

# General Certificate of Secondary Education 

## Mathematics 4306 <br> Specification A

## Paper 2 Foundation

Mark Scheme<br>2009 examination - November series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

[^0]Copyright © 2009 AQA and its licensors. All rights reserved.

## COPYRIGHT

AQA retains the copyright on all its publications. However, registered centres for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to centres to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Set and published by the Assessment and Qualifications Alliance.

## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Mdep A method mark dependent on a previous method mark being awarded.
B dep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe
Or equivalent. Accept answers that are equivalent.
eg, accept 0.5 as well as $\frac{1}{2}$

| Q | Answers | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{1 a}$ | Coventry | B1 | C |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 b}$ | Dundee | B1 | D |
| $\mathbf{1 c}$ | 7000000 | B1 | $7,000,000$ |
| $\mathbf{1 d}$ | 32800 | B1 | 32,800 |


| 2a | Tangent | B1 | Straight line is B0 |
| :---: | :--- | :---: | :--- |
| 2bi | $2.9-3.1 \mathrm{~cm}$ | B1 |  |
| 2bii | $2 \times$ their 2b | B1ft | $5.8-6.2$ oe |
| 2c | $90^{\circ}$ | B1 | Right angle. Allow $88-92$ |


| 3a | Green | B1 | G |
| :---: | :--- | :---: | :--- |
| 3b |  | B1 15 or $1 / 3$ | 0.33 or better, $33 \%$ or better <br> B0 for ratio or odds or 1 in 3 or 5 in 15 <br> B0 for 1 out of 3 or 5 out of 15 |
| 3c | 0 or $\frac{0}{15}$ | B1 | Bero, Impossible, None <br> B0 for ratio or odds or choice or $($ a number other than 15$)$ <br> B1 for 0 out of 15 or 0 in 15 provided <br> 5 in 15 or 5 out of 15 seen in part(b) |
| 3d | Mark at ${ }^{8} / 15$ | B1 | $\pm 2$ mm. Ignore any markings for red |
| Arrow not needed provided clear indication |  |  |  |


|  |  |  |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |


| $\mathbf{5 a}$ | $1,2,3,4,6,12$ | B2 | -1 eeoo Allow repetitions |
| :---: | :--- | :---: | :--- |
| $\mathbf{5 b}$ | 12 and $18,12+18$ | B2 | -1 eeoo OK to just circle or underline correct <br> answers |
| $\mathbf{5 c}$ | 11 or 13 or 17 or 19 | B1 | Accept more than one correct answer |
| $\mathbf{5 d}$ | All other prime numbers are odd | B1 | No more even <br> Because 2 will go into all even numbers <br> They would divide by either 2 or 3 |


| $\mathbf{6 a}$ | 148.877 | B1 | Accept $148.88,148.9$ but 149 is B0 |
| :---: | :--- | :---: | :--- |
| $\mathbf{6 b}$ | $6.057 \ldots$. allow more than 4 sf | B1 | Accept 6.06 <br> $6,6.05,6.1$ are all B0 |


| 7ai | $-5+8(=3)$ | B1 |  |
| :---: | :--- | :---: | :--- |
| 7aii | $-2+3-4(=-9)$ <br> $-2+-3+-4$ | B1 | Allow $-2-3=-5-4$ <br> B0 for just $-5-4$ on its own, <br> B0 for $-2-7$ on its own, <br> B0 for $-2-3+-5-4,-2=-3+-4$ |
| 7bi | Correct values | B1 | eg 10 and 6 |
| 7bii | Correct values | B1 | eg -2 and 0 |


| 8 |  | 5 |  |  | B2 | Or correct number of dots in each case |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3 | 6 | 4 | 1 |  |  |
|  |  | 2 |  |  |  |  |
|  |  |  |  |  |  | -1 eeoo |


| 9 | Any number between 0.2857 and |
| :--- | :--- |
| 0.42857 |  |
| eg $\frac{5}{14}, \frac{10}{28}$ oe |  |

