

# General Certificate of Secondary Education 

## Mathematics 4306 Specification A

Paper 2 Foundation

## Mark Scheme

2009 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Mdep A method mark dependent on a previous method mark being awarded.
B dep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$

## Paper 2F

| Q Answer | Mark | Comments |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 ( a )}$ 46009 B1 46,009 but B0 for 46.009 <br> $\mathbf{1 ( b )}$ Any number in range <br> 2000 to 3000 B1 Do not allow 2000 or 3000 <br> $\mathbf{1 ( c )}$ $1,2,5,10$ B2 B1 For 3 correct <br> $\mathbf{1 ( d ) ( i ) ~}$ 6790 B1  <br> $\mathbf{1 ( d ) ( i i ) ~}$ 6800 B1  |  |  |


| $\mathbf{2}$ | All correct heights for bars <br> $10,12,15,18,8$ | B1 | If no bar allow plotted $x$ for height <br> Allow single lines |
| :---: | :--- | :---: | :--- |
|  | Equal width bars | B1 | Bars must not be single lines |
|  | Bars labelled Y8, Y9, Y10, Y11 | B1 | Allow 7, 8, 9, 10, 11 as labels <br> Bars must not be single lines <br> Labels must be in middle of bar <br> Allow labels in bars and not on the axes <br> SC2 For 4 fully correct bars and <br> one incorrect or missing bar |


| $\mathbf{3 ( a ) ( i )}$ | Diameter | B1 |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{3 ( a ) ( i i ) ~}$ | Chord | B1 |  |
| $\mathbf{3 ( a ) ( i i i ) ~}$ | Radius | B1 |  |
| $\mathbf{3 ( b )}$ | Line touching circle at A <br> on either diagram | B1 | B0 If crosses circle <br> Do not penalise for another tangent at some <br> other point in addition to a correct one at A |


| 4(a) | 28 and 5 | B1 | Any order |
| :--- | :--- | :---: | :--- |
| 4(b) | 25,4 and 6 | B1 | Any order. All 3cards must be different <br> eg, 25, 5, 5 is not allowed |
| 4(c) | $25-6$ | B1 | Must be in this order |
| 4(d) | $25 \times 4$ | B1 | or 4 $\times 25$ |
| 4(e) | $50 \div 5$ | B1 | Must be in this order |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 5(a) | Correct number of tiles 6 and 8 | B1 | Allow different types of shading or striping; but B1total for correct 6 and 8 parts and no shading or incorrect shading |
|  | Correct discriminatory shading of their 6 and their 8 (must not be of pattern 1, 2 or 3 ) | B1 ft |  |
| 5(b) | Shaded 6 and 7 and striped 8 and 10 | B1 |  |
|  | Total 1417 | B1 ft | For adding their 6 and their 8 , and their 7 and their 10 |
| 5(c) | 32 | M1 | Continuing to add on 3 with a max. of one arithmetic error and at least 3 terms |
|  |  | A1 | SC1 $12+20$ |


| 6(a) | Both 6 (do not need 'Yes') <br> If box is ticked it must be the <br> correct one | B1 | Answer in range 20 to 21from measuring the <br> perimeters <br> Must have numbers |
| :---: | :--- | :---: | :--- |
| $\mathbf{6 ( b )}$ | Triangle $=4$ and hexagon =6 <br> (do not need 'No') <br> If box is ticked it must be the <br> correct one | B1 | Area triangle $=19.5$ to 19.9 and area <br> hexagon $=29.4$ to 29.8 from calculating the <br> areas <br> Must have numbers <br> Allow statements such as: <br> 'Two more triangles in hexagon'; '4 and 6', |


| 7(a) | If do not fill in any sectors but <br> write down 'all 5 numbers are 2, <br> or 'all numbers are2' oe | B1 | If fill in sectors then B0 if leave any sector <br> blank <br> B0 For correct statement and incorrect filling <br> in of diagram |
| :---: | :--- | :---: | :--- |
| 7(b) | If do not fill in any sectors but <br> write down 'All 5 numbers are <br> not even' oe | B1 | NB 0 is an even number <br> If fill in sectors then B0 if leave any sector <br> blank <br> B0 For correct statement and incorrect filling <br> in of diagram |
| 7(c) | If do not fill in any sectors but <br> write down ' Two of number 3 <br> and any other 3 numbers' | B1 | If fill in sectors then B0 if leave any sector <br> blank <br> B0 For correct statement and incorrect filling <br> in of diagram |


| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| $\mathbf{8}$ $3 \times 16200 \div 100$ M1 oe <br>  486 A1 SC1 For 16686 unless from fw when scores <br> both marks |  |  |


| 9 | $1.89-0.45$ or 1.44 | M1 | $189-45$ or 144 |
| :---: | :--- | :---: | :--- |
|  | Their $1.44 \div 0.9$ | M1 dep | Their $144 \div 90$, their $1.44 \div 90$ <br> Their $144 \div 0.9(0)$ or 160 or 0.016 seen |
|  | 1.6 | A1 | $1.60,1 \frac{3}{5}$ |


