

General Certificate of Secondary Education

Mathematics 4301
Specification A
2008

SPECIMEN ASSESSMENT MATERIALS



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Introduction

The GCSE awarding bodies have prepared revised specifications to incorporate the range of features required by GCSE and subject criteria. The specimen assessment material accompanying the specifications is provided to give centres a reasonable idea of the general shape and character of the planned question papers in advance of the first operational examination.

Papers

These specimen question papers have been designed to exemplify the question papers, Papers 1 and 2, to be set for Specification A, for first examination in June 2008. The associated mark scheme follows each paper.

The question papers are targeted at two tiers A* - D (Higher) and grades C - G (Foundation).

It should be noted that on both tiers candidates must not use a calculator for Paper 1.

The question papers should be read in conjunction with AQA Specification A for 2008. The specification is available on the web site www.aqa.org.uk

The question papers are intended to represent the length and balance of the papers that will be set for the examination and to indicate the types of questions that will be used. It must be emphasised, however, that the questions have not been subjected to the rigorous review that would take place with questions before use in examination.

If this document is printed from AQA's website, there is a possibility that it may not print in its original format. This will affect any questions where candidates are required to measure accurately.

Mark Schemes

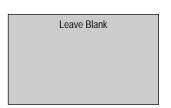
Principal Examiners have prepared these mark schemes for **specimen** papers. These mark schemes have not, therefore, been through the normal process of standardising that would take place for live papers.

Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics Specification A, Papers 1 and 2, marks are awarded under various categories.

- M Method marks are awarded for a correct method which could lead to a correct answer.
- A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
- **B** Marks awarded independent of method.
- **M dep** A method mark dependent on a previous method mark being awarded.
- ft Follow through marks. Marks awarded following a mistake in an earlier step.
- SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
- oe Or equivalent. Accept answers that are equivalent. eg accept 0.5 as well as $\frac{1}{2}$

Surname	Other Names
Centre Number	Candidate Number
Candidate Signature	



General Certificate of Secondary Education June 2008

MATHEMATICS (SPECIFICATION A) Foundation Tier Paper 1 Non-Calculator

4301/1F



Specimen Paper (Two-Tier Specification) 2008



For this paper you must have:

• mathematical instruments.





Time allowed: 1 hour 30 minutes

Instructions

- Use blue or black ink or ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- Answer the questions in the spaces provided.
- Do all rough work in this book.

Information

- The maximum mark for this paper is 100.
- The marks for questions are shown in brackets.
- You may ask for more answer paper, graph paper and tracing paper. This must be tagged securely to this answer book.

Advice

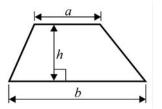
• In all calculations, show clearly how you work out your answer.

For Examiner's Use				
Pages	Mark			
3				
4 – 5				
6 – 7				
8 – 9				
10 – 11				
12 – 13				
14 – 15				
16 – 17				
18 – 19				
20 – 21				
TOTAL				
Examiner's Initials				

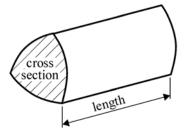
There are no questions printed on this page

Formulae Sheet: Foundation Tier

Area of trapezium = $\frac{1}{2}(a+b)h$



Volume of prism = area of cross section \times length



Answer all questions in the spaces provided.

1	The	price of a new car is £21 350.	
	(a)	Write the number 21 350 in words.	
			(1 mark)
	(b)	In the number 21 350, write down the value of the figure 5.	
		Answer	(1 mark)
	(c)	Write the number 21 350 to the nearest thousand.	
		Answer	(1 mark)
	(d)	Work out 1% of £21 350.	
		Answer £	(2 marks)
2	Woı	rk out	
	(a)	500 – 346	
		Answer	(1 mark)
	(b)	89 + 565	
			/1 1
		Answer	(1 mark)

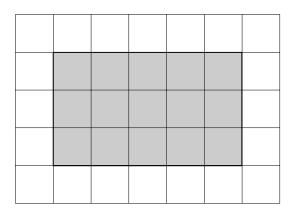
Turn over ▶

(1 mark)

Pat	tern 1 Patte	ern 2	Pattern	1 3	Patt	ern 4
(a)	Complete the table.					
	Pattern	1	2	3	4	
	Number of sticks	3	5			
(b)	Number of sticks How many sticks are					(1 mark)
(b)	How many sticks are	e there in Pat				(1 mark) (1 mark)
(b) (c)	How many sticks are	e there in Pat	etern 5?			

Answer

4 (a) A shaded rectangle is drawn on a centimetre square grid.

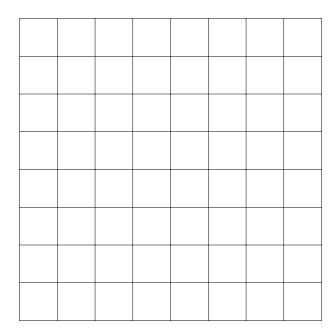


Work out the area of the shaded rectangle.

State the units of your answer.

•••••	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •

(b) On the centimetre square grid below draw a rectangle with a **perimeter** of 10 cm.

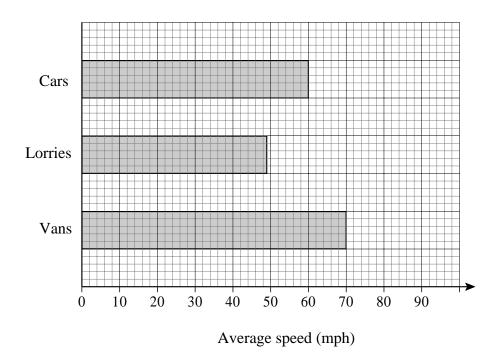


(1 mark)

7

Turn over

5 The bar chart shows the average speeds of cars, lorries and vans on a motorway.



(a) Write down the average speed of cars.

Answer mph (1 mark)

(b) Work out the difference between the average speeds of lorries and vans.

.....

Answer mph (2 marks)

(c) Andrew says that the graph shows that cars always travel faster than lorries on the motorway.

Is he correct?

Give a reason for your answer.

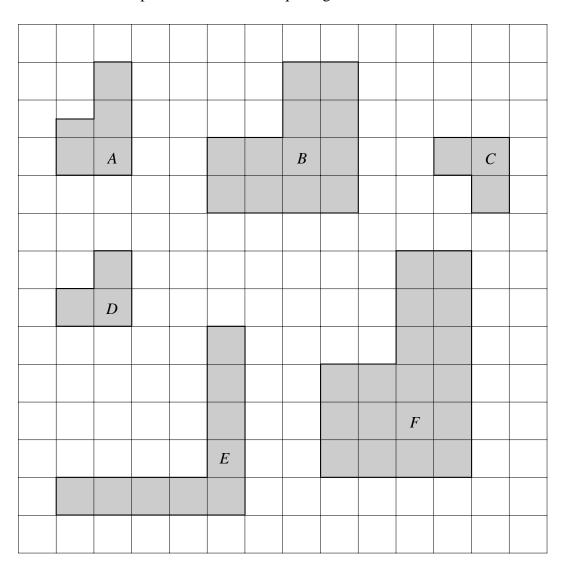
Answer

.....

(2 marks)

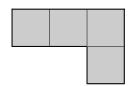
6	Here	is a list	of numb	ers.						
		4	11	12	15	17	21	25	30	
	From	this lis	t, write d	own						
	(a)	a numb	er greate	r than 15						
				Answe	r					(1 mark)
	(b)	two nu	mbers wit	th a sum						
				Answe	r					(1 mark)
	(c)	the nur	nber that	is half of	f 24					
				Answe	r					(1 mark)
	(d)	the two	factors o	of 30						
				Answe	r					(2 marks)
	(e)	a multi	ple of 7							
				Answe	r	•••••	•••••	•••••		(1 mark)
	(f)	a prime	e number							
				Answe	r					(1 mark)

7 (a) Here are six L-shapes on a centimetre square grid.

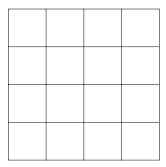


(i)	Which two L-shapes are congruent?	
	Answer and	(1 mark)
(ii)	Which L-shape is an enlargement of <i>A</i> ?	
	Answer	(1 mark)

(b) Here is a different L-shape.

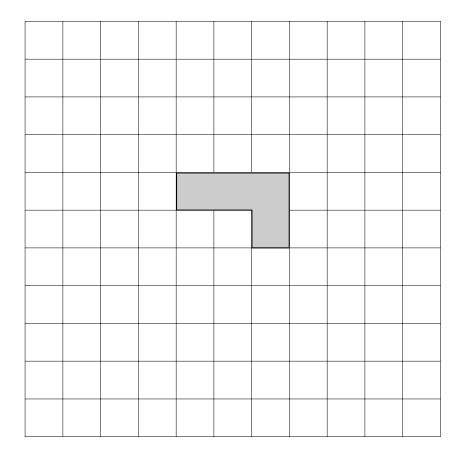


Show on the grid how four of these L-shapes can be fitted together to make a square.



(2 marks)

(c) Draw the L-shape on the centimetre square grid after a rotation of 180° .

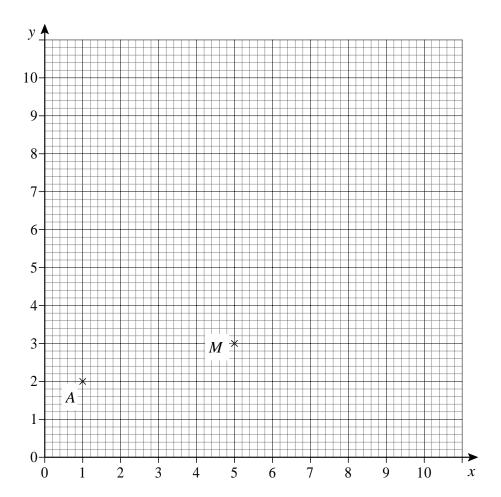


(2 marks)

6

Turn over ▶

8 The points A and M are shown on the grid.



(a) Write down the coordinates of A and M.

Answer $A (\dots, \dots)$ and $M (\dots, \dots)$ (2 marks)

(b) M is the mid-point of a line AB.

Work out the coordinates of *B*.

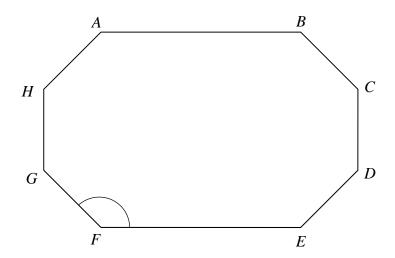
.....

.....

Answer $B(\dots, \dots)$ (2 marks)

9 (a) Work out $\frac{1}{4}$ of 12 (2 marks) (b) Work out $\frac{1}{4} + \frac{1}{8}$ (2 marks) Laura uses this method to work out 15% of 80. 10% of 80 = 8+ 5% of 80 = 4 15% of 80 = 12Use Laura's method to work out 15% of 140. Show your working. (3 marks) Answer Work out 85% of 140. (d) (2 marks) Answer

10 The diagram shows an eight-sided shape.



(a) What name is given to an eight-sided shape?

Answer (1 mark)

(b) Which line is parallel to BC?

Answer (1 mark)

(c) (i) Measure accurately the length of line AB.

Answer cm (1 mark)

(ii) Write down the length of line AB to the nearest centimetre.

Answer cm (1 mark)

(d) (i) What type of angle is angle F?

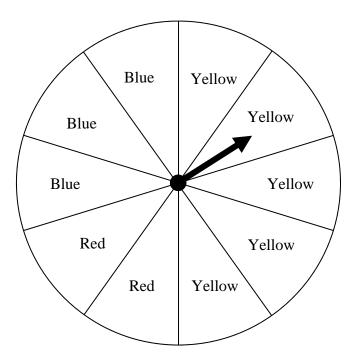
Answer (1 mark)

(ii) Measure accurately the size of angle F.

Answer degrees (1 mark)

11 A fair spinner has 10 equal sections.

Five sections are yellow, three are blue and two are red.



(a) The arrow is spun.

(i)	What is the	nrobability	of the arrow	landing on	blue
٦	-,	THE CITE OF CITE	procucinty	OI the third in	I WII WIII S OII	CIGO

(ii) What is the probability of the arrow landing on green?

.....

Answer (1 mark)

(b) The arrow is spun 100 times.

How many times do you expect the arrow to land on yellow?