B2 | B1 for a fraction rewritten with common |
| :--- |
| denominator that is a multiple of 7 or 0.286 and |
| 0.429 seen |
| B1 for eg $\frac{2.2}{7.3}, \frac{2.5}{7}, \frac{7.5}{21}$ oe |
| 212 sevenths |
| B0 for percentage |

| 10a | 74 | B1 | 74.0 |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 0 b i}$ | $2 \times 6+38=12+38$ | B1 | Must be evaluated to $12+38$ <br> Allow $50-38=12,12 \div 6=2$ |
| $\mathbf{1 0 b i i}$ | 80 | B1 |  |
| $\mathbf{1 0 b i i i}$ | 10 | B2 | Allow embedded answer eg $10 \times 6+38$ gets 2 <br> marks unless contradicted on answer line when only <br> 1 mark <br> B1 for 60 seen or $98-38 \div 6$ with or without brackets |
|  | 56 | B1 |  |
|  | 62 or their $56+6$ | B1ft |  |


| $\mathbf{1 1 a}$ | 6 | B1 | 6.0 |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 1 b}$ | Any rectangle with an area $12 \mathrm{~cm}^{2}$ | B1 |  |
| $\mathbf{1 1 c}$ | Any rectangle with a perimeter of <br> 12 cm | B1 |  |
| $\mathbf{1 1 d}$ | Any triangle with an area of $6 \mathrm{~cm}^{2}$ | B1 |  |


| 12a | Any angle bigger than 0 and less than <br> 90 | B1 |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{\text { 12b }}$ | Bigger than 90 and less than 180 | B1 | Be generous about whether 90 and/or 180 are <br> included provided both numbers are mentioned <br> eg between 90 and 180, <br> In range $90-180$ <br> But 'bigger than $90^{\prime}$ ' is B0 |
|  | Approx. isosceles triangle drawn with <br> angle $90^{\circ}$ shown (or right angle sign) | B1 |  |
|  | At least one $45^{\circ}$ shown or 2 sides <br> adjacent to 90 marked as equal with <br> numbers or a dash | B1 | B0 if hypotenuse and a side are marked as equal |


| 13a | 180 | B1 |  |
| :--- | :--- | :---: | :--- |
| 13b | B | B1 |  |
| 13c | 070 or 70 may be on diagram | B1 | 68 to 72,068 to 072 inclusive |
| 13d | 100 may be on diagram | B1 | 98 to 102,098 to 102 inclusive |


| $\mathbf{1 4 a}$ | B and C | B1 |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1 4 b}$ | A and D | B1 |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
| 14c |  |  |  |  |
|  |  |  |  | Or rotation of this diagram. |
|  |  |  |  | Must see correct internal line |


| $\mathbf{1 5 a}$ | Paper | B1 |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 5 b}$ | Glass and Plastic | B1 |  |
| $\mathbf{1 5 c}$ | $29-31$ | B1 |  |
| $\mathbf{1 5 d}$ | Bar over twice as high | B1 | oe eg $23 \times 2=46<60$. <br> 2002 is lower than 30 and 2005 is 60. <br> $2002=22$ and $2005=60$ gets B1 as do not need to <br> make a comparison |
| $\mathbf{1 5 e}$ | $1.7 \div 5.5(\times 100)$ | M1 | Oe |
|  | $31 \%$ | A1 | 30.9 or better with no working is M1A0 |


| $\mathbf{1 6 a}$ | $6 w=14+4$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | 3 | 36 | A1 |
| 3.0 |  |  |  |
| $\mathbf{1 6 c i}$ | Any valid values | B1 | 36.0 |
| 16cii | Any negative valid values | B1 | Eg $x=2, y=9$ oe $(4,13)$ <br> Do not accept $x=0$ or $y=0$ |


| $\mathbf{1 7 a}$ | $40 \times 12+200$ | B1 | $40 \times 0.12+2$ <br> just $4.80+2$ is B0 as must show that 40 prints cost <br> $£ 4.80$ |
| :---: | :--- | :---: | :--- |
|  | $100 \times 10+200$ or <br> $101 \times 8+300$ | M1 | $100 \times 0.1+2$ or <br> $101 \times 0.08+3$ |
|  | 1200 and 1108 | A1 | $£ 12.00$ and $£ 11.08$ |
|  | 92 p | A1 | $£ 0.92 \mathrm{p}$ gets full marks <br> but working with an answer of 0.92 p gets M1A1A0 |
| $\mathbf{1 7 c} \mathbf{c}$ | $7 \div 0.1$ | M1 | $700 \div 10$ |


| $\mathbf{1 8}$ | $12 \times 60 \times 10(=7200)$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $32400 \div$ their 7200 | M1 |  |
|  | 4.50 | A1 | 4.5 is A0 |


| 19 | B2 | B1 any enlargement sf 3 or enlargement from (0, 6) <br> with sf 2 <br> B1 for any 2 vertices in correct position and any <br> two sides the correct length |  |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1 9}$ | Rays from (0,6) through at least 3 <br> points | M1 |  |
| Alt | Correct shape | A1 |  |


