)$ | B1 | Condone missing brackets |
| :---: | :--- | :--- | :--- |
| (b) | $-\frac{1}{2}$ | B1 |  |


| 11 | $\frac{1}{2} \times 8 \times 3 \times \sin 30$ | M1 | oe |
| :---: | :--- | :---: | :--- |
|  | $\frac{1}{2} \times 8 \times 3 \times 6 \times \sin 30$ | M1 dep | oe |
| 36 | A1 |  |  |
| $\mathrm{cm}^{2}$ | B1 | Units mark |  |


| 12(a) | $C B=-\mathbf{t}+\mathbf{s}$ <br> or $B C=-\mathbf{s}+\mathbf{t}$ <br> or states route $A M=A C+C M$ <br> or states route $A M=A B+B M$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $C M=\frac{1}{2}(-\mathbf{t}+\mathbf{s})$ <br> or $B M=\frac{1}{2}(-\mathbf{s}+\mathbf{t})$ | M1 dep |  |
|  | $A M=\frac{1}{2} \mathbf{s}+\frac{1}{2} \mathbf{t}$ | A1 | oe <br> Must be simplified |
| (b) | i) Parallelogram | B1 | Accept quadrilateral |
| ii) Correct fact | B1 | Accept: In a straight line <br> $M$ is midpoint of $A D$ |  |
|  | B1 | Accept: <br> Properties of diagonal of a <br> parallelogram <br> Use of vectors |  |
| eg $\overrightarrow{A M}=\frac{1}{2} \overrightarrow{A D}$ |  |  |  |$|$| Valid explanation |
| :--- |


| 13 | Attempt to draw 1 line with either <br> correct gradient or correct <br> $y$-intercept | M1 | Attempt to add (or subtract) <br> simultaneous equations |
| :---: | :---: | :---: | :--- |
|  | Both lines correctly drawn | A 1 | $2 y=2$ or $0=4 x+4$ |
| Both lines of symmetry drawn <br> (for their lines) | A 1 ft | $y=1$ or $x=-1$ |  |
| $x=-1$ and $y=1$ | A 1 | $x=-1$ and $y=1$ on answer line or <br> explicitly given as lines of symmetry |  |


| 14(a) | $(a=) 5$ | B1 |  |
| :---: | :--- | :---: | :--- |
|  | $(b=) 15$ | B1 |  |
| (b) | 15 | B1 ft | their $b$ |


| $15($ a) | 2 | B1 | Answers from quadrants 2 \& 3 <br> eg 120 and 240 |
| :---: | :--- | :---: | :--- |
| (b) | 2 | B1 | Answers from quadrants 2 \& 3 <br> eg 104 and 256 |
| (c) | 1 | B1 | $180^{\circ}$ |
| (d) | 4 | B1 | One answer from each quadrant <br> eg 60, 120, 240, 300 |


| 16 | $\frac{(x+2)(x+1)}{x(x+1)}$ or $\frac{x(x-1)}{x(x+1)}$ | M1 | $(x+2)(x+1)-x(x-1)$ |
| :---: | :--- | :---: | :--- |
|  | $\frac{(x+2)(x+1)-x(x-1)}{x(x+1)}$ | M1 dep | $(x+2)(x+1)-x(x-1)=2(2 x+1)$ |
|  | M1 | $x^{2}+2 x+x+2-x^{2}+x$ <br> Allow one error |  |
| $x^{2}+2 x+x+2-x^{2}+x$ <br> Allow one error | A1 | $4 x+2=4 x+2$ <br> or $2(2 x+1)=2(2 x+1)$ |  |
| $\frac{4 x+2}{x(x+1)}=\frac{2(2 x+1)}{x(x+1)}$ |  |  |  |


| $17(\mathrm{a})$ | $A$ | B1 |  |
| :---: | :--- | :---: | :--- |
| (b) | $D$ | B1 |  |
| (c) | $C$ | B1 | Note: $C$ and $D$ reversed scores B0B1 |
| (d) | $B$ | B1 | Note: $A$ and $B$ reversed scores B0B1 |

