

Unit 2 Number and Algebra - Foundation tier (43602F)**Question 3**

- 3** Jay has £1.50 in change.
She only has 20 pence and 10 pence coins.
She has twice as many 20 pence coins as 10 pence coins.

How many 20 pence coins does she have? (2 marks)

Mark scheme:

3	6	B2	B1 for twice as many 20s as 10s or coins total £1.50
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This question was targeted at grade G and assessed AO3.

The most common strategy was to list coins and then use trials to work out the answer, usually by listing coins and figuring out the correct response by trial.

The mean score was 1.35 out of 2 with 63% of candidates scoring the full 2 marks.

Candidate A

3 Jay has £1.50 in change.
 She only has 20 pence coins and 10 pence coins.
 She has twice as many 20 pence coins as 10 pence coins.

How many 20 pence coins does she have?

..... 20 20 20 20 20

..... 10 10 10 20

Answer 6 (2 marks)

The candidate matched up 10p and 20p coins as far as 90p then realised that three more 20p coins were needed to achieve the correct result.

Mark awarded = 2

Candidate B

3 Jay has £1.50 in change.
 She only has 20 pence coins and 10 pence coins.
 She has twice as many 20 pence coins as 10 pence coins.

How many 20 pence coins does she have?

..... 20 + 20 + 20 + 20 + 10 + 10 = ~~£1.00~~ 1.00

.....

Answer 4 (2 marks)

This candidate scored 1 mark for having twice as many 20p coins as 10p coins, even though the total is not £1.50.

Mark awarded = 1

Candidate C

3 Jay has £1.50 in change.
She only has 20 pence coins and 10 pence coins.
She has twice as many 20 pence coins as 10 pence coins.

How many 20 pence coins does she have?

$20^p \ 20^p \ 10^p = 50^p$ $20^p \ 20^p \ 10^p = 50^p$

$10^p \ 20^p \ 20^p = 50^p$

Answer She has 6 20p coins (2 marks)

This candidate grouped the coins into $2 \times 20p$ and $1 \times 10p$ giving subtotals of 50p. Having formed three groups of 50p to make £1.50 the 20p coins are then counted for the answer.

Mark awarded = 2

Candidate D

3 Jay has £1.50 in change.
She only has 20 pence coins and 10 pence coins.
She has twice as many 20 pence coins as 10 pence coins.

How many 20 pence coins does she have?

$20p \times 5 = \pounds 1.00$
 $10 \times 5 = \pounds 0.50$
 $\pounds 1.00 + \pounds 0.50 = \pounds 1.50$

Answer 5 (2 marks)

This candidate scored 1 mark because the total of £1.50 given is correct, although the 'twice as many' requirement has not been met.

Mark awarded = 1

Question 6

*6 Here are the monthly charges for Mark's mobile phone.

Monthly charge £15
 100 free minutes then 12p per minute
 200 free texts then 10p per text

During one month, Mark makes 150 minutes of calls and sends 285 texts.

Work out the total charge for the month. (5 marks)

Mark scheme:

6	150 – 100 or 50 or 285 – 200 or 85	M1	
	their 50 × 12 or 600 or 6	M1	
	their 85 × 10 or 850 or 8.5(0)	M1	
	their 6 + their 8.5(0) + 15	M1	oe allow mixed units
	29.50	Q1	strand (i) correct notation do not accept 29.5 SC4 for 14.50 SC3 for 14.5

This question targeted grade F and assessed AO2 and functionality.

There were many good answers. Over 70% of candidates scored at least 3 of the possible 5 marks.

The mean mark was 3.36.

The most common error was to omit the £15 monthly charge.

Candidate E

*6 Here are the monthly charges for Mark's mobile phone.

Monthly charge £15
 100 free minutes then 12 p per minute
 200 free texts then 10 p per text

During one month, Mark makes 150 minutes of calls and sends 285 texts.

Work out the total charge for the month.

£15 for free 100 minutes and 200 free texts.
 50 more minutes = 12p x ~~50~~ 50 = £6.00
 85 more texts =

80	5	500	x	10	2
85	x	100		50	100
10	800	600			
	50	800			
		50			
		850			

8.50 + 6.00 + 15
 = 29.50

Answer £ 29.50 (5 marks)

A fully correct and well explained solution.

Mark awarded = 5

Candidate F

*6

Here are the monthly charges for Mark's mobile phone.

Monthly charge £15
 100 free minutes then 12 p per minute
 200 free texts then 10 p per text

During one month, Mark makes 150 minutes of calls and sends 285 texts.