| 20a | 16 | B1 |  |
| :---: | :---: | :---: | :---: |
| 20b | 27.50 | B1 | 27.5 scores B0 |
| 20c | $5 \text { /their(20a)answer }$ | B1 | $\begin{aligned} & 0.3125,0.312,0.313 \text {, oe } \\ & 31.25 \%, 31.2 \%, 31.3 \% \text { oe } \end{aligned}$ <br> Not ratio or odds or 5 in 16 or 5 out of 16 etc |
| 20d | $1 \text { - their }{ }^{5} / 16$ | B1ft | $\begin{aligned} & 0.6875,0.687,0.688 \text { oe } \\ & 68.75 \%, 68.7 \%, 68.8 \% \text { oe } \\ & \text { not ratio or odds } \\ & \text { allow } 11 \text { in } 16 \text { or } 11 \text { out of } 16 \text { if } 5 \text { in } 16 \text { or } 5 \text { out of } \\ & 16 \text { seen in } 20 \text { c } \end{aligned}$ |
| 20e | $\Sigma x$ for $\geq 14$ values $\begin{aligned} & 8+8+9+12+16+18+25+25+ \\ & 30+32+33+37+46+50+56+59 \\ & (=464) \end{aligned}$ <br> Or subtotals $25+46+50+132+46+165$ and must get one of 132 and 165 | M1 | Allow up to 3 misread errors but must include 1 of 30 and 50 . Any indication that the S\&L diagram is misunderstood, eg 0 for 30 $10+2+6+8=26$ for second row is M0 |
|  | Their $464 \div$ their(20a)answer | M1Dep |  |
|  | 29 | A1 |  |


| 21a | Too small a sample | B1 | oe eg They are only asking 10 people. <br> 10 people will not tell you how popular the <br> programmes are. |
| :---: | :--- | :---: | :--- |
|  | Biased sample | B1 | oe eg Most at school or work <br> Most don't watch TV during these times |
| 21b | Not enough choice of programmes <br> Not enough choice of responses <br> Leading question or biased | B1 | oe eg No 'No' box <br> Can't choose between them. <br> What if they don't watch these shows. |


| 22 | $5 x<9-3$ | M1 | $x<1 \frac{1}{5} \quad x<\frac{6}{5}$ |
| :--- | :--- | :---: | :--- |


| $\mathbf{2 3}$ | Any value -infinity $\leq x \leq 1$ stated | B1 |  |
| :---: | :--- | :---: | :--- |
|  | Show that for the chosen value of $x, x^{2}$ <br> $\geq x^{3}$. Must be evaluated correctly and <br> compared. | B1dep | B1B0 for ' $1^{2} 1^{3}$ as $1<1$ <br> B1B0 for ${ }^{\prime} 1^{2}=1 \quad 1^{3}=11^{2}>1^{3}$, |


| $\mathbf{2 4 a}$ | $\pi \times 12^{2} \div 2$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | 226 to 226.224 | A1 | $72 \pi$ |
| $\mathbf{2 4 b}$ | $100 \mathrm{~cm}=1 \mathrm{~m}, 400 \mathrm{~cm}=4 \mathrm{~m}$ oe | B1 | Accept dividing by 100 <br> $1 \mathrm{~m}^{2}=100 \mathrm{~cm}^{2}$ is B0 |
|  | $\div 100 \div 100$ | B1dep | oe but just $40000 \div 10000=4$ is B0B0. <br> $10000 \mathrm{~cm}^{2}=1 \mathrm{~m}^{2}$ so $40000 \mathrm{~cm}^{2}=4 \mathrm{~m}^{2}$ is B0B0 |
|  | $1 \mathrm{~cm}=0.01 \mathrm{~m}$ | B1 |  |
| ALT | $40000 \times 0.01 \times 0.01$ | B1dep |  |


| $\mathbf{2 5 a}$ | $0.5+0.1 \times 1500 \times 0.1$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | 15.50 | A1 | 15.5 is A0 |
| $\mathbf{2 5 b}$ | $1: 8$ |  | $\frac{1}{8}$ and $8: 1$ are B0 |
|  |  | B1 | 8 |
| $\mathbf{2 5} \mathbf{c} \mathbf{c}$ | $3.5+0.02 \times 12000 \times 0.1(=27.5)$ | M1 | 27.50 |
|  | their $8 \times$ their $15.5-$ their 27.5 | M1Dep | $124-27.50$ |
|  | 96.50 | A1 | 96.5 is A0, but allow 96.5 if 15.5 seen in part(a) |


[^0]:    Further copies of this Mark Scheme are available to download from the AQA Website: www.aqa.org.uk