| $\mathbf{1 0 ( a )}$ | 60 (answer may be on diagram) | B1 | 60.0 |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 0 ( b )}$ | Drawing ft their(a) for arrow | B1 ft | Allow correct arrow here even if part(a) is not <br> attempted or part (a) is wrong <br> Must be an arrow drawn but it can slope |
| $\mathbf{1 1 ( a )}$ | 4 | B1 | $4.0, \frac{28}{7}, 28 / 7 \quad$ B0 For $28 \div 7$ |


| 11(b) | 40 | B2 | B1 For 40y or B1 for $(y=) 8$ provided there is <br> no other answer <br> eg, $y=8,48 \div 5=9.6$ and 9.6 on <br> answer line is B0 |
| :---: | :--- | :---: | :---: |
| $\mathbf{1 1 ( c )}$ | $(3 \times 7)-20$ | M1 | $21+20$ is M0 |
|  | 1 | A1 | Allow $3 x+5 y=1 \quad$ SC1 For 21x-20y |


| 12(a)(i) | 65 | B1 |  |
| :---: | :--- | :---: | :--- |
| 12(a)(ii) | 105 | B1 |  |
| 12(b) | Total is 390 not 360 | B1 | Need both numbers but allow just a few words <br> eg ' 390 not 360 ' |
| $\mathbf{1 2 ( c )}$ | $180 \div 5$ | M1 |  |
|  | 36 | A1 |  |
| $\mathbf{1 2 ( d )}$ | $180-(90+43)$ | M1 | $90-43$ |
|  | 47 | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 13(a) | 15 | B1 |  |
|  | 11 | B1ft | Their 15-4 |
| 13(b) | Subtract 4 or $35-4 n$ <br> May be seen in part(a) | B1 | oe take away 4 , minus $4,-4$, take 4 off but B 0 for $n-4, n=-4, x=-4,-4 n$, difference of 4 etc |
| 13(c) | Terms are -1 and -5 (need both numbers) <br> May be seen in part(a) | B1 | oe $-1-4=-5$ <br> $35-4 n=-3$ does not have an integer solution |


| 14(a)(i) | $\frac{1}{50}$ | B1 | $2 \%, 0.02 \text { oe }$ <br> ' $\frac{1}{50}$ or $1: 50$ ' on answer line is B0 |
| :---: | :---: | :---: | :---: |
| 14(a)(ii) | $\frac{10}{50} \text { or } \frac{5}{25} \text { or } \frac{2}{10} \text { or } \frac{1}{5}$ <br> or $20 \%$ or 0.2 | B2 | B1 For $\frac{11}{50}$ or $\frac{9}{50}$ or equivalent $\%$ or decimal. <br> B1 For $10 /($ any number $>10$ ) or 10 out of 50 scores B1 <br> ‘ $\frac{10}{50}$ or $10: 50$ ' on answer line is B0 |
| 14(b)(i) | $\frac{20}{50}$ or $\frac{10}{25}$ or $\frac{2}{5}$ or $\frac{4}{10}$ or $40 \%$ or 0.4 | B2 | B1 For 20/(any number>20) or 20 out of 50 scores B1 |
| 14(b)(ii) | $\frac{3}{5} \text { oe or } 1-\text { their }(\mathrm{b})(\mathrm{i})$ | B1ft | eg 30 out of 50 scores B1 ft provided 20 out of 50 is seen in part(b)(i) |


| 15(a)(i) | 51.8(4) | B1 | $\frac{1296}{25}$ must be 3significant figures at least |
| :---: | :---: | :---: | :---: |
| 15(a)(ii) | 2.68(328...) | B1 | Must be 3significant figures at least B0 For $6 \sqrt{ } 5 / 5$ |
| 15(a)(iii) | 373(.248) | B1 | $\frac{46656}{125}$ must be 3 significant figures at least |
| 15(a)(iv) | 1.93... | B1 | Must be 3significant figures at least |
| 15(b) | 5 | B1 | 5.(000 ...) |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{1 6 ( a )}$ | $4 \times 14.80$ or $4 \times 1480$ | M1 | $59.2(0) \quad$or $4 \times$ their $(14.8(0)+3.2(0))$ <br> or $4 \times 1800$ |
| :--- | :--- | :---: | :---: |
|  | $5 \times 3.20$ or $5 \times 320$ | M1 | $16+3.20$ or +320 |
|  | 75.20 <br> or 7520 p and $£$ sign crossed out | A1 | M2 Only for 75.2 |
| $\mathbf{1 6 ( b ) ~}$ | $111.20-3.20$ | M1 | $111.20-$ their 75.20 |
|  | Their $108 \div(3.20+14.80)$ | M1dep | $36 \div 18(=2)$ |
|  | 6 | A1 |  |