Work out the total charge for the month.

$150 - 100 = 50$ $50 \times 12 = 600$ (£6.00)
 12, 24, 36, 48, 60...
 $285 - 200 = 85$ $85 \times 10 = 850$ (£8.50)
 $£6.00 + £8.50 = £14.50$

Answer £ 14.50 (5 marks)

This candidate has omitted the £15 charge.

Mark awarded = 4

Candidate G

*6

Here are the monthly charges for Mark's mobile phone.

Monthly charge £15
 100 free minutes then 12 p per minute
 200 free texts then 10 p per text

During one month, Mark makes 150 minutes of calls and sends 285 texts.

Work out the total charge for the month.

.....
 Limit is 100 mins $12 \times 150 = 600$
 $£6$ $5 \times 85 = £4.85$
 $£4.85 + £6 = £10.85$

Answer £ 10.85 (5 marks)

This candidate calculates $50 \times 12p = £6.00$, but then multiplies 85 by 5 instead of 10. The candidate also omits the £15.

Mark awarded = 2

Candidate H

*6 Here are the monthly charges for Mark's mobile phone.

Monthly charge £15
 100 free minutes then 12 p per minute
 200 free texts then 10 p per text

During one month, Mark makes 150 minutes of calls and sends 285 texts.
 Work out the total charge for the month.

.....

$50 \times 12p = 60p$
 $85 \times 10p = \text{£}8.50$
 $+ \text{£}15.00$

60p
 8.50p
 $\text{£}15.00p$

 24.10
 |

.....

.....

.....

.....

Answer $\text{£} 24.10$ (5 marks)

This candidate makes an arithmetic error, giving $50 \times 12p = 60p$. This is the only error.

Mark awarded = 4

Candidate 1

*6

Here are the monthly charges for Mark's mobile phone.

Monthly charge £15
100 free minutes then 12 p per minute
200 free texts then 10 p per text

During one month, Mark makes 150 minutes of calls and sends 285 texts.

Work out the total charge for the month.

150 calls - 100 free calls = 50
 $50 \div 12 = 4.166666666666667$ £4.82

285 texts - 200 free texts = 85
 $85 \div 10 = 8.5$ £8.50

£4.82 + £8.50 =
 $\begin{array}{r} 4.82 \\ + 8.50 \\ \hline 13.32 \end{array}$

Answer £ 13.32 (5 marks)

This candidate used an incorrect method, giving $50 \div 12$ and $85 \div 10$. £8.50 has been obtained using the same incorrect method.

Mark awarded = 1 (for using 50 and 85 for the 'extra' minutes and texts).

Question 7

- 7 Kay has 325 beads.
 Sharon has 165 beads.
 Kay gives Sharon some beads.
 They now have the same number of beads.

How many beads does Kay give Sharon? (3 marks)

Mark scheme:

7	325 + 165 (=490)	M1	or 325 – 165 (= 160)
	their 490 ÷ 2 (=245)	M1dep	or their 160 ÷ 2
	80	A1	
	alternative method		
	Correct trial to make difference smaller eg. 300 and 190	M1	
	Improved correct trial eg. 225 and 265	M1	
	80	A1	

This question was targeted at grade F and assessed AO3.

Many candidates set out a correct method, but poor arithmetic frequently resulted in incorrect answers.

The mean mark was 1.77 out of 3 with over 50% of the candidates scoring 2 or the full 3 marks.

Candidate J

7 Kay has 325 beads.
 Sharon has 165 beads.
 Kay gives Sharon some beads.
 They now have the same number of beads.

How many beads does Kay give Sharon?

$165 + 35 = 200$

$200 + 125 = 325$ $35 + 125 = 160$

$165 + 80 = 245$

$325 - 80 = 245$

Answer 80 (3 marks)

This candidate works out the difference of 160 and correctly adds/subtracts 80 from each.

Mark awarded = 3

Candidate K

7 Kay has 325 beads.
 Sharon has 165 beads.
 Kay gives Sharon some beads.
 They now have the same number of beads.

How many beads does Kay give Sharon?

$325 - 5 + 5$ to 165 = 170 leaving Kay with
 320 and Sharon 170 $320 - 20 + 20 = 170 =$
 190 leaving Kay with 300 and Sharon
 with 190 $300 - 5 + 5$ to 190 = 195 =
 that leaves them with both the same

Answer 30 beads (3 marks)

This candidate uses a strategy of adding and subtracting equal amounts, starting with 5 and then 20. However, at the third step an arithmetic error is made, $300 - 5 = 195$, which leads to an incorrect answer.