11

Turn over

12	The stem and leaf	diagram shows	the number of	of books on	12 shelves	in a library
	The stelli and lear	diagram shows	the number (or cooks on	12 SHCIVES	m a morary.

 3
 1
 2
 7
 9
 9

 4
 0
 0
 2
 3

 5
 9

 6
 5

 7
 3

Key 3 1 represents 31 books

(a)	How many of the shelves have less than 40 books?	
	Answer	(1 mark)
(b)	What is the median number of books?	
(c)	Answer	(1 mark)
	Answer	(1 mark)
(d)	The mean number of books per shelf is 45.	
	Which average, mean or median, better represents the data? Give a reason for your answer.	

(1 mark)

13	(a)	Find the value of $4x - 3y$ when $x = 5$ and $y = -6$	
		Answer	
	(b)	Find the value of $\frac{x}{y}$ when $x = 30$ and $y = -2$	
		Angyor	
		Answer	(2 marks)
14	(a)	Solve $4x = 12$	
		Answer $x = \dots$	(1 mark)
	(b)	Solve $y + 7 = 11$	
		Answer $y = \dots$	(1 mark)

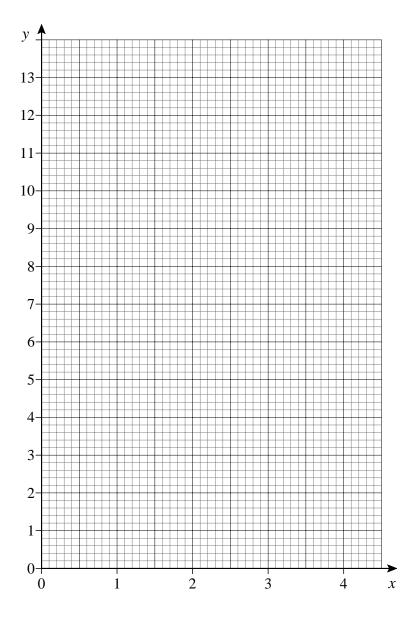
15 (a) Complete the table of values for y = 3x + 1

х	0	1	2	3	4
у	1		7		13

.....

(1 mark)

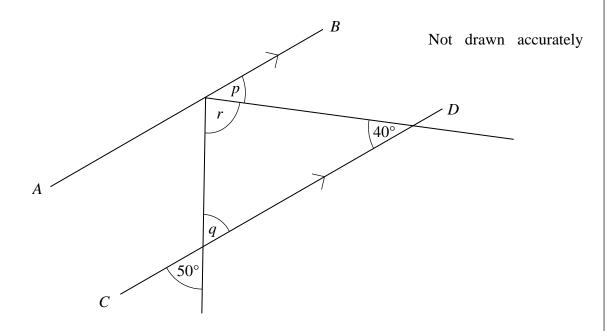
(b) On the grid draw the graph of y = 3x + 1 for values of x from 0 to 4.



(2 marks)

	(c)	Use your graph to solve $5.5 = 3x + 1$	
		Answer $x = \dots$	(2 marks)
16	(a)	Work out the value of 2^3	
		Answer	(1 mark)
	(b)	Work out $6 \times 15 + 4 \times 15$	
		Answer	(2 marks)
	(c)	Use approximations to estimate the value of $\frac{37.48 \times 6.13}{(1.95)^2}$ You must show your working.	
		Answer	(3 marks)

17 The lines AB and CD are parallel.



(a) Write down the value of *p*. Give a reason for your answer.

Answer $p = \dots degrees$

Reason

(2 marks)

(b) Write down the value of *q*. Give a reason for your answer.

Answer $q = \dots degrees$

Reason

(2 marks)

(c) Work out the value of r.

.....

Answer r = degrees (2 marks)

18	p is an even number.q is an odd number.								
	(a)	(a) Is pq an odd number, an even number or could it be either? Tick the correct box.							
		odd	O.V.O.D.	could be either					
		odd	even	could be entire	(1 mark)				
	(b) Is p a prime number, not a prime number or could it be either?Tick the correct box.								
		prime	not prime	could be either	(1 mark)				
	(c)	Is $q \div p$ an intege Tick the correct b	r, not an integer or could it be o	either?					
		integer	not on integer	aculd be either					
		integer	not an integer	could be either	(1 mark)				
	Turn over for the next question								

Turn over ▶

(2 marks)

19 500 people voted in an election.

The table shows the four candidates and the votes received by two of them.

Allgood	Betterdon	Carewell	Didright
155	105		

Carewell received twice as many votes as Didright.

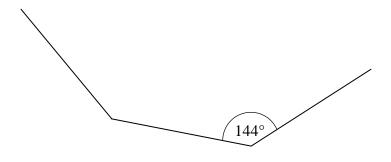
	How	w many votes did Carewell receive?	
			••••••
		Answer	(3 marks)
20	(a)	Expand $d(d^2 + 6)$	
		Answer	(2 marks)
	(b)	Simplify $g^4 \times g^4$	
		Answer	(1 mark)
	(c)	Expand and simplify $2(p+5) + 3(2p-1)$	

Answer

21 (a) On the triangular paper below, show clearly that regular hexagons will tessellate.

(2 marks)

(b) The diagram shows part of a regular polygon. Each interior angle is 144°.



Not drawn accurately

(i) Calculate the size of the exterior angle of the polygon.

.....

Answer degrees (2 marks)

(ii) Calculate the number of sides of the polygon.

.....

END OF QUESTIONS

14

4301/1F Mark Scheme

Q	Answers	Mark	Comments
1a	Twenty one thousand three hundred (and) fifty	B1	
1b	Fifty or 50	B1	Accept tens Do not accept 10
1c	21000	B1	
1d	21350 ÷ 100 or 213.5	M1	oe
Tu	(£) 213.50 (p)	A1	
2a	154	B1	
2b	654	B1	
3a	7 9	B1	
3b	11	B1	
3c	21	B1	
	5×3	M1	oe
4a	15	A1	
	cm ²	B1	Units mark
4b	Correct rectangle drawn	B1	4 × 1 3 × 2
5a	60 (mph)	B1	
5b	70 – 49 or 10 + 10 + 1	M1	allow 70 – (48 to less than 50)
	21 (mph)	A1	
	No with attempt at reason	B1	Note: No can be implied
5c	Valid reason	B1	eg only average speeds eg some cars go slower eg only looking at a sample
6a	17 or 21 or 25 or 30	B1	Ignore extras unless contradictory
6b	17 and 21	B1	
6c	12	B1	
6d	15 and 30	B2	B1 for each answer Do not allow extras
6e	21	B1	
6f	11 or 17	B1	Ignore extras unless contradictory

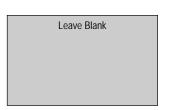
Q	Answers	Mark	Comments			
7ai	C and D	B1				
7aii	F	B1				
7b	Attempt to put 2 L shapes together without overlap	M1				
	Fully correct diagram	A1				
7c	Any rotation	M1				
70	Correct rotation	A1	in any position			
	4/1.2	D.1				
8a	A (1, 2)	B1	penalise reversed coordinates on fire occurrence only in whole question.			
	M(5,3)	B1	occurrence only in whole question.			
8b	Evidence of adding on correctly to at least one coordinate	M1	May be shown on diagram Allow M1 for (3, 2.5)			
	eg one coordinate correct (9, 4)	A1				
	$^{1}/_{4}\times12$	M1	oe			
9a	3	A1				
OI.	Common denominator seen	M1	$eg^{2}/_{8}$ and $^{1}/_{8}$ or $^{8}/_{32}$ and $^{4}/_{32}$			
9b	3/8	A1	oe Accept decimals			
	(10% of 140) = 14	M1				
9c	(5% of 140) = 7	M1	eg 16 followed by 8 scores M0M1			
	(15% of 140) = 21	A1				
9d	140 - 21 or $8 \times 14 + 7$ or $\frac{85}{100} \times 140$	M1	140 – their 21 oe			
	119	A1ft	ft only on 140 – their answer from (c)			
10a	Octagon	B1				
10b	GF	B1	Accept AE			
10ci			± 0.2 cm			
10cii	5 (cm)	B1ft	ft provided (i) not an integer			
10di	Obtuse	B1	Accept: Interior			
10dii	135	B1	± 2°			
			1			

Q	Answers	Mark	Comments
11ai	$0.3 \text{ or } ^3/_{10}$	B2	B1 for 3 in numerator or 10 in denominator eg 3 in 10 penalise 1 mark on first occasion
11aii	0	B1	Accept: Impossible, Zero, Nought, $\operatorname{Nil}, {}^0/_{10}$
	$^{1}/_{2} \times 100$	M1	50% scores M1A0
11b	50	A1	Accept $^{50}/_{100}$ Do not ignore cancelling down eg $^{50}/_{100} = ^{1}/_{2}$ scores M1 only
- 10	T -	D1	
12a	5	B1	
12b	40	B1 B1	
12c 12d	12c 42 median, mean affected by extreme		must give a reason; median can be
	values		implied
13a	$4 \times 5 (-) 3 \times -6$ or 20 (-) -18 or 20 + 18	M1	2 implies M1A0
	30/_2	M1	oe
13b	-15	A1	not eg $^{-15}/_1$
140	2	D1	
14a	3	B1	
14b	4	B1	
15a	4 10	B1	
	At least 2 correct points plotted	M1	May be implied by a correct line
15b	Correct ruled line drawn	A1	Tolerance 1 square from points
	Attempt to read off at $y = 5.5$	M1	Tolerance $\pm \frac{1}{2}$ square
15c	1.5	A1ft	Use of graph not essential ft is from their line

Q	Answers	Mark	Comments
16a	8	B1	
16b	10×15 or $90 + 60$ or their $90 +$ their 60	M1	with attempt at multiplication seen
	150	A1	
	Sight of two from 40, 6 and 2	M1	Allow 36, 37, 38
16c	<u>240</u> 4	M1dep	oe or <u>6 x (their 36, 37 or 38)</u> 4
	60	A1	54, 55.5, 57
	40	B1	
17a	Alternate	B1	Do not accept: Z angle Accept: Corresponding angle if corresponding angle seen. Accept: Allied or interior if angle seen
	50	B1	
17b	Opposite	B1	Accept: Vertically opposite Straight line (= 180) if 130 seen
17c	180 - 40 - 50 or $180 - 40$ – their q	M1	oe
	90	A1ft	
18a	Even	B1	
18b	Could be either	B1	
18c	Not an integer	B1	
	500 – 155 – 105 or 240	M1	
19	their 240 ÷ 3 (× 2)	M1dep	oe
	160	A1	

Q	Answers	Mark	Comments
20a	$d^3 + 6d$	B2	B1 for each term Do not accept d6
20b	g ⁸	B1	
	2p + 10 + 6p - 3	M1	For 3 correct terms
20c	8p + 7	A1	SC1 for $8p + n$ or $np + 7$ provided consistent with any working shown
	any regular hexagon	B1	
21a	any three regular hexagons meeting at a point	B1	
21bi	180 – 144	M1	
2101	36	A1	
21bii	360 ÷ 36 or 360 ÷ their 36	M1	
	10	A1	

Surname			Other Names							
Centre Number						Candi	date Number			
Candidate Signature										



General Certificate of Secondary Education June 2008

MATHEMATICS (SPECIFICATION A) Higher Tier Paper 1 Non-Calculator

4301/1H



Specimen Paper (Two-Tier Specification) 2008



For this paper you must have:

• mathematical instruments.





Time allowed: 2 hours

Instructions

- Use blue or black ink or ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- Answer the questions in the spaces provided.
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- The maximum mark for this paper is 100.
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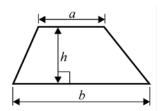
Advice

• In all calculations, show clearly how you work out your answer.

