

General Certificate of Secondary Education June 2011

Methods in Mathematics (Pilot)
93652F
(Specification 9365)
Unit 2: Methods in Mathematics
Written Paper (Foundation)

Mark Scheme

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Q Marks awarded for quality of written communication. (QWC)
M Dep A method mark dependent on a previous method mark being awarded.

BDep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe $\quad$ Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$

## M2 Foundation Tier

| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |

Note: Consistent use of coordinates the wrong way round. Deduct 1 mark.

| 1(a) | $(2,4)$ | B1 |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 ( b )}$ | Correct plot | B1 |  |
| $\mathbf{1 ( c )}$ | $(2,7),(5,7)$ | B2 | B1 Each (square need not be shown) |
| Alt 1 <br> $\mathbf{1 ( c )}$ | $(2,1),(5,1)$ | B2 | (square need not be shown) |
| Alt 2 <br> $\mathbf{1}$ (c) | $(3.5,5.5),(3.5,2.5)$ | B2 | SC1 For correct square drawn but wrong <br> (square need not be shown) <br> For example plotting B B at (4,5) gives a <br> square at (3,2) and (5,3) or (1,6) and (3,7) |
| Alt 3 <br> $\mathbf{1 ( c )}$ | Follow through their plot for B |  |  |


| 2 | £ $1-72 \mathrm{p}(=28)$ in either (a) or (b) | B1 |  |
| :---: | :---: | :---: | :---: |
| 2(a) | ```\(10(p), 5(p) .5(p), 5(p), 1(p), 1(p)\), 1 (p) or \(5(p), 5(p), 5(p), 5(p), 5(p), 2(p)\), 1 (p) or \(20(p), 1(p), 1(p), 1(p), 1(p), 2(p)\), 2 (p) or \(10(p), 10(p), 2(p), 2(p), 2(p), 1(p)\), 1 (p) or \(10(p), 5(p), 5(p), 2(p), 2(p), 2(p), 2(p)\)``` | B1 ft | ft On their ' 28 ' if calculation seen, <br> eg, $£ 1-72=32 p$, but only for 1 mark maximum in (a) or (b) <br> Their 28 can be found by adding coins ie, do not need to see working. |
| 2(b) | $20(p), 5(p), 2(p), 1(p)$ | B1 ft | If their 4 coins total is the same as the seven coin total in (a) only if no calculation seen in (a) |


| 3(a) | 3480 | B1 |  |
| :--- | :--- | :--- | :--- |
| 3(b) | 3500 | B1 |  |
| 3(c) | 8734 | B2 | B1 For 8374 or 8743 |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 4(a) | Radius is half of the diameter or <br> diameter is twice the radius <br> or $d=2 r$ or $r=\frac{1}{2} d$ | Q1 | Strand (iii) - Correct grammar or notation |
| :---: | :--- | :--- | :--- |
| 4(b) |  | B1 | Any chord, including one that looks as <br> though it may be a diameter <br> Freehand lines must be straight to within <br> 1mm tolerance <br> Accept lines beyond circle <br> No shading |
| 4(c) |  | Bither side of chord must be shaded or <br> clearly indicated <br> Any segment including a semi-circle <br> Freehand lines must be straight to within <br> 1 mm tolerance |  |


| $\mathbf{5}$ | $110-10-10(=90)$ | M1 | $20+3 d=100 \quad$ oe <br> Sight of 90 implies M1 |
| :--- | :--- | :---: | :--- |
|  | Their '90' $\div 3$ | M1 | $3 d=90$ |
|  | 30 | A1 |  |
|  | Any value chosen for $d$, multiplied by <br> 3 and 20 added | M1 | oe |
|  | Another value chosen for $d$, <br> multiplied by 3 and 20 added that <br> gives a value closer to 110 | M1 | $3 d=90$ |
|  | 30 | A1 |  |