| $\mathbf{1 7}$ | $40 \times 20 \div(10 \times 10)$ | M1 | $40 \times 10$ or $20 \times 20$ |
| :---: | :--- | :---: | :--- |
|  | 3 | A1 | 8 with no working is M0 A0 |


| $\mathbf{1 8 ( a )}$ | 15625 | B1 | $15625 .(0)$ |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 8 ( b )}$ | Because $5 \times 5=\ldots 5$ | B1 |  |
|  | This then repeats for each power | B1 |  |


| 19 |  | B3 | Allow front and side elevations to be transposed <br> Allow Plan to be a rotation. <br> B1 for each |
| :---: | :---: | :---: | :---: |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 20(a) | $3 \mathrm{R}+4 \mathrm{Q}$ or $\mathrm{R} \times 3+\mathrm{Q} \times 4$ | B1 | $4 Q+3 R$ allow lower case letters <br> Need + sign, <br> Expression need not be simplified <br> B0 For R3 or Q4, $\mathrm{R}^{3}+\mathrm{Q}^{4}$ |
| :---: | :---: | :---: | :---: |
| 20(b) | Square around diagram | M1 | R2 or Q4 in two term expression <br> $2 R$ or 4 Q in two term expression <br> $\mathrm{R} \times 2$ or $\mathrm{Q} \times 4$ in two term expression |
|  | $2 \mathrm{R}-4 \mathrm{Q}$ or $2(\mathrm{R}-2 \mathrm{Q})$ | A1 | Allow lower case letters, need - sign <br> Expression need not be simplified <br> $R \times 2-Q \times 4$ scores full marks <br> Penalise 1 mark for R2 or Q4 or both eg, R2 - Q4 scores 1 mark <br> $R 2-4 Q$ scores 1 mark <br> But $\mathrm{R}^{2}-\mathrm{Q}^{4}$ is M0 A0 |


| 21(a) | $1.8970 \ldots$ | B1 | $\frac{129}{68}$ or $1 \frac{61}{68}$ |
| :--- | :--- | :---: | :--- |$|$| B1ft | ft Any value $\geq 3 \mathrm{sf}$ <br> or any value with at least 3 dp <br> 1.90 is B0 |
| :--- | :--- |
| 21(b) | 1.9 |


| 22(a) | $7 x-3 x=5+9$ | M 1 | Allow one sign error |
| :--- | :--- | :---: | :--- |
|  | $4 x=14$ | A 1 |  |
|  | $3.5,3 \frac{1}{2}, \frac{14}{4}, \frac{7}{2}$ | A 1 ft | ft On one error only |
| $2 \mathbf{2 2 ( b )}$ | $7 y-7 \times 9=3 y+5$ | M 1 | Multiply both by 7, allow one error in first <br> or second line |
|  | $7 y-3 y=5+7 \times 9$ | A 1 | $4 y=68$ |
|  | 17 | A 1 ft | ft On one error only |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 23 | Correct key example | B1 | Numbers in key do not need to be one of the data values |
|  | 1 9    <br> 2 2 2 7 9 <br> 3 3 5   <br> 4 2 5 6  <br> 5 3 6 8  <br> 6 7 8   | B2 | Correct and ordered <br> B1 For 1 or 2 omissions or 1 or 2 extras or correct but not ordered |


| 24(a) | $\frac{1}{2} \times \pi \times 3^{2}$ or $\frac{1}{4} \times \pi \times 3^{2}$ | M1 | $7.06(\ldots), 7.07(\ldots) 14.1$ <br> Allow 6 as radius 56 to 57, 28.(...) <br> Beware $\pi^{2} \times \frac{3}{4}=7.402$ so if no working is seen only allow the ranges above |
| :---: | :---: | :---: | :---: |
|  | 36 - their 14.1 | M1dep |  |
|  | 21.8-21.9 | A1 | $36-4.5 \pi$ or 22 with working |
| 24(b) | (No), it has two lines of symmetry | B1 | oe does not need 'No' or 'lines of symmetry' provided clear implication <br> eg, only has 2 , only 2 , it has 2 <br> But just ' 2 ' is B0 |


| 25 | $500-379$ | M1 | 121 |
| :---: | :--- | :---: | :--- |
|  | Their $(500-379) \div 500 \times 100$ | M1dep | Can use 'build up' method <br> eg, £ $100=20 \%, £ 20=4 \%, £ 1=0.2 \%$ <br> M2 For $100-379 / 500 \times 100$ |
|  | 24.2 | A1 |  |


| $\mathbf{2 6}$ | $3,4,7$ <br> $11,12,23$ <br> 14,16 | B2 | B1 For 7 out of 8 cells correct <br> or B1 For 2 of these <br> (provided all 8 cells are completed): <br> two more girls than boys <br> a quarter of girls are left handed <br> total left handed is 7 |
| :---: | :---: | :---: | :---: |


[^0]:    Set and published by the Assessment and Qualifications Alliance.