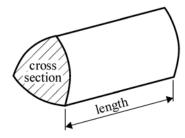
For Examiner's Use					
Pages	Mark				
3					
4 – 5					
6 – 7					
8 – 9					
10 – 11					
12 – 13					
14 – 15					
16 – 17					
18 – 19					
20 – 21					
22 – 23					
TOTAL					
Examiner's Initials					

Formulae Sheet: Higher Tier

Area of trapezium =
$$\frac{1}{2}(a+b)h$$

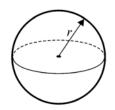


Volume of prism = area of cross section \times length



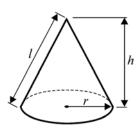
Volume of sphere
$$=\frac{4}{3}\pi r^3$$

Surface area of sphere = $4\pi r^2$



Volume of cone =
$$\frac{1}{3}\pi r^2 h$$

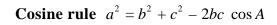
Curved surface area of cone = $\pi r l$

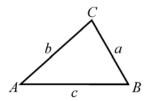


In any triangle ABC

Area of triangle =
$$\frac{1}{2} ab \sin C$$

Sine rule
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$





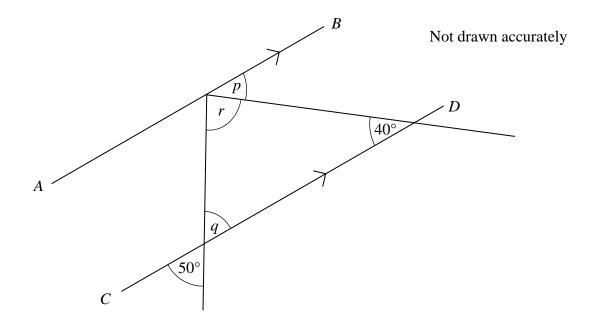
The Quadratic Equation

The solutions of $ax^2 + bx + c = 0$, where $a \ne 0$, are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

Answer all questions in the spaces provided.

1 The lines AB and CD are parallel.



(a) Write down the value of *p*. Give a reason for your answer.

Answer $p = \dots degrees$

Reason

(2 marks)

(b) Write down the value of *q*. Give a reason for your answer.

Answer $q = \dots degrees$

Reason

(2 marks)

(c) Work out the value of r.

Answer r = degrees (2 marks)

6

Turn over ▶

2	Solve the equation $3(z-2) = 27$
	Answer $z = \dots (3 \text{ marks})$
3	Which of these fractions is closest to $\frac{1}{4}$?
	You must show your working.
	$\frac{2}{5}$ $\frac{3}{10}$ $\frac{7}{20}$ $\frac{13}{40}$
	(3 marks)
	(=)

(a)	Tick the correct bo	er, an even number or could ox.	it de either?	
	odd	even	could be either	(1 mark
(b)	Is p a prime number Tick the correct be	er, not a prime number or coox.	ould it be either?	
	prime	not prime	could be either	(1 mank
(c)	Is $a \div p$ an integer	, not an integer or could it b	e either?	(1 mark)
(c)	Is $q \div p$ an integer. Tick the correct be	, not an integer or could it box.	e either?	(1 mark
(c)	Tick the correct bo	OX.		(1 mark)
(c)	Is $q \div p$ an integer. Tick the correct be integer	not an integer or could it box. not an integer	could be either	(1 mark)
(c)	Tick the correct bo	OX.		
(c)	Tick the correct bo	OX.	could be either	
(c)	Tick the correct bo	not an integer	could be either	

Turn over ▶

5 500 people voted in an election.

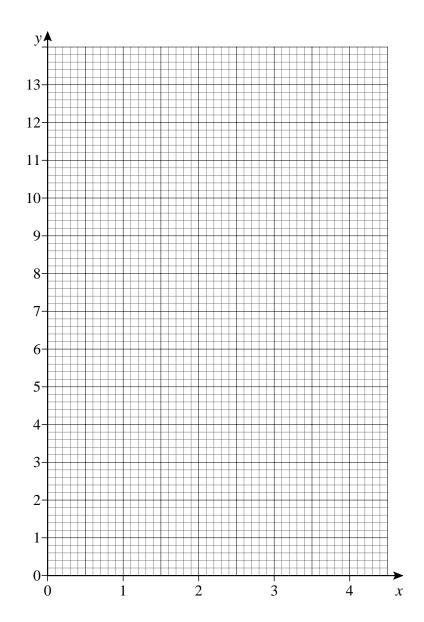
The table shows the four candidates and the votes received by two of them.

Allgood	Betterdon	Carewell	Didright
155	105		

(a)	What percentage of the votes did Allgood receive?	
		••••••
	Answer %	(2 marks)
(b)	Carewell received twice as many votes as Didright.	
	How many votes did Carewell receive?	
	Answer	(3 marks)

6 (a) On the grid draw the graph of y = 3x + 1 for values of x from 0 to 4.

.....



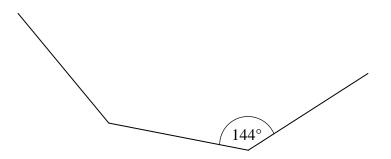
(3 marks)

(b) Use your graph to solve 5.5 = 3x + 1

.....

Answer $x = \dots (2 marks)$

7 The diagram shows part of a regular polygon. Each interior angle is 144°.



Not drawn accurately

(3 marks)

Calculate the size of the exterior angle of the polygon.			
Answer			
Use approximations to estimate the value of You must show your working.	$\frac{37.48 \times 6.13}{(1.95)^2}$		

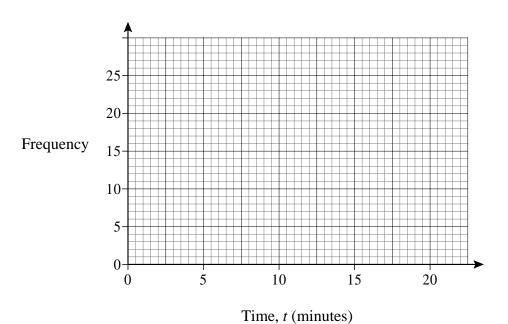
9 50 people were asked how long they had to wait for a bus. The table shows the results.

Time, t (minutes)	Frequency	Mid-point	
$0 < t \leqslant 5$	16		
5 < <i>t</i> ≤ 10	21		
10 < t ≤ 15	10		
$15 < t \leqslant 20$	3		

(a) Calculate an estimate of the average time they had to wait.

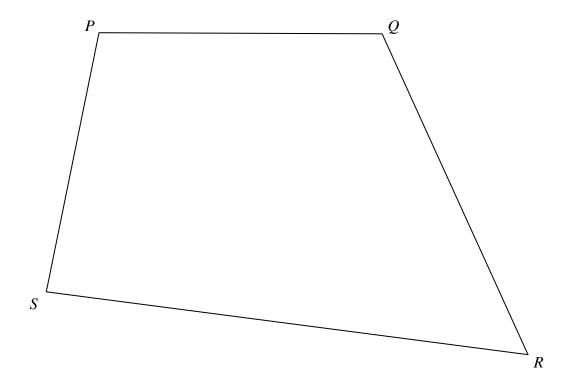
Answer minutes (3 marks)

(b) Draw a frequency diagram to represent the data.



(2 marks)

10 The diagram shows a quadrilateral *PQRS*.



(a) Draw the locus of points that are the same distance from P as from Q.

(2 marks)

(b) Shade the region inside the quadrilateral which is less than $7 \, \text{cm}$ from S and nearer to Q than to P.

(2 marks)

11 A sequence of numbers is shown.

5 9 13 17 21

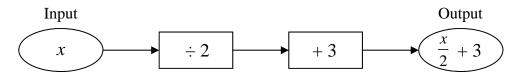
(a) Find an expression for the nth term of the sequence.

(b) Explain why 83 will not be a term in this sequence.

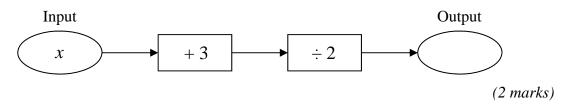


(2 marks)

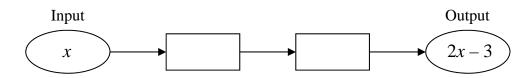
12 A function diagram produce algebraic expressions. For example



(a) Fill in the missing expression in this function diagram.

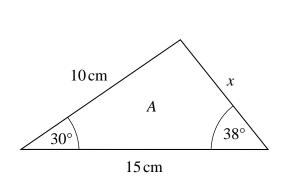


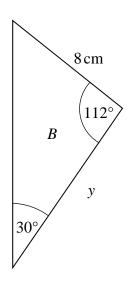
(b) Fill in the missing operations in this function diagram.



(2 marks)

13 The triangles *A* and *B* are congruent.





Not drawn accurately

(a) Write down the values of x and y.

Answer x = cm , y = cm (2 marks)

(b) Given that $\sin 30^{\circ} = 0.5$, calculate the area of triangle A. State the units of your answer.

.....

.....

14	(a)	x is	an integer.	
		List	all the values of x such that $-1 < 2x \le 8$	
		•••••		
		•••••		•••••••••••
			Answer	(3 marks)
	(b)	(i)	Factorise $y^2 - 8y + 15$	
				•••••
			Answer	(2 marks)
		(ii)	Hence solve the equation $y^2 - 8y + 15 = 0$	
			Answer	(1 mark)

Turn over for the next question

15 Emma has a box of counters.

The counters are green, red or blue.

She picks a counter at random.

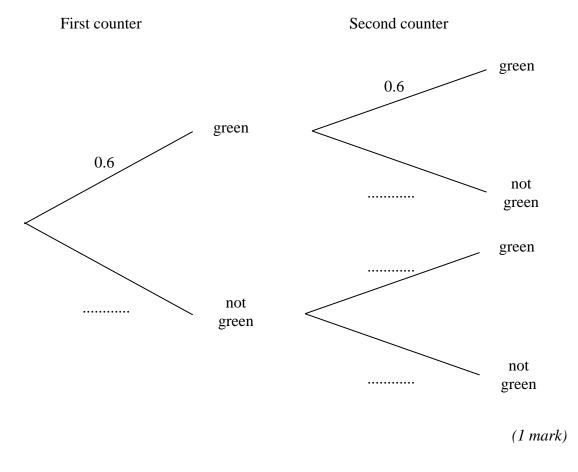
The table shows the probability that she picks a green counter and the probability that she picks a red counter.

Colour	Probability
Green	0.6
Red	0.25
Blue	

(a)	What is the probability that Emma picks a blue counter?			
	Answer	(2 marks)		
(b)	There are 10 red counters in the box.			
	How many green counters are in the box?			
	Answer	(3 marks)		

- (c) Emma picks a counter at random.

 She replaces it in the box and then picks another counter at random.
 - (i) Complete the tree diagram.



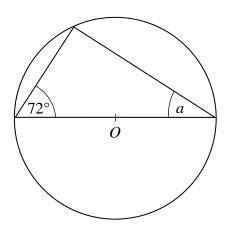
(ii) What is the probability that at least one of the counters is green?

Answer (3 marks)

9

Turn over

16 (a) O is the centre of the circle.



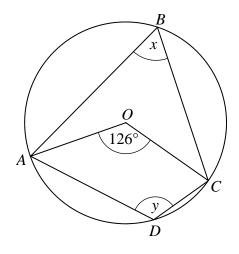
Not drawn accurately

Calculate the value of *a*.

.....

Answer degrees (2 marks)

(b) O is the centre of the circle. A, B, C and D are points on the circumference. Angle $AOC = 126^{\circ}$



Not drawn accurately

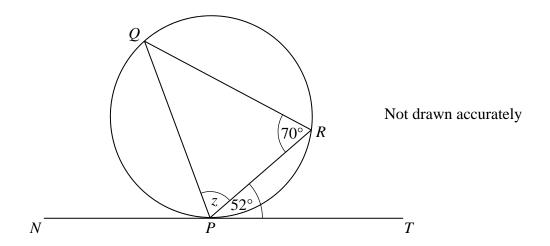
(i) Calculate the value of x.

Answer degrees (1 mark)

(ii) Calculate the value of y.

Answer degrees (1 mark)

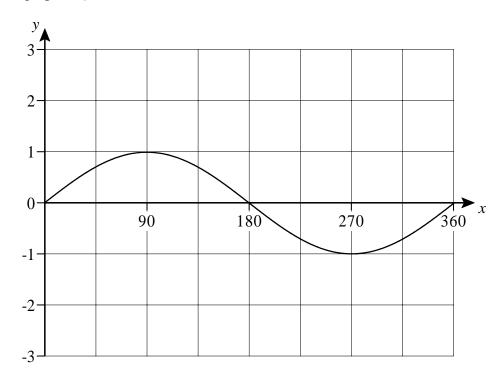
(c) P, Q, and R are points on the circumference of the circle. NPT is the tangent to the circle at P.



Calculate the value of z . Give a reason for each step	of your working.	
•	o or your working.	

