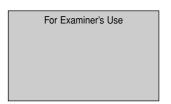
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Centre Number						Candidate Number			
Candidate Signature									



General Certificate of Secondary Education November 2008

# MATHEMATICS (MODULAR) (SPECIFICATION B) Module 5 Higher Tier Paper 1 Non-calculator





Thursday 6 November 2008 9.00 am to 10.15 am

#### For this paper you must have:

· mathematical instruments.



You must not use a calculator.

Time allowed: 1 hour 15 minutes

#### **Instructions**

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Answers written in margins or on blank pages will not be marked.
- Do all rough work in this book.

#### **Information**

- The maximum mark for this paper is 70.
- The marks for questions are shown in brackets.
- You may ask for more answer paper, graph paper and tracing paper. This must be tagged securely to this answer book.

#### **Advice**

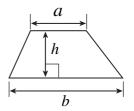
• In all calculations, show clearly how you work out your answer.

For Exam	iner's Use
Pages	Mark
3	
4-5	
6–7	
8-9	
10-11	
12-13	
14-15	
TOTAL	
Examiner's Initials	

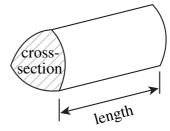


## Formulae Sheet: Higher Tier

Area of trapezium =  $\frac{1}{2}(a+b)h$ 

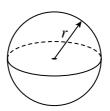


**Volume of prism** = area of cross-section  $\times$  length



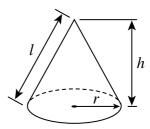
Volume of sphere = 
$$\frac{4}{3}\pi r^3$$

**Surface area of sphere** =  $4\pi r^2$ 



Volume of cone = 
$$\frac{1}{3} \pi r^2 h$$

Curved surface area of cone =  $\pi rl$ 

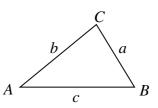


In any triangle ABC

**Area of triangle** =  $\frac{1}{2}ab \sin C$ 

Sine rule 
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

**Cosine rule**  $a^2 = b^2 + c^2 - 2bc \cos A$ 



# The Quadratic Equation

The solutions of  $ax^2 + bx + c = 0$ , where  $a \ne 0$ , are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

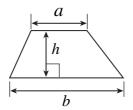
## Answer all questions in the spaces provided.

1 The diagram shows a trapezium.

 $a = 5 \,\mathrm{cm}$ 

 $b = 7 \,\mathrm{cm}$ 

 $h = 4 \,\mathrm{cm}$ 



Not drawn accurately

Work out the area of the	trapezium.		
State the units of your a	nswer.		
•			
	•••••	 	 
	•••••	 	 
	Answer	 •••••	 (3 marks)

Turn over for the next question

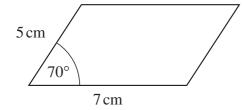


2	(a)	Factorise fully	$x^3 - 4x^2$	
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.....

2 (b) Work out the value of  $14^3 - 4 \times 14^2$ 

3 The diagram shows a sketch of a parallelogram.

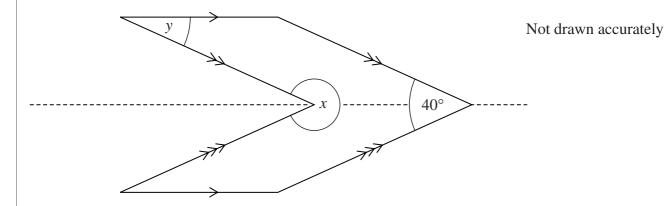


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Make an accurate drawing of the parallelogram.

(3 marks)

4 The diagram shows a chevron. It has one line of symmetry as shown.



4 (a) Work out the value of x.

••••	 	 
••••	 	 

Answer ...... degrees (2 marks)

**4** (b) Work out the value of y.

Answer ...... degrees (2 marks)

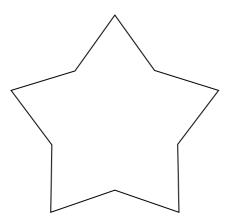


5	(a)	Shad	Shaded and unshaded circles are used to make a sequence of patterns as shown.					
			0					
		Pa	attern 1	Pattern 2	Pattern 3	Pattern 4		
5	(a)	(i)	There are 12	2 unshaded circles in	nshaded circles in Pattern 6.			
			Work out th	e number of shaded	circles in Pattern 7.			
				Answer			(1 mark)	
5	(a)	(ii)	There are $n$	unshaded circles in	Pattern $p$ .			
			Write down	the number of shade	ed circles in Pattern	(p + 1).		
				Answer			(1 mark)	
5	(a)	(iii)	The total nu	mber of circles in a	pattern is given by t	he formula		
				$C = \frac{p}{n}$	$\frac{(p+1)}{2}$			
			C is the tota $p$ is the patt	al number of circles. ern number.				
			Work out th	e value of $C$ when $p$	= 100			
							(2 marks)	

