ASSESSMENT and
OUALIFICATIONS

# General Certificate of Secondary Education 

## Mathematics 3302 Specification B

Module 3 Tier H 33003H

## Mark Scheme

## 2005 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

M Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
oe Or equivalent.
eeoo Each error or omission.

MODULE 3 HIGHER TIER

| 1 | $\frac{15}{100} \times 60(=9)$ <br> or $100-15(=85)$ | M1 | $60-53(=7)$ or $\frac{53}{60} \times 100(=88)$. |
| :---: | :--- | :---: | :--- |
| $60-$ their $9(=51)$ <br> or $\frac{85}{100} \times 60(=51)$ | M1 dep | $\frac{\text { their } 7}{60} \times 100(=11.6 \ldots)$ <br> or $100-$ their $88.3 \ldots(=11.6 \ldots)$ |  |
| Yes and explanation <br> eg 2 pounds more or sight of 51 <br> No ft on explanations | A1 | Yes and explanation <br> eg About 3\% more or sight <br> of 11.6... <br> No ft on explanations <br> SC2 9 and Yes |  |


| 2 | $\frac{7}{9} \times 279000$ | M1 | For the 9 allow their sum of 2 and 7 |
| :---: | :--- | :---: | :--- |
|  | 217000 | A1 | SC1 Answers of 62000 <br> or both of 62000 and 217000 |


| 3 (a) | $2500 \times 1.02(=2550)$ | M1 | $2 \%$ of $2500+2500$ |
| :---: | :--- | :---: | :--- |
|  | their $2550 \times 1.02^{2}$ <br> Note: $2500 \times 1.02^{3}$ scores M1M1 | M1 dep | $2 \%$ of their $2550+$ their 2550 <br> $(=2601)$ <br> $2 \%$ of their 2601 + their 2601 |
|  | 2653.02 | A1 | Do not accept 2653 unless full value <br> seen earlier (however answer of <br> 2653 implies M2) <br> SC1 Answer of 4320 or 2650 |
| (b) | $221.45=103 \%$ | M1 | 1.03 seen |$|$| M1 dep |
| :--- |
| oe |


| 4(a) | J(upiter) | B1 | Accept $1.9 \times 10^{27}$ |
| :---: | :---: | :---: | :---: |
| (b) | $\frac{6.0 \times 10^{24}}{3.3 \times 10^{23}} \quad\{=18 .(\ldots)\} \quad$ or $1.8 \times 3.3 \times 10^{23}\left(=5.94 \times 10^{23}\right.$ <br> or $5.9 \times 10^{23}$ or $\left.6 \times 10^{23}\right)$ <br> or $\frac{6.0 \times 10^{24}}{1.8}\left(=3.3 \ldots \times 10^{24}\right)$ | M1 | Allow 3 to be used for 3.3 (giving 20) <br> Allow 2 to be used for 1.8 (giving $6.6 \times 10^{23}$ ) <br> Allow 3 to be used for 3.3 (giving $5.4 \times 10^{23}$ ) <br> Allow 2 to be used for 1.8 (giving $3 \times 10^{24}$ ) |
|  | No and valid explanation (No may be implied by explanation) | A1 | eg For explanation - obtains the answers given in M1 or refers to powers of 10 being different <br> SC2 No calculations seen but totally convincing answer in words eg States that it is about 18 times as heavy |
| (c) | $6.53(0) \times 10^{9}$ | B1 | Allow any number of zeros after the 3 |
| (d) | $4.86 \times 10^{4} \div 2.27 \times 10^{3}$ | M1 | Allow approximations of these numbers to 1 or 2 sf |
|  | 21.4(0969163...) | A1 | Allow rounding or truncating to 1 dp or better |
|  | 21 or 21.4(:1) | B1 ft | ft from value or calculation seen to 1,2 or 3 sf <br> SC1 0.05 or 0.047 or 0.0467 |


| $5($ a) | $8.5 \times 10$ | M1 | $90-0.5 \times 10$ |
| :---: | :--- | :---: | :--- |
|  | 85 | A1 |  |
| (b) | 75 | B1 |  |
|  | No and complete explanation <br> eg $(85+75=) 160$ | B1 ft | ft for explanation <br> their minimum nuts $(84.5$ to 85 <br> inclusive) + their minimum treacle <br> $(74.5$ to 75 inclusive $)$ |


| 6(a) | $d=k t^{2}$ | M1 | Allow $d \propto t^{2}$ |
| :---: | :--- | :---: | :--- |
|  | $490=k \times 100$ | M1 dep |  |
|  | $k=4.9$ | A 1 | $d=4.9 t^{2}$ only needed if equation not <br> seen for first M1 |
| (b) | 30.625 | B 1 ft | ft only from $d=k t^{2}$ with incorrect $k$ <br> Condone 30.6 and 30.63 |
| (c) | Correct sketch of parabola <br> starting from origin | B 1 |  |


| 7 (a) | 19683 | B1 |  |
| :---: | :--- | :---: | :--- |
| (b) | 0.03125 or $\frac{1}{32}$ | B1 |  |


| 8 | $0.5 \times 0.6 \times \frac{x}{(100)}=0.255$ | M1 | oe $50 \times 60 \times x=25.5$ is M0 |
| :---: | :--- | :---: | :--- |
|  | $x=\frac{0.255(\times 100)}{0.5 \times 0.6}$ | M1 dep |  |
|  | 85 | A1 | Correct answer scores 3 marks <br> unless clearly from an incorrect <br> method |


| Alt 8 | Starts with a number of applicants <br> eg 100 and calculates (50 and) 30 | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $x=\frac{25.5(\times 100)}{30}$ | M1 dep | oe |
|  | 85 | A1 |  |