Turn over for the next question

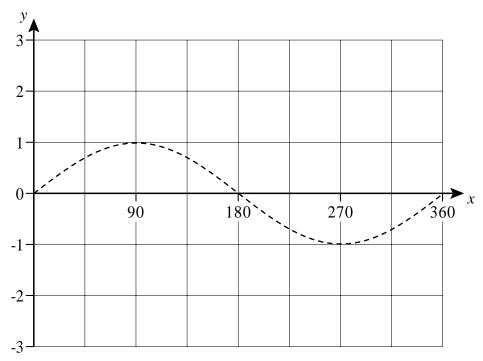
17 This is the graph of $y = \sin x$ for $0^{\circ} \leqslant x \leqslant 360^{\circ}$



Draw the graphs indicated for $0^{\circ} \leqslant x \leqslant 360^{\circ}$

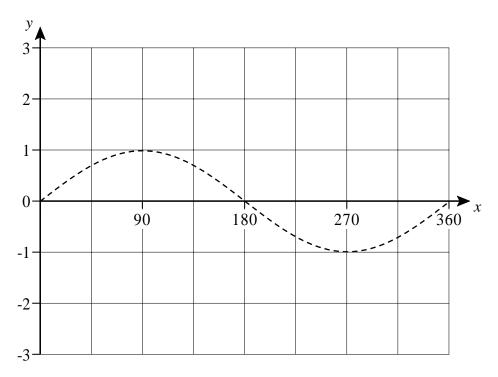
In each case the graph of $y = \sin x$ is shown to help you.

(a) $y = 2\sin x$



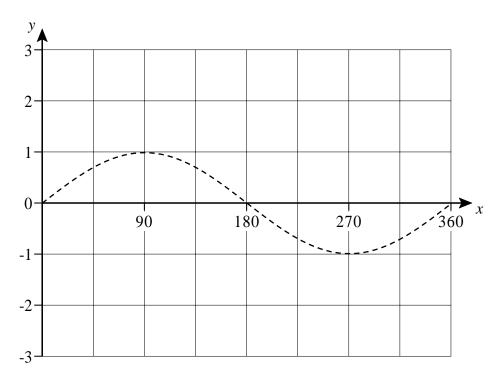
(1 mark)

(b) $y = -\sin x$



(1 mark)

(c) $y = \sin 2x$

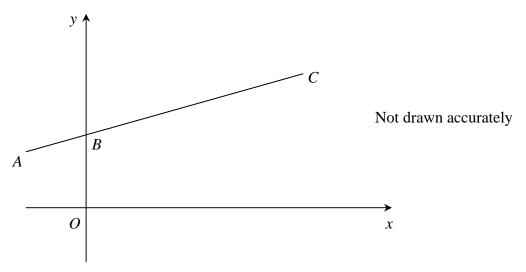


(1 mark)

Turn over

(3 marks)

18 The diagram shows the points A(-2, 2), B(0, 3) and C(8, 7).



Find the equation of the straight line which passes through A, B and C.

Answer $y = \dots$

19 (a) Find the value of $36^{\frac{1}{2}}$

Answer (1 mark)

(b) Simplify $2^{-2} \times 81^{\frac{1}{4}}$

Answer (3 marks)

20	(a)	Simplify
		(i) $\sqrt{3} + \sqrt{3}$
		Answer (1 mark)
		(ii) $\sqrt{3} \times \sqrt{3}$
		Answer (1 mark)
	(b)	Show that $\frac{\sqrt{75} - \sqrt{12}}{\sqrt{75} + \sqrt{12}}$ simplifies to $\frac{3}{7}$

Turn over for the next question

(3 marks)

(7 *marks*)

21 Solve the simultaneous equations

$$y = 2x + 3$$

$$x^2 + y^2 = 2$$

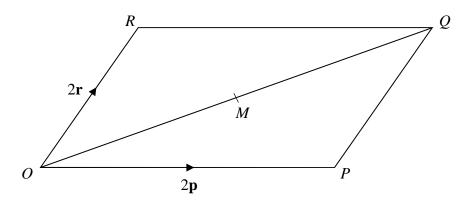
You **must** show your working.

Do **not** use trial and improvement.

1	

22 OPQR is a parallelogram.M is the mid-point of the diagonal OQ.

 $\overrightarrow{OP} = 2\mathbf{p} \text{ and } \overrightarrow{OR} = 2\mathbf{r}$



(a) Express OM in terms of **p** and **r**.

.....

Answer $\overrightarrow{OM} = \dots$ (1 mark)

(b) Use vectors to prove that M is also the mid-point of PR.

(3 marks)

END OF QUESTIONS

4301/1H Mark Scheme

Q	Answers	Mark	Comments
	40	B1	
1a	Alternate	B1	Do not accept: Z angle Accept: Corresponding angle if corresponding angle seen. Accept: Allied or interior if angle seen
11.	50	B1	
1b	Opposite	B1	Accept: Vertically opposite Straight line (= 180) if 130 seen
1c	180 - 40 - 50 or $180 - 40$ – their q	M1	oe
	90	A1ft	
	3z - 6 = 27	M1	or $z - 2 = 9$
2	3z = 27 + 6	M1	or $z = 9 + 2$
	11	A1	
	Attempt to find common denominator	M1	eg 16/40, 12/40, 14/40, 13/40
3	Any correct conversion	A1	
	3/10	A1	oe
4a	Even	B1	
4b	Could be either	B1	
4c	Not an integer	B1	
		<u> </u>	1
5a	155/500 × 100	M1	or 155 ÷ 5
5a	31	A1	31 / ₁₀₀ scores M1A0
6 1	500 – 155 – 105 or 240	M1	
5 b	their 240 ÷ 3 (× 2)	M1dep	oe
	160	A1	

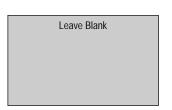
Q	Answers	Mark	Comments
	any 2 pts calculated from (0, 1) (1, 4) (2, 7) (3, 10) (4, 13)	M1	May be implied from a correct line
6a	at least 2 of these correct pts plotted	M1	
	Correct ruled line drawn from (0, 1) to (4,13)	A1	Tolerance 1 square from points
	Attempt to read off at $y = 5.5$	M1	Tolerance $\pm \frac{1}{2}$ square
6b	1.5	A1ft	Use of graph not essential, but then mark will be 2 or 0 ft is from their line
	180 – 144	M1	
7	36	A1	
	30	711	
	Sight of two from 40, 6 and 2	M1	Allow 36, 37, 38
8	240 4	M1dep	oe or <u>6 x (their 36, 37 or 38)</u>
	60	A1	54, 55.5, 57
	correct midpoints 2.5, 7.5, 12.5 and 17.5	B1	
9a	$\sum mf = 375$	M1	40,157.5, 125, 52.5 allow 1 error
	mean = 7.5	A1	
9b	correct polygon or histogram	B2	-1 eeoo eg curve or incorrect point if all plots consistently at r.h. edge of the intervals, award SC1
10a	Line through mid-point of PQ	B1	± 2mm 2 pairs of arcs but no line: SC1
	Perpendicular to PQ	B1	± 2°
10b	Arc of radius 7cm, centre <i>S</i> , at least from <i>SR</i> to their p.b.	M1	± 2mm
100	Area shaded	A1	Arc attempted (well) without use of compass + correct area shaded: SC1

Q	Answers	Mark	Comments
11a	4n + 1	B2	oe Accept $n \times 4 + 1$ $4 \times n + 1$ B1 for any of these: $n4 + 1$ $4n \pm c$ with $c \neq 0$
	81 or 85 seen	B1	
11b	$T_{20} = 81$, next term is 85	B1	oe <u>alternative</u> $4n + 1 = 83$ B1 82 not divisible by 4 (oe) B1 SC1 for: $4n \pm c = 83 \Rightarrow n$ not a whole number or T_{20} and T_{21} from their $4n \pm c$
	$(x+3) \div 2 \text{ or } \frac{x+3}{2}$	B2	B1 for $x+3$ or $\frac{x}{2}+3$
12	×2	B1	
	-3	B1	sc B1 for -3 and ×2
	x = 8	B1	
13a	y = 10	B1	
	$^{1}/_{2}$ x 10 x 15 x 0.5	M1	oe
13b	37.5	A1	
	cm ²	B1	Units mark
1.4	$-\frac{1}{2} < x \le 4$	M1	may not be seen
14a	0, 1, 2, 3, 4	A2	-1 eeoo
14bi	$(y \pm a)(y \pm b)$ where $ab = 15$	M1	
	(y-3)(y-5)	A1	
14bii	(+) 3 and (+) 5	B1	ft from b(i) if M awarded

Q	Answers	Mark	Comments
	1-0.6-0.25	M1	0.69 implies M1 if 0.31 seen
15a	0.15	A1	
	10 ÷ 0.25	M1	oe or 40 seen
15b	their 40 x 0.6	M1dep	
	24	A1	
15ci	0.6 on all "up" branches 0.4 on all "down" branches	B1	
	0.6 x 0.6 or 0.6 x 0.4 or 0.4 x 0.6	M1	one correct product seen (could be on tree diagram)
	addition of 2 or more of these	M1dep	
15cii	0.84	A1	Alternative method 0.4 x 0.4 M1 1 – their 0.16 M1dep 0.84 A1
	100 00 70	N/1	1
16a	180 – 90 – 72	M1	oe
16bi	63	A1 B1	
16bii	117	B1	or 180 – their 63 correctly evaluated
	52 at Q	M1	(do not allow 90) or angle NPQ = 70 may be credited from diagram
16c	(angles in) alternate segment	B1	
	58	A1	58 as answer scores M1A1
17a	curve through (0,0) (90,2) (180,0) (270,-2) (360,0)	B1	
17b	curve through (0,0) (90,-1) (180,0) (270,1) (360,0)	B1	
17c	curve through (0,0) (45,1) (90,0) (135,-1) (180,0) (225,1) (270,0) (315,-1) (360,0)	B1	

Q	Answers	Mark	Comments
	Attempt at $\frac{7-2}{82}$	M1	or $\frac{7-3}{8-0}$ or $\frac{3-2}{02}$
18	$(\text{their}^{1}/_{2}) x + c$	M1	their $1/2$ must come from an attempt at a gradient
	$\frac{1}{2}x + 3$	A1	
19a	(±)6	B1	
174	1/4		on 0.25
101		B1	or 0.25
19b	3	B1	
	3/4	B1	
20ai	2√3	B1	
20aii	3	B1	
	5√3 seen	M1	or $2\sqrt{3}$
20b	$(5\sqrt{3}-2\sqrt{3}=)\ 3\sqrt{3}$	M1	$(5\sqrt{3} + 2\sqrt{3} =) 7\sqrt{3}$
	Cancelling $\sqrt{3}$ to get $^3/_7$	A1	
	$x^2 + (2x+3)^2 = 2$	M1	
	$4x^2 + 6x + 6x + 9$	M1	condone one error
	$5x^2 + 12x + 7 = 0$	A1	oe
21	(x+a)(5x+b)=0	M1	ab = 7 or by the formula
	(x+1)(5x+7) = 0	A1	
	$x = -1 \text{ or } -\frac{7}{5}$	A1	Alternative (-1, 1) A1
	$y = 1 \text{ or } \frac{1}{5}$	A1	(-7/5, 1/5) A1
22a	p + r	B1	
	$PM = -2\mathbf{p} + \mathbf{p} + \mathbf{r}$	M1	or $MR = -(\mathbf{p} + \mathbf{r}) + 2\mathbf{r}$ or $PR = -2\mathbf{p} + 2\mathbf{r}$
22b	$PM = -\mathbf{p} + \mathbf{r}$	A1	or $MR = -\mathbf{p} + \mathbf{r}$
	PR = 2PM so M is mid-point	A1	

Surname			Other I	Names			
Centre Number				Candi	date Number		
Candidate Signature							



General Certificate of Secondary Education June 2008

MATHEMATICS (SPECIFICATION A) Foundation Tier Paper 2 Calculator

4301/2F



Specimen Paper (Two-Tier Specification) 2008



For this paper you must have:

- a calculator
- mathematical instruments.



Time allowed: 1 hour 30 minutes

Instructions

- Use blue or black ink or ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Answer the questions in the spaces provided.
- Use a calculator where appropriate.
- Do all rough work in this book.
- If your calculator does not have a π button, take the value of π to be 3.14 unless another value is given in the question.

