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For Examiner's Use

General Certificate of Secondary Education November 2008

MATHEMATICS (MODULAR) (SPECIFICATION B) Module 5 Higher Tier Paper 2 Calculator





Wednesday 12 November 2008 9.00 am to 10.15 am

For this paper you must have:

- · a calculator
- mathematical instruments.



Time allowed: 1 hour 15 minutes

Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Answers written in margins or on blank pages will not be marked.
- Use a calculator where appropriate.
- Do all rough work in this book.
- If your calculator does not have a π button, take the value of π to be 3.14 unless another value is given in the question.

Information

- The maximum mark for this paper is 70.
- The marks for questions are shown in brackets.
- You may ask for more answer paper, graph paper and tracing paper. This must be tagged securely to this answer book.

Advice

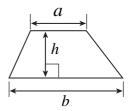
• In all calculations, show clearly how you work out your answer.

For Examiner's Use				
Pages	Mark			
3				
4–5				
6–7				
8–9				
10-11				
12–13				
14-15				
TOTAL				
Examiner's Initials				

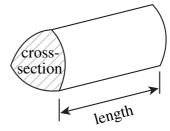


Formulae Sheet: Higher Tier

Area of trapezium = $\frac{1}{2}(a+b)h$

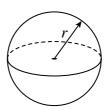


Volume of prism = area of cross-section \times length



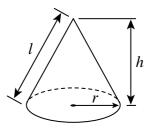
Volume of sphere =
$$\frac{4}{3}\pi r^3$$

Surface area of sphere = $4\pi r^2$



Volume of cone =
$$\frac{1}{3}\pi r^2 h$$

Curved surface area of cone = πrl

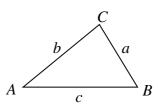


In any triangle ABC

Area of triangle = $\frac{1}{2}ab \sin C$

Sine rule
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$



The Quadratic Equation

The solutions of $ax^2 + bx + c = 0$, where $a \ne 0$, are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

Answer all questions in the spaces provided.

1 A wheel of a bicycle is shown.



1	(a)	The circumference is 70 cm.
		Calculate the diameter.
		Answer cm (2 marks)
1	(b)	The bicycle travels 50 metres.
		How many complete revolutions does the wheel make?
		Answer

5

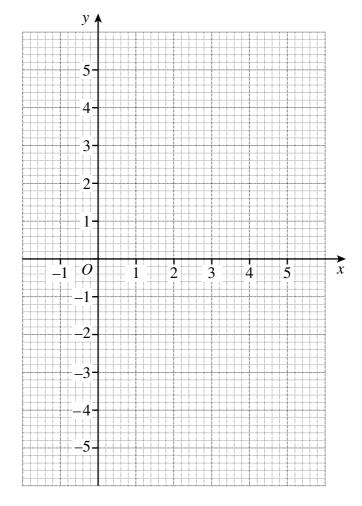


2 (a) Complete the table of values for $y = x^2 - 4x$

x	-1	0	1	2	3	4	5
у		0	-3	-4		0	5

(2 marks)

2 (b) On the grid, draw the graph of $y = x^2 - 4x$ for values x from -1 to 5.



(2 marks)

2 (c) Use your graph to find the solutions of the equation $x^2 - 4x = 2$

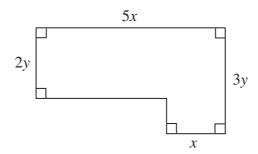
Answer and (2 marks)

2 (d) Explain why you cannot find solutions of the equation $x^2 - 4x = -5$

.....

(1 mark)

3 In this diagram, all lengths are in centimetres.



Not drawn accurately

3 (a) Tian says the perimeter of this shape is 6x + 5y.

Explain why Tian is wrong.

.....(1 mark)

3 (b) Work out the correct expression for the perimeter.

Give your answer in its simplest form.

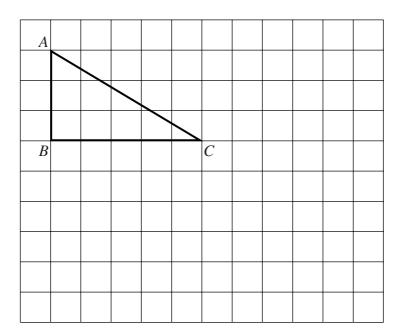
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(2 marks)

10

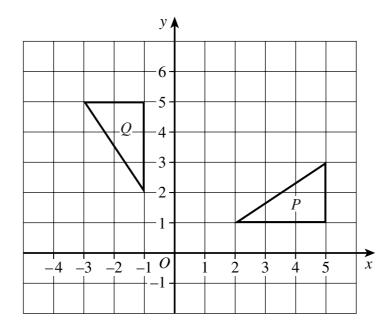


4 (a) Enlarge triangle ABC by scale factor 2, using A as the centre of enlargement.



(2 marks)

4 (b) Triangle P has been transformed to triangle Q.



Describe fully the **single** transformation which takes triangle P to triangle Q.