$6 \quad E, B, A, D, C$
B2
B1 For any of these seen in the order $E B, B A, A D, D C$

| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 7(a) | 12 | B1 |  |
|  | $\mathrm{cm}^{3}$ | B1 |  |
| 7(b) | $2+3+2+3+2+3$ | M1 | oe At least 5 seen |
|  | 15 | A1 |  |


| 8(a) |  | B2 | B1 For reversed shape anywhere |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 8(b)(i) | 2 |  |  |  |
| 8(b)(ii) | 2 |  |  |  |


| 9 | Any two numbers that total 10 <br> multiplied together, eg $6 \times 4=24$ | M1 | Product total must be seen |
| :---: | :--- | :---: | :--- |
|  | Second attempt with both values <br> closer to actual answers | M1 |  |
|  | 3.5 and 6.5 | A1 |  |
|  | $a+b=10$ or $a b=22.75$ | M1 |  |
|  | $a(10-a)=22.75$ | M1 | oe |
|  | 3.5 and 6.5 | A1 |  |


| $\mathbf{1 0}$ | $6 \times 30(=180)$ | M1 | $\frac{6}{5}$ or 1.2 |
| :---: | :--- | :---: | :--- |
|  | Their $180 \div 5$ | M1 | $\frac{6}{5} \times 30$ is M2 |
|  | 36 | A1 |  |
| $\mathbf{1 1 ( a )}$ | $2,-4$ | B2 | B1 Each |
| $\mathbf{1 1 ( b )}$ | Odd, or all terms even | B1 | oe |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 12(a) | Reference to sides being 4 and 3 or areas of other shapes and $P$ being 36 | B1 |  |
| 12(b) | $C$ and $E$ or $A$ and $C$ or $A$ and $E$ | B1 | Allow more than one correct answer but any 2 answers, with one wrong is B0 |
| 12(c) | Sight of 36 and $4\left(\mathrm{~cm}^{2}\right)$ | M1 | $3^{2}$ |
|  | 9 | A1 |  |


| 13 | $w$ and $4 w$ and attempt to add or dashes marked on diagram | M1 | Any multiple of 22 seen implies M1 |
| :---: | :---: | :---: | :---: |
|  | $22 w$ | A1 |  |
|  | (Width = ) 2.5, $\frac{55}{22}$ or equivalent | A1 ft | ft If $M$ awarded. <br> 2.5 seen then 10 ( 3 marks) 10 from valid working but no 2.5 seen (2 marks) |
| Alt 13 | Values for length and width chosen in ratio 4:1 and perimeter of large rectangle correctly calculated ( $22 \times$ width) | M1 |  |
|  | Another pair of values for length and width chosen in ratio 4:1 and perimeter of large rectangle correctly calculated ( $22 \times$ width) giving an answer closer to 2.5 | M1 |  |
|  | (Width $=$ ) 2.5, $\frac{55}{22}$ or equivalent | A1 |  |


| 14 | Any three different acute angles that <br> add up to $180^{\circ}$ (accept $90^{\circ}$ as acute) | B2 | B1 For any three acute angles <br> or any three angles that add up to <br> $180^{\circ}$ |
| :---: | :--- | :---: | :---: |
| 15(a) | $5.24913 \ldots$ | B1 |  |
| 15(b) | 5.25 | B1 ft | ft Their (a) if at least 3 dp |


| Q | Answer |  | Mark |
| :---: | :--- | :---: | :--- |
| ${ }^{*}$ *16 | Sight of 1.035 or 103.5 | B1 | Sight of digits 4968 implies B1 |
|  | $480 \times 1.035$ | M1 | oe |
|  | 496.80 | Q1 | 496.8 is Q0 SC1 for 648 (from 0.35) |
|  | $480 \times 3.5 \div 100$ | M1 | oe |
|  | 16.8 | M1 |  |
|  | 496.80 | Q1 | 496.8 is Q0. SC1 for 648 (from 0.35) |