Information

- The maximum mark for this paper is 100.
- The marks for questions are shown in brackets.
- You may ask for more answer paper, graph paper and tracing paper. This must be tagged securely to this answer book.

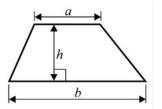
Advice

• In all calculations, show clearly how you work out your answer.

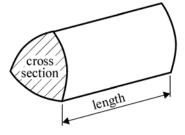
For Exam	For Examiner's Use					
Pages		Mark				
3						
4 – 5						
6 – 7						
8 – 9						
10 – 11						
12 – 13						
14 – 15						
16 – 17						
18 – 19						
20 – 21						
22 – 23						
24 – 25						
26						
TOTAL						
Examiner's Initials						

Formulae Sheet: Foundation Tier

Area of trapezium = $\frac{1}{2}(a+b)h$



Volume of prism = area of cross section \times length



Answer all questions in the spaces provided.

1 (a) Complete the shopping bill.

		£	p
Onions	4 kg at £0.79 per kg		
Apples	3 kg at £1.96 per kg		
Lemonade	5 bottles at £0.85 per bottle		
	Total		

(4 marks)

(b)	Adam buys 9 pens at 57 pence each.
	He pays with a f 10 note

How much change does he receive?

2 (a) Write $\frac{1}{2}$ as a percentage.

(b) Write 25% as a fraction.

Answer (1 mark)

8

Turn over ▶

3 (a) Which **two** of these fractions are equivalent to $\frac{1}{3}$?

 $\frac{2}{6}$ $\frac{5}{12}$ $\frac{6}{18}$ $\frac{11}{30}$

.....

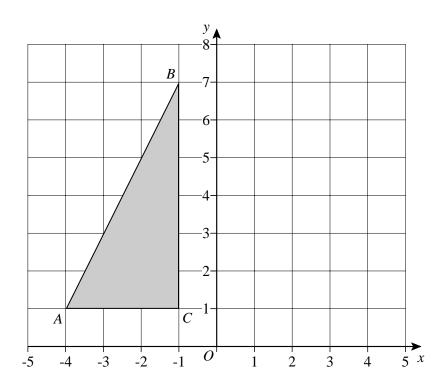
(b) Write 70% as a decimal.

Answer (1 mark)

(c) Write $\frac{3}{10}$ as a decimal.

Answer (1 mark)

4 The diagram shows a triangle drawn on a centimetre square grid.



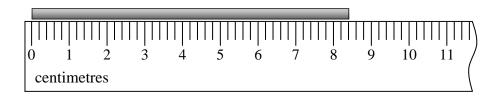
(a) Write down the coordinates of A.

Answer $A (\dots, \dots, \dots)$ (1 mark)

(b) Draw the reflection of the triangle in the y-axis.

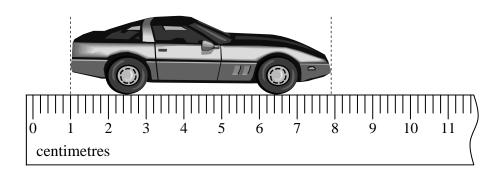
(2 marks)

5 (a) Write down the length of this stick.



Answer cm (1 mark)

(b) Tom has a toy car.



Turn over for the next question

6	(a)	Write dow	n the	next tw	o numb	ers in thi	s sequence	
		3	9	15	21		•••••	
								(2 marks)
	(b)	Another se	equen	ce of nu	mbers l	begins		
		4	5	7				
		The rule f	or con	tinuing	the seq	uence is		
						Mult	iply by 2	
						1	hen	
						Sub	otract 3	
		What are						
			•••••					
				Answ	er		,	 (2 marks)

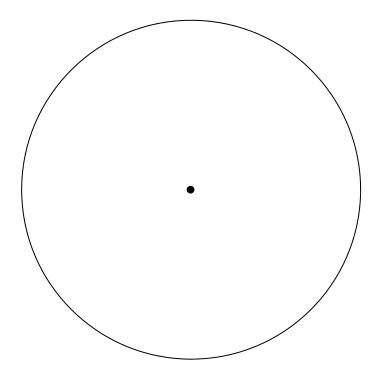
Answer,

7 (a) A circle has a radius of 4 cm.

Write down the length of the diameter.

Answer cm (1 mark)

- (b) On the circle below
 - (i) draw a diameter
 - (ii) mark with a cross a point on the circumference
 - (iii) draw a tangent

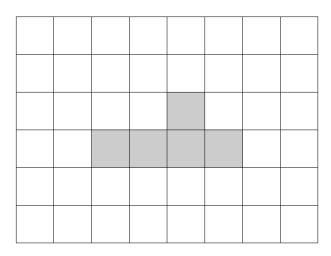


(3 marks)

8

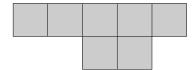
Turn over ▶

8 (a) (i) Shade one more square so that the shaded shape is a net of a cube.

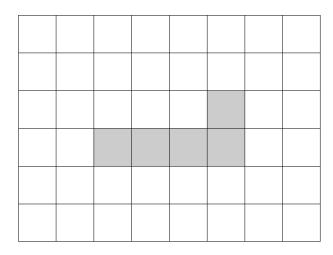


(1 mark)

(ii) Explain why this shape is **not** the net of a cube.

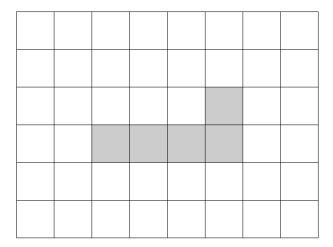


(b) (i) Shade one more square so that the shaded shape has one line of symmetry.



(1 mark)

(ii) Shade one more square so that the shaded shape has rotational symmetry of order 2.



(1 mark)

4

Turn over ▶

9 A table has four columns A, B, C and D. Part of the table is shown.

A	В	С	D
1	6	94	36
2		93	49
4	9		
7			144

(a) This is the 2nd row of the table.

\boldsymbol{A}	В	C	D
2		93	49

The number in column B = The number in column A + 5

Work out the number in column B in this row.					
		(1 mark)			

TS/SP08/4301/2F

ĺ	(b)) This	is	the	3rd	row	of	the	table	
١	U,	, 11115	10	uic	JIU	10 W	OI	uic	table	•

A	В	С	D
4	9		

-	٠	`
- 1	1	١
١.	1	J

The number in column C = 100 – The number in column B

•••••	••••••	•••••	•••••	•••••

Answer (1 mark)

(ii)

The number in column D = The number in column B squared

Work out the number in column *D* in this row.

Work out the number in column *C* in this row.

.....

Answer (1 mark)

(c) This is the 4th row of the table.

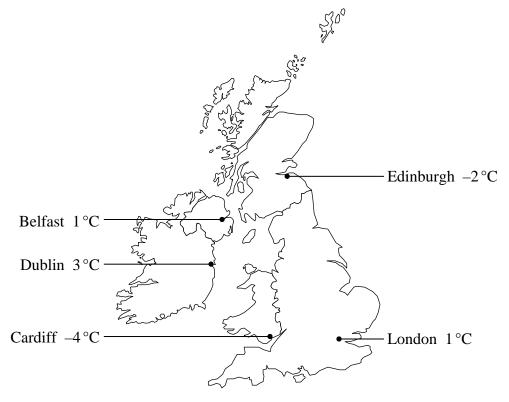
\boldsymbol{A}	В	C	D
7			144

Work out the number in column *C* in this row.

5

Turn over ▶

10 The map shows the temperatures at sunset in five cities in the British Isles.



(a) In which city is the temperature the lowest?

Answer	(1	l mark,)
--------	----	---------	---

(b) How much higher is the temperature in Dublin than the temperature in Edinburgh?

Answer°C (1 mark)

(c) The temperature in Cardiff at midday is 10 °C higher than it is at sunset.

What is the temperature at midday in Cardiff?

Answer°C (1 mark)

(d) The temperature in Edinburgh at midnight is 3 °C **lower** than it is at sunset.

What is the temperature at midnight in Edinburgh?

.....

Answer°C (1 mark)

11	(a)	(i)	Simplify	2n + 3p - n + 7p			
				Answer	(2 marks)		
		(ii)	Simplify	$2n \times 5n$			
				Answer	(1 mark)		
	(b)	Afza	Afzal scored x marks in a test.				
		(i)	Ben scored	13 more marks than Afzal.			
			Write an ex	xpression for Ben's score in terms of x .			
				Answer	(1 mark)		
		(ii)	Jason score	ed half of Afzal's marks.			
			Write an ex	xpression for Jason's score in terms of x .			
				Answer	(1 mark)		

Turn over for the next question

2 (a)			etty take a scores are		al arithmet	tic tes	st each we	ek for	seven we	eks.
			8	9	8	9	9	7	6	
	(i)	What i	s the mode	e of A	dam's scor	es?				
			Ansv	wer						(1 mark)
	(ii)	What i	s the medi	an of	Adam's sc	ores?				
			Ansv	wer						(2 marks)
(b)	Bett	y's test s	scores are							
			3	6	7	8	8	4	6	
	Con	plete th	is table.							
					Range		Mean			
			Adam	1	3		8			
			Betty		5					
		•••••				••••••		•••••	••••••	
		••••••		• • • • • • • • • • • • • • • • • • • •		•••••		•••••	••••••	
	•••••	•••••	•••••		•••••••••••	••••••	••••••	••••••	•••••	•••••

	(c)	Use the range and mean to compare their test scores.
		(2 marks)
13	Here	are four number cards.
		3 6 4 7
	(a)	Use all four cards to make the largest possible odd number.
		Answer (1 mark)
	(b)	Use two of the cards to make the number that is closest to the following numbers. The first one has been done for you.
		$egin{pmatrix} 6 \ \hline \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
		(i) \longrightarrow 3 0 (1 mark)
		(ii)

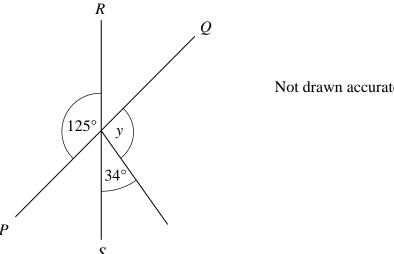
Turn over ▶

14 A bag contains only red, blue and white counters. The table shows the probability of taking a red or blue counter from the bag at random.

Colour	Red	Blue	White
Probability	0.25	0.3	

Work out the probability of taking	g a white counter from the bag.	
Answer		(2 marks)

PQ and RS are straight lines.



Not drawn accurately

Work out the value of y.

Answer $y = \dots$ degrees (3 marks) **16** (a)

Zoo Admission Prices

£14.00 Adults Children £10.75

Answer £	
Zoo Admission Prices	
For groups of more than 10	
Adults £11.20 Children £8.60	
One adult goes free for every 10 children	
total cost is £265.80 e are 27 children in the group.	
t	Zoo Admission Prices For groups of more than 10 Adults £11.20 Children £8.60

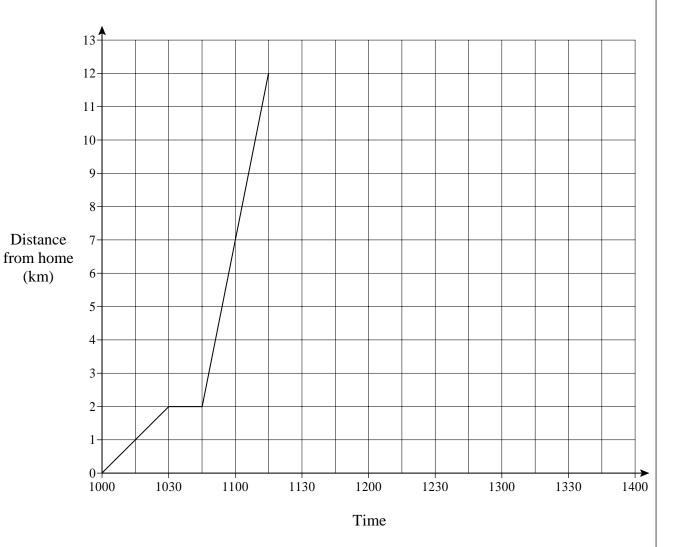
Turn over ▶

17 Mr Smith leaves home at 10 am to go to the shopping mall.

He walks to the station where he catches a train.

He gets off at the mall.

The travel graph shows his journey.



(a) How far is Mr Smith from home at 11 am?

Answer km (1 mark)

(b) After shopping Mr Smith goes home by taxi.