.....

(3 marks)

5 (a) Complete the following.

$$\frac{3}{4} = \boxed{\frac{3}{28}}$$

$$\frac{1}{7} = \frac{28}{28}$$

(2 marks)

5 (b) Simplify $\frac{3x}{4} + \frac{x}{7} - \frac{x}{2}$

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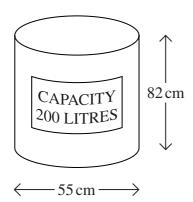
Turn over for the next question

10

6	(a)	Solve the equation $\frac{y}{4} + 1 = 3 - y$
		Answer $y = \dots (3 \text{ marks})$
6	(b)	List all the integer solutions of the inequality $-6 \le 3n < 5$
		Answer (3 marks)
6	(a)	Calva the simultaneous equations
6	(c)	Solve the simultaneous equations
		4x + y = 5 $3x - 2y = 12$
		Do not use trial and improvement.
		You must show your working.
		Anoman (2 1)
		Answer $x = \dots, y = \dots (3 \text{ marks})$



7 The diameter of a cylindrical water-butt is 55 cm. The height is 82 cm.



Not drawn accurately

One litre = $1000 \, \text{cm}^3$

Is this accurate?

The label states that the capacity of the water-butt is 200 litres.

You must snow your w	orking.	
		(4 marks)
(a) Multiply out	x(3-x)	, , ,
	Answer	(1 mark)

8 (b) Expand and simplify (2q-7)(3q-4)

Answer

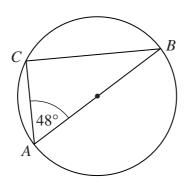
Turn over ▶

(3 marks)



8

9 AB is a diameter of the circle shown. Angle BAC is 48°



Not drawn accurately

- 9 (a) Give a reason why angle ACB is a right angle.

 (1 mark)
- 9 (b) The length of AB is 8.6 cm.

Calculate the length of *BC*.

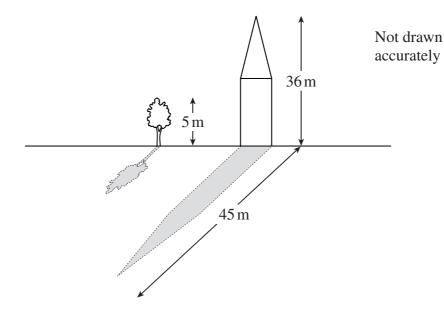
Give your answer to a suitable degree of accuracy.

10 Show that $(y+2)^2 - (y-2)^2 \equiv 8y$

.....

(3 marks)

A church spire is 36 metres high and a tree is 5 metres high. At 4pm, the shadow of the church spire is 45 metres long.



Answer m	(3 marks)
salesane the rengin or the state of the tree.	
Calculate the length of the shadow of the tree.	

Turn over for the next question

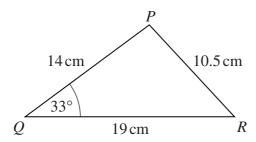
11



12 Make v the subject of the formula $f = \frac{uv}{u+v}$	
Answer	(4 marks)



13 In triangle PQR, angle $Q = 33^\circ$, QP = 14 cm, PR = 10.5 cm and QR = 19 cm.



Not drawn accurately

10

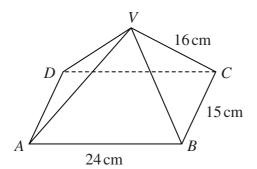
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(3 marks)



14 *VABCD* is a pyramid.

The vertex V is directly above the centre of the rectangular base ABCD. AB = 24 cm, BC = 15 cm and each slant edge is 16 cm.

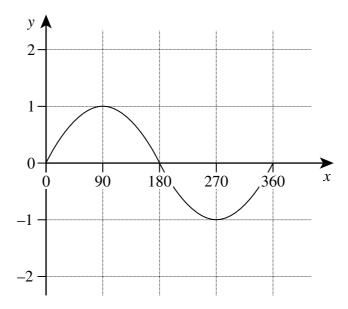


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Calculate the vertical height of the pyramid.
Answer cm (5 marks)



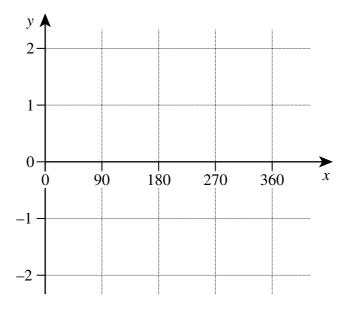
15 The graph $y = \sin x$ is shown for $0^{\circ} \le x \le 360^{\circ}$



15 (a) Describe how you would use the graph of $y = \sin x$ to sketch the graph of $y = 1 + \sin x$

(1 mark)

15 (b) On the grid below, sketch the graph of $y = \sin 2x$ for $0^{\circ} \le x \le 360^{\circ}$



END OF QUESTIONS

(1 mark)