| 17(a) |  | B3 | Part marks to a maximum of 2 for <br> 6 in 'outside’ B1 <br> 12 in overlap B1 <br> 26 total in both circles B1 |
| :---: | :---: | :---: | :---: |
| Alt 17(a) | $x$ marked in intersection, $23-x$ in History, $15-x$ in French | M1 |  |
|  | $x+23-x+15-x+6=32$ | M1 |  |
|  | $x=12$ | A1 |  |
| 17(b) | 3 | B1 ft | ft Their Venn diagram if the intersection is populated. |


| $\mathbf{1 8 ( a )}$ | Evidence of counting squares or <br> breaking shape into squares and <br> triangles/trapezia, etc | M1 | Can draw a rectangle round the outside <br> and use a 'subtraction' method <br> If perimeter indicated in working M0A0 |
| :---: | :--- | :---: | :--- |
|  | Correct area shown for at least <br> 2of the shapes | A1 | 15 to 17 (if M1 awarded) |
|  | 16 | A1 |  |
| $\mathbf{1 8 ( b )}$ | Right or 90 | B1 |  |
| *18(c) | Shapes fit together (to cover plane) <br> or shapes leave no gaps or all <br> shapes fitting together at a point <br> have angle total $360^{\circ}$ | Q1 | Strand (i) |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 19 | $\pi \times 9^{2}$ | M1 | $\pi \times 4.5^{2}$ or $\pi \times 18^{2}$ |
|  | 254.3 to 254.5 or $81 \pi$ | A1 | 254 with working |


| 20(a) | 18 | B1 |  |
| :--- | :--- | :---: | :--- |
| $\mathbf{2 0 ( b )}$ | 2 | B1 |  |
| $\mathbf{2 0 ( c )}$ | Evidence of trying any number <br> between their 20(a) and their 20(b) | M1 |  |
|  | 2.4 | A1 |  |
| Alt 20(c) | $6 x-12=x$ | M1 |  |
|  | 2.4 | A1 |  |


| 21 | Rotation | B1 | Do not accept 'turn' |
| :---: | :--- | :---: | :--- |
|  | (Anticlockwise) $90^{\circ}$ | B 1 | Clockwise $270^{\circ}$ <br> (Do not accept $-90^{\circ}$ or $90^{\circ} \mathrm{C}$ ) |
|  | (Centre or about) $(2,-2)$ | B 1 |  |

\(\left.$$
\begin{array}{|l|l|c|l|}\hline \text { 22 } & \begin{array}{l}\text { Other two vertices plotted at (1, 4) } \\
\text { and (5, 4) and all sides drawn }\end{array} & \text { B3 } & \begin{array}{l}\text { Part marks to maximum of 2/3 } \\
\text { B1 Any kite with } A B \text { as long diagonal } \\
\text { B1 For two vertices plotted on } y=4 \text { and } \\
\text { not symmetrical. }\end{array}
$$ <br>
B2 For other two vertices plotted on <br>
y=4 and symmetrical about (3, 4) <br>
B2 For any kite with area 10 \mathrm{~cm}^{2} <br>

(ie vertices plotted on x=1 and x=5)\end{array}\right]\)| 23(a) | 4 | B1 |
| :--- | :---: | :--- |
| 23(b) | 5 | B1 |
| 23(c) | $3 y-6=4-2 y$ | M1 |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 24(a) | Triangle (C) drawn at $(8,5),(8,13)$ and (16, 5) | B2 | B1 For at least 2 rays from $(0,9)$ through corners of triangle B <br> or any triangle of correct size <br> or triangle with two of $(8,5),(8,13)$, $(16,5)$ as vertices <br> SC1 Enlarging $A$ by sf 2 to triangle at $(10,1),(14,1)$ and $(10,5)$ |
| :---: | :---: | :---: | :---: |
| 24(b) | (Scale factor) 4 | B1ft | ft For their triangle |
|  | (Centre) (4, 5) | B1ft | ft If rays drawn |