The taxi leaves the mall at 1 pm and arrives at his home at 1.45 pm.

Complete the travel graph.

(2 marks)

18 Use your calculator to work out $\frac{95.4+18.9}{35.2-17.3}$

(a) Write down your full calculator display.

Answer (1 mark)

(b) Give your answer to 2 significant figures.

Answer (1 mark)

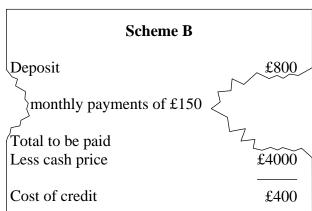
Turn over for the next question

19 A car dealer is offering two different schemes to buy a car. Some parts of Scheme B are missing.



CASH PRICE £4000

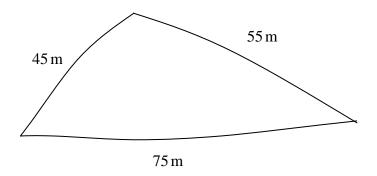
Scheme A				
Deposit	£1200			
12 monthly payments of £250	£3000			
Total to be paid Less cash price	£4200 £4000			
Cost of credit	£200			



(a)	Work out the total to be paid using Scheme B.				
	Answer £	(1 mark)			
(b)	Work out the number of monthly payments using Scheme B.				
	Answer	(2 marks)			

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20 The diagram shows a rough sketch of a triangular field.



(a) Using ruler and compasses only, make an accurate scale drawing of the field. Use a scale of 1 cm to represent 10 m.

You **must** show clearly all your construction arcs.

(3 marks)

(b) The length of one side of the field is 75 metres. This length is measured to the nearest metre.

What is the smallest possible length of this side.

Answer m (1 mark)

7

Turn over ▶

21 (a) Expand 3(x+2)

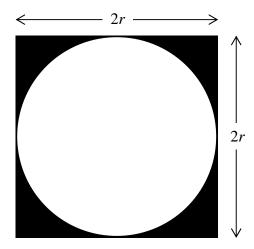
.....

Answer (1 mark)

(b) Factorise 6a - 10

Answer (1 mark)

(c) A star shape is made by cutting quadrants of a circle from a square of side 2r.



Show that the shaded area is given by the formula

$$A = 4r^2 - \pi r^2$$

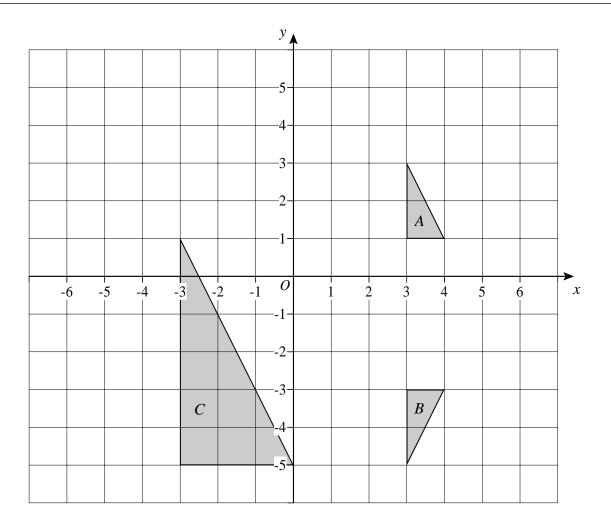
.....

.....

.....

(2 marks)

22



(a)	Describe the transformation that maps triangle A to triangle B.					
	(2 marks)					

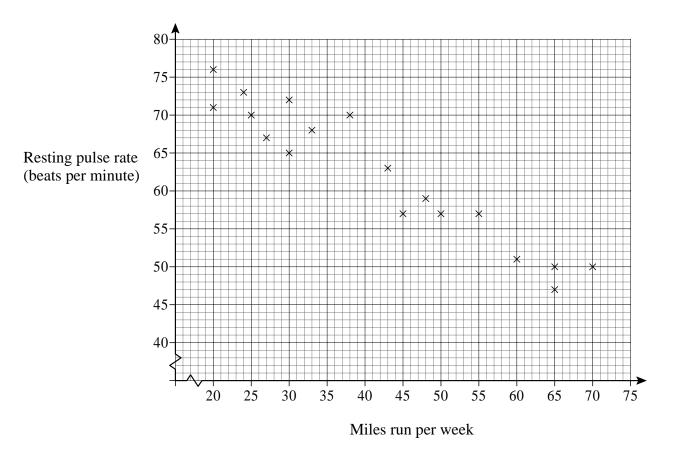
- (b) Triangle C is an enlargement of triangle A.
 - $\label{eq:write_down} \text{(i)} \quad \text{Write down the scale factor of the enlargement.}$

Answer (1 mark)

(ii) Write down the coordinates of the centre of the enlargement.

Answer (.....) (1 mark)

23 Some runners recorded their resting pulse rates and miles run per week. The scatter graph shows the results.



(a) How many runners have a resting pulse rate of 57 beats per minute?

Answer (1 mark)

(b) Draw a line of best fit.

(1 mark)

(c) Predict the resting pulse rate of a runner who runs 40 miles per week.

Answer beats per minute (1 mark)

(d) Describe the relationship between the resting pulse rate and miles run per week.

(1 mark)

24 Use trial and improvement to complete the table to find a solution to the equation

$$x^3 - 2x = 90$$

Give your answer to 1 decimal place.

x	x^3-2x	Comment
4	56	Too low
5	115	Too high

Answer $x = \dots (3 \text{ marks})$

25 Jane earns £11 400 per year. After her pay rise she earns £12 198 per year.

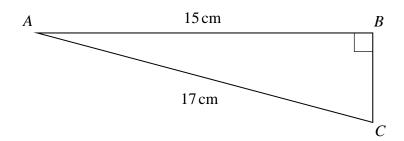
What was her percentage pay rise?

•••••	•••••	•••••	 ••••••

.....

Answer		%	(3 marks)
--------	--	---	-----------

26 ABC is a right-angled triangle. AB = 15 cm, AC = 17 cm



Not drawn accurately

Calculate the length of	f the side <i>B</i>	C.			
	Answer			cm	(3 marks)

END OF QUESTIONS

4301/2F Mark Scheme

Q	Answers	Mark	Comments
	(£) 3.16	B1	
	(£) 5.88	B1	
1a	(£) 4.25	B1	
	(£) 13.29	B1ft	
1b	$10 - 9 \times 0.57$ or 5.13	M1	oe eg 513(p)
	4.87	A1	
2a	50	B1	
2b	1/4	B1	oe
3a	$^{2}/_{6}$ and $^{6}/_{18}$	B2	-1 eeoo 2 right 1 wrong B1 1 right 2 wrong B0
3b	0.7(0)	B1	
3c	0.3(0)	B1	
4a	(-4, 1)	B1	
4b	Correct reflection	B2	B1 Reflected triangle in wrong position, or Any 2 points in correct position
5a	8.4	B1	allow ± 1mm
5b	69	B2	allow ± 1mm (68 to 70) B1 6.9 or (their 6.9) × 10 or digits 68 to 70 SC1 79
	27	B1	
6a	33	B1ft	(their 27) + 6
	11	B1	
6b			(their 11) × 2 – 3 Sc. B1 19 and 11 reversed on answer line only

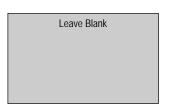
Q	Answers	Mark	Comments
7a	8 cm	B1	
7bi	Any diameter drawn	B1	Straight line within 2 mm of centre
7bii	Any cross on the circumference	B1	± 2 mm
7biii	Any tangent drawn	B1	Straight line within 2 mm of circumference
8ai	or or or	B1	
8aii	Explanation eg Too many squares There is a gap (when folded) One square needs to move	B1	oe Ignore irrelevant statements Penalise contradictory statements
8bi	or	B1	
8bii		B1	
9a	7	B1	
9bi	91	B1	
9bii	81	B1	
	$7 + 5 \text{ or } \sqrt{144}$	M1	or 12
9с	88	A1	
10a	Cardiff	B1	allow –4
10b	5	B1	
10c	6	B1	
10d	_5	B1	

Q	Answers	Mark	Comments
110;	10	B2	B1 each term
11ai	n+10p		B1 each term
11aii	$10n^2$	B1	
11bi	x+3	B1	or $3 + x$
11bii	$\frac{x}{2}$	B1	or $x \div 2$ or $\frac{1}{2}x$ or $\frac{1}{2} \times x$ or $x \times \frac{1}{2}$
12ai	9	B1	
	6, 7, 8, 8, 9, 9, 9	M1	
12aii	8	A1	
	3+6+7+8+8+4+6	M1	or 42
12b	(their 42) ÷ 7	M1	
	Mean = 6	A1	
	Betty's scores are more spread out	B1ft	Betty has bigger range of scores oe
12c	Betty has a lower average score	B1ft	Betty has a lower mean score oe Deduct 1 for contradictory statement(s)
13a	7643	B1	
13bi	34	B1	
13bii	47	B1	
	1 (0.25 (0.5)		
14	1 - (0.25 + 0.3)	M1	oe
	0.45	A1	
	180 – 125	M1	or 55
15	180 – (55 + 34)	M1	or 360 – (125 + 55 + 55 + 34) oe M2 125 – 34 oe
	91	A1	

Q	Answers	Mark	Comments
	$2 \times 14 + 2 \times 10.75$	M1	or £49.50 oe
16a	(their 49.5) – 45	M1	
	4.50	A1	or 4.5 M2A0
	27 × 8.6	M1	or £232.20 oe
	265.8 – (their 232.2)	M1	or £33.60 oe
16b	33.6 ÷ 11.2 or 3	M1	
	(their 3) + 2 or 5	A1ft	ft if M2 awarded and integer answer SC1 2 (adults) go free seen only
17a	7	B1	
17b	Line from (11.15,12) to (13.00, 12)	B1	± 1mm.
	'Line' from (13.00, 12) to (13.45,0)	B1ft	ft their $(13.00, 12) \pm 1$ mm.
	6.385475, 6.38547486	B1	6.3854
18	6.4	B1ft	f.t. their answer if correctly rounded from a value seen greater then 2d.p. 6.40 is B0
19a	4400	B1	
	(their 4400 – 800) ÷ 150	M1	
19b	24	A1ft	ft if M1 awarded.
	Line of 7.5 cm (or 4.5 cm or 5.5 cm) drawn	B1	± 2 mm
20a	Two intersecting arcs for remaining lengths	M1	1 length correct ± 2 mm
	Fully accurate triangle	A1	All lengths ± 2 mm
20b	74.5	B1	
21a	3x+6	B1	2/5 2 3
21b	2(3a-5)	B1	or $-2(5-3a)$
21	$(A) = (2r)^2$	B1	oe
21c	(–) a full circle	B1	Must make reference to full circle or 4 × quarter circles

Q	Answers	Mark	Comments
	Reflection	B1	Must be single transformation
22a	y = -1	B1	
22bi	3	B1	or 3:1 or 6:2
22bii	22bii (6, 4)		Accept any clear indication eg 6-4 or marked on grid
23a	3	B1	
23b	Line between limits	B1	Passing between (20, 71) and (20, 76) (inclusive) at one end and (65, 47) and (70, 50) (inclusive) at the other. If not 'ruled' B0.
23c	(63)	B1ft	ft their line. ± 1mm
23d	Negative correlation or More miles run, lower pulse rate	B1	oe
	Guess between 4 and 5	B1	Must be evaluated correctly to at least nearest whole number (4.1, 60.721), (4.2, 65.688), (4.3, 70.907), (4.4, 76.384), (4.5, 82.125), (4.6, 88.136), (4.7, 94.423), (4.8, 100.992), (4.9, 107.849)
24	Bracketing answer between 4.6 and 4.7 (inclusive)	B1	Any values between 4.6 and 4.7 that bracket answer.
	Testing a value ≤ 4.65 and > actual answer (4.6301141) and stating answer as 4.6	B1	(4.65, 91.244625), (4.64, 90.617344)
	12198 – 11400	M1	798 implies M1. 12198/11400x100 = (x) M1 12198/1140 = 1.07 M1
25	Their 798/11400 x 100	DM1	Their 'x' - 100 DM1 (1.07 - 1) x (100) DM1
	7	A1	
	17 ² – 15 ² (=64)	M1	or $x^2 + 15^2 = 17^2$
26	√64	DM1	For squaring, subtracting and indication of square rooting
	8	A1	

Surname		Other I	Names			
Centre Number			Candi	date Number		
Candidate Signature						



General Certificate of Secondary Education June 2008

MATHEMATICS (SPECIFICATION A) Higher Tier Paper 2 Calculator

4301/2H



Specimen Paper (Two-Tier Specification) 2008



For this paper you must have:

- a calculator
- mathematical instruments.