| 9(a) | $\frac{1}{0.2}$ or $1 \div 0.2$ | M1 | $\frac{10}{2}$ oe fraction |
| :--- | :--- | :--- | :--- |
|  | $5(.0)$ | A1 | Do not allow equivalents |
| (b) | i) 5 | B1 | oe |
|  | ii) $\frac{4}{3}$ | B1 | oe |


| 10 | $\frac{500(x) 2}{40(+) 60}$ or $\frac{505(x) 2}{40(+) 60}$ or $\frac{510(\times) 2}{40(+) 60}$ | M1 | Two out of four correct |
| :---: | :--- | :--- | :--- |
|  | A1 | Condone for 2 marks <br> $\frac{500 \times 1.9}{100}=9.5$ and $\frac{505 \times 2}{101}=10$ <br> and $\frac{505 \times 1.9}{101}=9.5$ |  |


| 11(a) | $2(x) 18 \text { or } 3(x) 12 \text { or } 2^{2}(x) 9$ or $4(x) 3^{2}$ or $2(x) 3(x) 6$ | M1 | For correct use of prime and other factor(s) <br> May be seen on 'exploding tree' or 'division' list <br> List of factors is M0 unless paired and includes 2,18 or 3,12 |
| :---: | :---: | :---: | :---: |
|  | $2 \times 2 \times 3 \times 3$ or 2.2.3.3 | A1 | $2^{2} \times 3^{2} \quad$ " $1 \times$ " included is A0 |
| (b) | $45=3(\times) 3(\times) 5$ | M1 | $36,72,108,144,180, \ldots$ $\text { and } 45,90,135,180, \ldots$ |
|  | 180 | A1 | Accept $2^{2} \times 3^{2} \times 5$ SC1 Answer of any other common multiple eg 360, 540, 720 etc |


| 12(a) | i) -2 and 3 | B1 | If non-graphical method used B0 |
| :---: | :---: | :---: | :---: |
|  | ii) $-1.6 \leq x \leq-1.5$ | B1 |  |
|  | $2.5 \leq x \leq 2.6$ | B1 |  |
| (b) | $x^{2}-x-6=x+3(=y)$ <br> or attempt to subtract the given equations | M1 | oe |
|  | $x^{2}-2 x-9=0$ | A1 |  |
| (c) | $x^{2}-x-6-x+2(=0)$ <br> or attempt to subtract the equations $(y=) x^{2}-x-6$ and $(0=) x^{2}-2 x-4$ | M1 | $x^{2}-2 x-4+x-2$ |
|  | $y=x-2$ | A1 | Must have $y=$ (may be seen on the graph) <br> SC1 $y=x+2$ or $y=-x-2$ or $y=2-x$ |


| 13(a) | $\frac{18}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}=\left(\frac{18 \sqrt{3}}{3}\right)$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $6 \sqrt{3}$ | A1 | Allow $\frac{6 \sqrt{3}}{1}$ |
| (b) | $3^{4}=81$ or $4^{4}=256$ | M1 | $100^{\frac{1}{4}}=10^{\frac{1}{2}}=\sqrt{10}$ |
|  | $3^{4}=81$ and $4^{4}=256$ | A1 | $3^{2}$ is 9 (or less than 10 ) and $4^{2}$ is 16 (or greater than 10 ) <br> or $\sqrt{9}=3$ and $\sqrt{16}=4$ <br> Accept $\sqrt{10}$ is 3.(...) |


| 14(a) | $\frac{1}{6}$ and $\frac{2}{3}$ | B1 B1 | One or two correct and one incorrect <br> answer given will be B1B0 <br> One or two correct and both <br> incorrect answers given B0B0 |
| :---: | :--- | :---: | :--- |
| (b) | $0 . \dot{2}$ | B1 | Accept $0.2^{\mathrm{r}}$ or 0.2... |
| (c) | $1000 x=154 . \dot{5} \dot{4}$ <br> $10 x=1.5 \dot{4}$ and subtracts | M1 | $100 x=15.4 \dot{5} \dot{4}$ and subtracts $\boldsymbol{x}$ |$|$| $990 x=153$ | A1 | $99 x=15.3$ |
| :--- | :--- | :--- |
| $\frac{153}{990}$ (oe fraction) $=\frac{17}{110}$ | A1 | Must see an equivalent fraction as $\frac{17}{110}$ <br> as well |


| Alt <br> $14(\mathrm{c})$ | $0.1+0.054$ <br> $1000 n=54.54$ <br> $10 n=0.54$ and subtracts | M1 | $100 n=5.45$ and subtracts $n$ |
| :---: | :--- | :---: | :--- |
|  | $990 n=54$ | A1 | $99 n=5.4$ |
|  | $\frac{153}{990}$ (oe fraction) $=\frac{17}{110}$ | A1 | Must see an equivalent fraction <br> as well as $\frac{17}{110}$ |


| $15(\mathrm{a})$ | $\sqrt{ } 20=2 \sqrt{ } 5$ | B1 |  |
| :---: | :--- | :---: | :--- |
|  | $3 \sqrt{5}$ | B1 |  |
| (b) | $3 \sqrt{ } 5-2 \sqrt{ } 5$ | M1 | $\frac{\sqrt{5}(1+\sqrt{ } 4)}{\sqrt{5}(\sqrt{9}-\sqrt{ } 4)}$ |
|  | $\frac{\text { their } p \sqrt{ } 5}{\sqrt{5}}$ | A1 ft |  |
|  | 3 | A1 |  |