5	(b)	The <i>n</i> th term of a sequence is given by the formula $2n - 1$
		Write down the first four terms of the sequence
		Write down the first <b>four</b> terms of the sequence.
		Answer
6	(0)	Solve $6x + 9 = 2x + 7$
6	(a)	Solve $0x + 9 = 2x + 7$
		Answer $x = \dots (3 \text{ marks})$
6	(b)	Expand and simplify $3(7a-5b) + 2(4a-3b)$
Ü	(0)	2. Apania ana simping (14 00)   2(14 00)
		Answer (3 marks)
		This wer
6	(c)	Given that $a = 8$ , $b = -3$ , $c = 1$ and $d = -5$
		a + b
		work out the value of $\frac{a+b}{cd}$
		Answer



7 The diagram shows a decagon. All the sides are equal in length.



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The interior angles of the decagon have a sum of  $1440^{\circ}$ . Each reflex interior angle is  $200^{\circ}$ .

Work out the size of each acute interior angle.

	Answer	deorees	
•••••		 	



8	(a)	Simplify $8^4 \times 8^5$ Leave your answer as a power of 8.	
		Answer	(1 mark)
8	(b)	Simplify $w^6 \div w^2$	
		Answer	(1 mark)
8	(c)	Chris simplifies $3x \times 4x^5$	
		His answer is $7x^5$	
		Explain the mistakes he has made.	
			(2 marks)
8	(d)	Simplify fully $15y^6z^3 \div 5y^2z$	
		Answer	(2 marks)

10



9 Here are some expressions.r, h, l, w and b represent lengths.

$\pi r^2$	$\pi r^2 h$	2l + 2w	lwh	$\frac{1}{2}bh$	$2\pi r$

9	(a)	Put a tick und	ler each ex	coression v	which re	presents	volume
,	(a)	I ut a tick uni	ici cacii cz	vpression v	willell le	presents	Volume

(2 marks)

9	(b)	Ismail says that any expression containing exactly two letters must represent area.
		Is he correct? Explain your answer.
		(2 marks)



10	You	ma	y u	se	the	gr	rap	h !	paj	er	· b	elo	W	to	h	elp	Эу	ou	ıw	ith	tŀ	is	qι	ies	ti	on											
	The	poi	nts	<i>A</i> (	0,	10)	) a	nd	<b>B</b> (	(5,	-2	2) a	are	; jo	oin	ied	l b	y a	a si	rai	igł	nt ]	lin	e.													
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10	(b)		(i)	W	<sup>7</sup> orl	k o	ut	the	e g	rac	die	nt	of	î li	ne	· A	В.																				
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									A	ns	we	r.	••••			· • • •	••••			• • • •			· • • •	•••			••••							(2	ma	ırk	s)
10	(b)	(	ii)	W	<sup>7</sup> rit	e d	lov	vn	th	e e	qu	ati	ior	10	f 1	ine	e A	B																			
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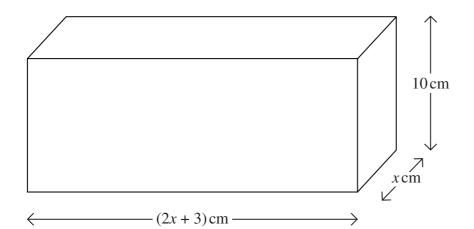
Turn over ▶

10



11 The diagram shows a cuboid.

The volume of the cuboid is 900 cm<sup>3</sup>.



Not drawn accurately

11 (a) Show that  $2x^2 + 3x - 90 = 0$ 


(3 marks)

11 (b) Solve  $2x^2 + 3x - 90 = 0$ 

 	 •••••	
 	 	••••••
 	 	•••••

Answer .....

(3 marks)

11	(c)	Here is a similar cuboid.
		Not drawn accurately
		Work out the volume of this cuboid.
		Answer cm <sup>3</sup> (3 marks)

Turn over for the next question



12	Simp	plify fu	$\frac{4x^2 - 25}{6x^2 - 15x}$	
			Answer	(3 marks)
13	(a)	$\mathbf{s}$ and $\overrightarrow{AB} =$	t are vectors.	
		$\overrightarrow{BC} =$	s + t $2s + t$ $s + 2t$	
13	(a)	(i)	Show that $\overrightarrow{BD}$ is parallel to $\overrightarrow{AB}$ .	
				(2 marks)
13	(a)	(ii)	Write down the ratio $BD: AB$	
13	(a)	(iii)	Answer	(1 mark)
				(1 mark)



13	(b)	O is the origin.  F, G and H are three points such that
		$\overrightarrow{OF} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$
		$\overrightarrow{OG} = \begin{pmatrix} 3 \\ -3 \end{pmatrix}$
		$\overrightarrow{OH} = \begin{pmatrix} 6 \\ 2 \end{pmatrix}$
		Prove that angle <i>GFH</i> is a right angle. You <b>must</b> show your working.
		(4 marks)

END OF QUESTIONS

11