Time allowed: 2 hours

Instructions

- Use blue or black ink or ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Answer the questions in the spaces provided.
- Use a calculator where appropriate.
- Do all rough work in this book.
- If your calculator does not have a π button, take the value of π to be 3.14 unless another value is given in the question.

Information

- The maximum mark for this paper is 100.
- The marks for questions are shown in brackets.
- You may ask for more answer paper, graph paper and tracing paper. This must be tagged securely to this answer book.

Advice

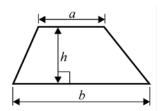
• In all calculations, show clearly how you work out your answer.

For Examiner's Use			
Pages	Mark		
3			
4 – 5			
6 – 7			
8 – 9			
10 – 11			
12 – 13			
14 – 15			
16 – 17			
18 – 19			
20 – 21			
22			
TOTAL			
Examiner's Initials			

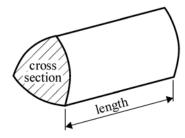
There are no questions printed on this page

Formulae Sheet: Higher Tier

Area of trapezium =
$$\frac{1}{2}(a+b)h$$

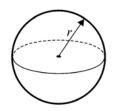


Volume of prism = area of cross section \times length



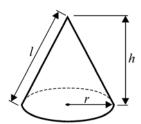
Volume of sphere
$$=\frac{4}{3}\pi r^3$$

Surface area of sphere =
$$4\pi r^2$$



Volume of cone =
$$\frac{1}{3}\pi r^2 h$$

Curved surface area of cone = $\pi r l$

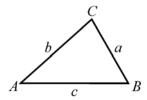


In any triangle ABC

Area of triangle =
$$\frac{1}{2} ab \sin C$$

Sine rule
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine rule
$$a^2 = b^2 + c^2 - 2bc \cos A$$



The Quadratic Equation

The solutions of $ax^2 + bx + c = 0$, where $a \ne 0$, are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

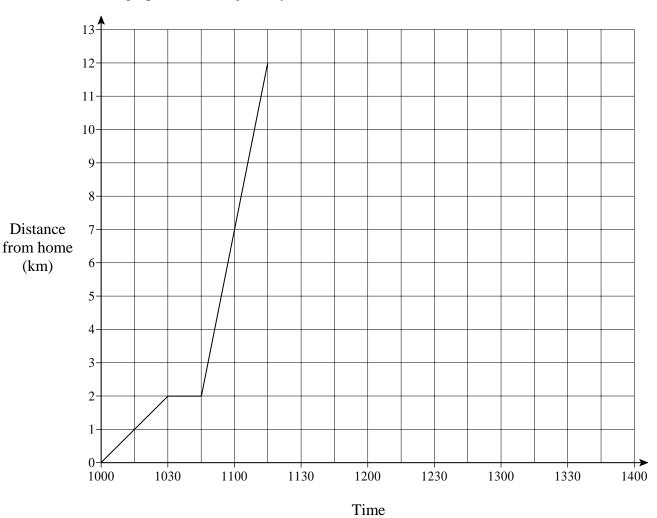
Answer all questions in the spaces provided.

1 Mr Smith leaves home at 10 am to go to the shopping mall.

He walks to the station where he catches a train.

He gets off at the mall.

The travel graph shows his journey.



After shopping Mr Smith goes home by taxi.

The taxi leaves the mall at 1 pm and arrives at his home at 1.45 pm.

(a) Complete the travel graph.

(2 marks)

(b) Calculate the average speed of the taxi.

.....

Answer km per hour

(2 marks)

2 A camera is advertised in two shops. VAT is 17.5%





	Answer		(4 marks)
In which shop is the ca	amera cheaper and by	now much?	

4

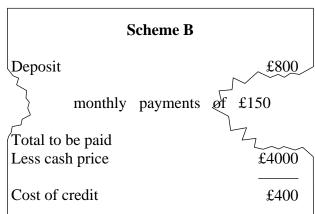
TS/SP08/4301/2H Page 96

3 A car dealer is offering two different schemes to buy a car. Some parts of Scheme B are missing.



CASH PRICE £4000

Scheme A	
Deposit	£1200
12 monthly payments of £250	£3000
Total to be paid	£4200
Less cash price	£4000
Cost of credit	£200



(a)	Work out the total to be paid using Scheme B.	
	Answer £	(1 mark)
(b)	Work out the number of monthly payments using Scheme B.	
	Answer	(2 marks)

7

Turn over ▶

4 Part of a number grid is shown below.

1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31	32	33	34	35

The shaded cross is called C_{11} because it has the number 11 at the centre.

(a) This is C_n

n – 7	
n	

Fill in the empty boxes.

(2 marks)

(b) Kevin notices that 4 + 10 + 12 + 18 = 44and that $4 \times 11 = 44$

times the number at the centre of the cross.

Show, using algebra, that the sum of the arms of any cross is equal to four

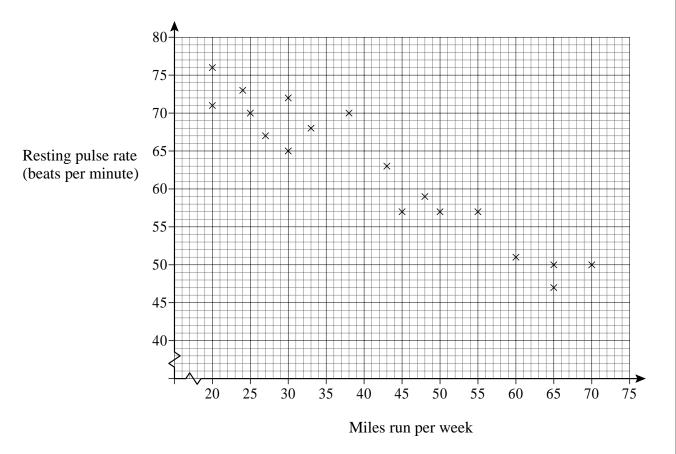
(2 marks)

5	Use your calculator to work or	$\frac{95.4 + 18.9}{35.2 - 17.3}$	
	(a) Write down your full cale	culator display.	
	Answe	r	(1 mark)
	(b) Give your answer to 2 sig	gnificant figures.	
	Answe	r	(1 mark)
6	Bag A contains x counters. Bag B contains 8 more counter Bag C contains twice as many		
	(a) Write down the number of	of counters in bags B and C .	
	x		
	$\operatorname{Bag} A$	Bag B	Bag C
	Answe	r Bag B count	
	(b) Show that the total numb	er of counters in bags A, B and C is $4(x +$	

(2 marks)

Dan	Dan and Doris are doing a survey on the type of music people buy.			
(a)	This is one question from Dan's survey.			
		Classical music is just for snobbish people. Don't you agree? Tick (✓) a box. Strongly agree		
	Give tw	o criticisms of Dan's question.		
	Criticism	n 1		
	Criticism	m 2		
			(2 marks)	
(b)	This is a	a question from Doris' survey.		
		Do you buy CDs? Yes No		
		If yes, how many CDs do you buy on average each month?		
		2 or less 3 or 4 5 or 6 More than 6		
	Give tw	o reasons why this is a good question.		
	Reason	1		
	Reason	2		
			(2 marks)	

8 Some runners recorded their resting pulse rates and miles run per week. The scatter graph shows the results.



(a) How many runners have a resting pulse rate of 57 beats per minute?

Answer (1 mark)

(b) Draw a line of best fit.

(1 mark)

(c) Predict the resting pulse rate of a runner who runs 40 miles per week.

Answer beats per minute (1 mark)

(d) Describe the relationship between the resting pulse rate and miles run per week.

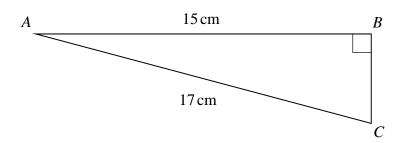
.....

(1 mark)

8

Turn over ▶

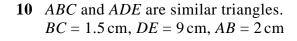
9 ABC is a right-angled triangle. AB = 15 cm, AC = 17 cm



Not drawn accurately

Calculate the length of the side BC.

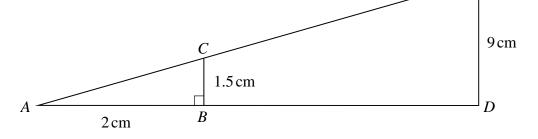
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•••••	 ••••••	•••••



Not drawn accurately

 \boldsymbol{E}

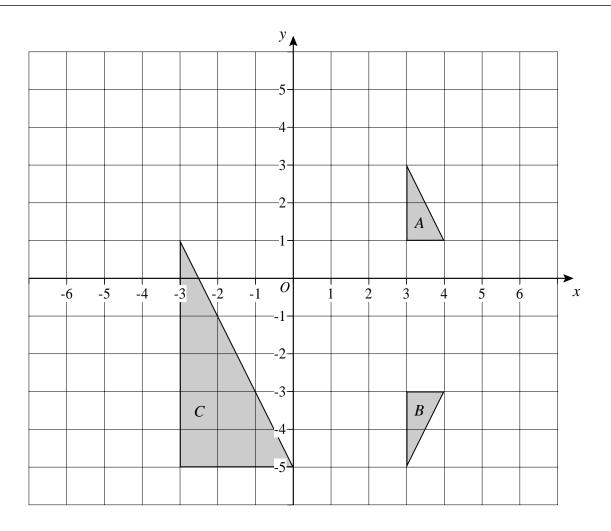
(3 marks)



Calculate the length of BD.

11	(a)	Expand $3(x+2)$
		Answer
	(b)	Factorise $6a - 10$
		Answer
	(c)	Factorise fully $6a^2b + 9ab^2$
		Answer
12		sh contains 2000 bacteria. number of bacteria increases by 16% per hour.
	How	many bacteria will be in the dish after 12 hours?
	•••••	
	•••••	
		Answer

13



(a)	Describe the transformation that maps triangle A to triangle B.
	(2 marks)

(b)	Triangle <i>A</i> is rotated 90° anti-clockwise about $(0, -1)$.
	Draw the image of A after this transformation.

(2 marks)

- (c) Triangle C is an enlargement of triangle A.
 - (i) Write down the scale factor of the enlargement.

Answer (1 mark)

(ii) Write down the coordinates of the centre of the enlargement.

Answer (.....) (1 mark)

14 Use trial and improvement to complete the table to find a solution to the equation

$$x^3 - 2x = 90$$

Give your answer to 1 decimal place.

x	x^3-2x	Comment
4	56	Too low
5	115	Too high

Answer $x = \dots (3 \text{ marks})$

15	(a)	Write 0.000 000 07 in standard form.	
		Answer	(1 mark)
	(b)	The planet Mercury is approximately a sphere of radius 2440 km.	
		Calculate the approximate volume of the planet Mercury. Give your answer in standard form to an appropriate degree of accuracy.	
		Answer km ³	(3 marks)
16	AB =	C is a right-angled triangle. $= 60 \mathrm{m}$ $B \bigcirc C$	
	Ang	gle $BAC = 32^{\circ}$	
		60 m Not drawn a	ccurately
		32°	
	Find	and the length of BC .	
		Answer m	(3 marks)

17 Cases each weigh 20 kg to the nearest kilogram.			
	What is the least that six cases could weigh?		
	Answer kg (2 marks)		
18	Solve the equation $\frac{x+3}{3} + \frac{x-4}{2} = 1$		
	Answer $x = \dots (4 \text{ marks})$		

Turn over for the next question

19

Sale

Exercise Bike

 $17\frac{1}{2}$ % off

Now £181.50

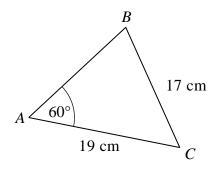


How much was the exercise bike before the reduction?	
Answer £	

20	y is inversely proportional to the square root of x. When $x = 16$, $y = 2$				
	Wha	at is the value of y when $x = 0.25$?			
		Answer	(3 marks)		
21	(a)	Solve the inequality $3x + 7 \ge 13$			
		Answer	(2 marks)		
	(b)	A mathematics teacher says			
		I am thinking of an integer. I double the integer and add 1. The result is less than –7.			
		What is the largest integer the teacher could have thought of?			
		Answer	(2 marks)		

Turn over ▶

22 (a) ABC is a triangle. $AC = 19 \text{ cm}, AC = 17 \text{ cm} \text{ and angle } BAC = 60^{\circ}$

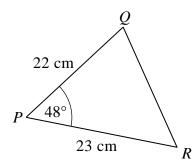


Not drawn accurately

Calculate the size of angle	e ABC.	

Answer degrees

(b) PQR is a triangle. PR = 23 cm, PQ = 22 cm and angle $QPR = 48^{\circ}$

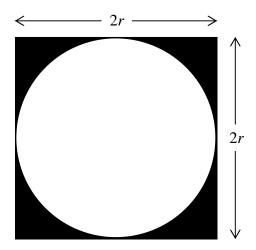


Not drawn accurately

(3 marks)

Calculate the length of	_		
		 •••••	•••••
		 •••••	
		 •••••	

23 A star shape is made by cutting quadrants of a circle from a square of side 2r.



(a) Show that the shaded area is given by the formula

	. 2	
Α	$=4r^{2}$	$-\pi r$

•••••	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	•••••
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(2 marks)

(b) Rearrange the formula $A = 4r^2 - \pi r^2$

to make r the subject.

.....

Answer (3 marks)

11

Turn over ▶

24	The	triangle	number	600	mence	ic
<i>2</i> 4	1 ne	triangie	number	seq	uence	18

1, 3, 6, 10, 15, 21, ...

The nth term of this sequence is given by

$$\frac{1}{2} n(n+1)$$

(a)	Write down an algebraic expression for the $(n-1)$ th term of the sequence.
	Answer
(b)	Prove, algebraically, that the sum of any two consecutive triangle numbers is a square number.
	(3 marks)

25 The table shows the weights of 100 children in year 7.

An estimate of the mean weight of the children is calculated as 44 kg.

Calculate the values of a and b.

Weight, w (kg)	Frequency
$20 < w \leqslant 30$	12
$30 < w \leqslant 40$	21
40 < w ≤ 50	38
50 < w ≤ 60	а
60 < w ≤ 70	ь

Answer $a = \dots$, b =	(6 marks)

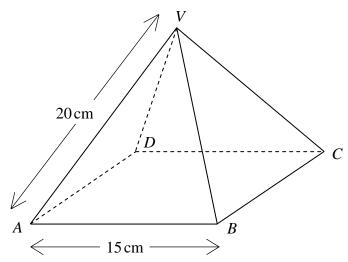
10

26 *VABCD* is a right pyramid on a square base.

V is vertically above the centre of the square.

$$VA = VB = VC = VD = 20 \text{ cm}$$

$$AB = 15 \,\mathrm{cm}$$



Not drawn accurately

Calculate the angle between the edge VA and the base $ABCD$.			

END OF QUESTIONS

Answer degrees

(5 marks)

4301/2H Mark Scheme

Q	Answers	Mark	Comments
	Line from (11.15,12) to (13.00, 12)	B1	± 1mm.
1a	'Line' from (13.00, 12) to (13.45,0)	B1ft	ft their $(13.00, 12) \pm 1$ mm.
1b	'Their 12' ÷ 'Their 45m'	M1	oe i.e 12 ÷ 0.45, 1200 ÷ 45 etc Allow ft from the 'distance' and 'time' on their graph
	16	A1ft	ft if M1 awarded rounded to ≥ 3 sf.
	sight of 0.175	B1	
	330 × 1.175	M1	
2	387.75	A1	
	Carry's by £2.75	A1	must see £ sign Carry's can be implied
3a	4400	B1	
	(their 4400 – 800) ÷ 150	M1	
3b	24	A1ft	ft if M1 awarded.
4a	<i>n</i> -1, <i>n</i> +1, <i>n</i> +7	B2	-1 eeoo NB <i>n</i> -8, <i>n</i> +8 is one error
	n-1+n+1+n-7+n+7	M1	Attempt to add their 'arms'
4b	$=4 \times n$	A1	Accept 4 <i>n</i> . Do not need to see 'cancelling'
	6.385475, 6.38547486	B1	6.3854
5	6.4	B1ft	f.t. their answer if correctly rounded from a value seen greater then 2d.p. 6.40 is B0
	x + 8	B1	
6a	$\frac{x+8}{2x}$	B1	
	x + x + 8 + 2x	M1	
6b	4x + 8 = 4(x+2)	A1	Can be shown either way but must be stated. SC1 Complete correct numerical verification

Q	Answers	Mark	Comments
70	Valid criticism	B1	eg Question offensive Leading question
7a	Valid criticism	B1	eg No option to disagree Not enough choices
7b	Valid reason	B1	eg Yes No answer Simple question
70	Valid reason	B1	eg All possible responses covered. Not too many choices for responses.
8a	3	B1	
8b	Line between limits	B1	Passing between (20, 71) and (20, 76) (inclusive) at one end and (65, 47) and (70, 50)(inclusive) at the other. If not 'ruled' B0.
8c	(63)	B1ft	ft their line. ± 1mm
8d	Negative correlation or More miles run, lower pulse rate	B1	oe
	T	<u> </u>	
	$17^2 - 15^2$ (=64)	M1	or $x^2 + 15^2 = 17^2$
9	√64	M1dep	For squaring, subtracting and indication of square rooting
	8	A1	
	r 0		1.
	$\frac{x}{2} = \frac{9}{1.5}$	M1	oe. Scale factor 6, $\frac{1}{6}$ etc.
10	(AD=)12	A1	SC 12 on answer line with no working B1.
	BD = 10	A1	

Q	Answers	Mark	Comments		
	2 1 6	D1			
11a	3x+6	B1			
11b	2(3a-5)	B1	-2(5-3a)		
11c	3ab(2a+3b)	B2	B1 for $3ab$ B1 for $(2a + 3b)$ B1 for correct partial factorisation with at least two common factors outside bracket. eg $3a(2ab + 3b^2)$		
12	Sight of 1.16	B1	If calculate 'interest' and 'add on' method used award M1 if at least three years shown. A1 for all 12 values accurate or rounded ≈ 2320, 2691, 3122, 3621, 4201, 4873, 5652, 6557, 7606, 8823, 10235, 11872.		
	2000 x their '1.16',12	M1	Their 1.16 must be sensible 1.016, 1.6 etc.		
	11870 to 11875	A1	Allow 11900 or 12000 if working seen.(no ft) 9872 is sc2 unless 11872 seen then fw.		
13a	Reflection	B1	Must be single transformation		
13b	B1 B2 B1 B2	B1 B2	B2 Fully correct B1 if 90° clockwise about (0, -1) B1 if 90° anti-clockwise about (-1, 0) B1 if 90° clock-wise about (0, 1)		
13c	3	B1	or 3:1 or 6:2		
	(6, 4)	B1	Accept any clear indication eg 6-4 or marked on grid		

Q	Answers	Mark	Comments
14	Guess between 4 and 5	B1	Must be evaluated correctly to at least nearest whole number (4.1, 60.721), (4.2, 65.688), (4.3, 70.907), (4.4, 76.384), (4.5, 82.125), (4.6, 88.136), (4.7, 94.423), (4.8, 100.992), (4.9, 107.849)
	Bracketing answer between 4.6 and 4.7 (inclusive)	B1	Any values between 4.6 and 4.7 that bracket answer.
	Testing a value ≤ 4.65 and $>$ actual answer (4.6301141) and stating answer as 4.6	B1	(4.65, 91.244625), (4.64, 90.617344),
15a	7 x 10 ⁻⁸	B1	
	$(V =) \frac{4}{3} \pi x \cdot 2440^{3}$	M1	2440 could be 2400, 2450
15b	5.5 to 6.2 x 10 ¹⁰ (Does not have to be SF)	A1	If $\pi = 3$ used accept 5.8 x 10^{10} If $\pi = 3.1$ used accept 6 x 10^{10}
	Any value between 5.5 and 6.2 rounded to 4sf or better x 10 ¹⁰	B1	ft their volume if a value ≥ 4sf seen or implied and correctly rounded to 1sf, 2sf., 3 s.f. or 4sf
16	Sight of tan	M1	NB alternative methods such as sine rule must be used correctly for M1 and must be complete, so if for example Hypotenuse found Pythagoras or further trig must be used.
	(BC =) 60 tan 32	M1dep	
	BC = 37.5, 37.49()	A1	
17	6x19.5	B1	
	117	B1	

Q	Answers	Mark	Comments
18	2(x+3)+3(x-4)	M1	Allow one error. No brackets must be recovered $2(x+3) + 3(x-4) = 6$ is M2
	5x-6	A1	oe
	Their ' $5x - 6$ ' = 6	M1dep	M1dep for = 6. NB $5x = 7$ implies A1 if RHS = 1 and M1 awarded
	$(x=)^{12}/_{5}=2.4$	A1ft	ft 'their $5x - 6$ ' = 6 if both Ms awarded.
	Sight of 0.825	B1	82.5% = 181.50 M1
10	181.50 ÷ 0.825	M1	$1\% = 2.2$ A1 oe $181.5 \div 82.5 \times 100$
19			1/0 - 2.2 AT 0C 181.3 · 82.3 X 100
	220	A1	
	$y \alpha \frac{1}{\sqrt{x}} \text{ or } y = \frac{k}{\sqrt{x}}$	M1	oe
20	k = 8	A1	k = -8
	(y =) 16	A1	-16
	$3x \ge 13 - 7(6)$	M1	
21a	$x \ge 2$	A1	
21b	2x + 1 < -7 or attempt at inverse function	M1	eg -7 -1 ÷ 2
	x = -5	A1	
22a	$\frac{\sin B}{19} = \frac{\sin 60}{17}$	M1	$\begin{array}{ccc} Accept & \underline{19} & = & \underline{17} \\ Sin B & & sin 60 \end{array}$
	Sin B = 0.9679(1)	A1	
	B = 75.4()	A1	
22b	$x^2 = 22^2 + 23^2 - 2 \times 22 \times 23 \times \cos 48$	M1	
	$x^2 = 335.8()$	A1	
	x = 18.32()	A1ft	ft only if an error made in calculation of x^2 but not on $(22^2+23^2-2 \text{ x}22\text{x}23 (=1))\cos 48$ $(=\sqrt{0.669}=0.818)$

Q	Answers	Mark	Comments
23a	$(A =) (2r)^2$	B1	oe
	(-) (a full circle)	B1	Must make Reference to full circle or 4 x quarter circles
23b	$(A =) r^2(4-\pi)$	M1	
	$r^2 = A \div (4 - \pi)$	A1	
	$r = \sqrt{(A \div (4 - \pi))}$	A1	oe. Must have $r =$
24a	$\frac{1}{2}n(n-1)$	B1	or equivalent
24b	$\frac{1}{2}n(n-1) + \frac{1}{2}n(n+1)$	M1	or equivalent eg $\frac{1}{2}n(n+1) + \frac{1}{2}(n+1)(n+2)$
	$\frac{1}{2}n^2 - \frac{1}{2} + \frac{1}{2}n^2 + \frac{1}{2}$	A1	$n^2 + 2n + 1$
	n^2	A1	$(n+1)^2$
	a+b=29	B1	Sight of 29 alone is not B1
	12×25 + 21×35 + 38×45 +55 <i>a</i> +65 <i>b</i> (= 4400)	M1	
	55a + 65b = 1655	A1	oe
25	55a + 55b = 1595	M1	oe $65a + 65b = 1885$ for balancing and attempting to eliminate.
	10b = 60	A1	10a = 230
	a = 23, b = 6,	A1	Need both Ucb, lcb used B1, M0, A0, M1, A0 possible.
26	Identifying $\triangle VAC$ or $\angle VAC$	B1	Can be implied by working.
	$AC^2 = 15^2 + 15^2$	M1	oe
	$^{1}/_{2}AC = 10.6(066)$	A1	$\sqrt{450 \div 2}$ is A1 $\sqrt{450}$ is A1 if used in cos rule on <i>VAC</i> .
	$VAC = \cos^{-1}(\text{their }^{1}/_{2}AC \div 20)$	M1dep	
	$VAC = 57.97^{\circ} \text{ or } 58^{\circ}$	A1	