Marks are awarded for correct trial followed by an improved correct trial.

Mark awarded = 2

Candidate L

7 Kay has 325 beads.
Sharon has 165 beads.
Kay gives Sharon some beads.
They now have the same number of beads.

How many beads does Kay give Sharon?

$$\begin{array}{r}
 165 \rightarrow 200 = 35 \quad 325 - 35 = \overset{3}{290} \\
 290 \quad 200 + 45 = 245 \quad 290 \\
 - 45 = 245
 \end{array}$$

Answer 245 (3 marks)

This candidate uses the same strategy as in the previous example and is successful in reaching a final total of 245 for each person. However, the final step of stating the number of beads given to Sharon is omitted.

Mark awarded = 2

Candidate M

7 Kay has 325 beads.
 Sharon has 165 beads.
 Kay gives Sharon some beads.
 They now have the same number of beads.

How many beads does Kay give Sharon?

$325 - 165 = 160$

~~325~~ 325 $490 \div 2 = 285$

$165 -$ $\frac{165}{490}$

160 $\frac{165}{490}$

Answer ... 160 (3 marks)

This candidate uses two methods, but marks are awarded for correct steps in either method.

Initially the candidate subtracts 165 from 325 to correctly obtain 160. The candidate then restarts by adding 165 to 325 to obtain the total number of beads, 490. This is followed by an attempt to divide by 2. The arithmetic in the calculation is incorrect. Finally, the candidate gives 160 as the answer.

Mark awarded = 2

Candidate N

7 Kay has 325 beads.
 Sharon has 165 beads.
 Kay gives Sharon some beads.
 They now have the same number of beads.

How many beads does Kay give Sharon?

~~325~~ $325 - 55 = 270$

$165 + 55 = \del{215} 220$

$270 - 25 = 245$

$215 + 25 = \del{240} 245$

Answer 80 beads (3 marks)

This candidate used the strategy of adding and subtracting equal values to balance the number of beads. The candidate then deduced the correct answer.

Mark awarded = 3

Question 8

8 (b) The numbers in this different sequence decrease by the same amount each time.

26 6

What are the **three** missing numbers? (2 marks)

Mark scheme:

8(b)	(26 – 6) ÷ 4 or 5 seen	M1	or their difference ÷ 4
	21, 16, 11	A1	Any order

This question was targeted at grade F and assessed AO3.

Many correct answers were given (over 66% of candidates) and a mean mark of 1.35 out of 2 was achieved.

The most common strategy was to use trial and improvement.

Candidate O

8 (b) The numbers in this different sequence decrease by the same amount each time.

26 21 16 11 6

What are the **three** missing numbers?

$26 - 6 = 20$ $20 \div 5$

Answer 21 , 16 , 11 (2 marks)

This candidate correctly works out the difference between the given terms as 20. $20 \div 5$ could be an attempt to verify that gaps of 5 give 4 steps, as marked on the sequence. The correct answer is then given leading to full marks.

Mark awarded = 2

Candidate P

8 (b) The numbers in this different sequence decrease by the same amount each time.

26 21 16 11 6

What are the **three** missing numbers?

..... $26 - 8 = 18$ $26 - 4 = 22$ $26 - 5 = 21$

..... $18 - 8 = 10$ $22 - 4 = 18$ $21 - 5 = 16$

..... $10 - 8 = 2$ $18 - 4 = 14$ $21 - 5 = 16$

.....

Answer21.....,16.....,11..... (2 marks)

This was a typical solution using trial and improvement. The candidate tried a gap of 8 then 4 then 5 - the correct amount.

Mark awarded = 2

Candidate Q

8 (b) The numbers in this different sequence decrease by the same amount each time.

26 6

What are the **three** missing numbers?

$26 - 6 = 20$ $26 - 8 = 18$ $26 - 4 = 22$

$20 - 6 = 14$ $18 - 8 = 10$ $22 - 4 = 18$

$14 - 6 = 8$ $10 - 8 = 2$ $18 - 4 = 14$

$26 - 5 = 21$ $14 - 4 = 10$

$21 - 5 = 16$

$16 - 5 = 11$

$11 - 5 = 6$

Answer 16 , 11 , 6 (2 marks)

This shows another trial and improvement solution. The candidate tried 6 then 8 then 4 then identifies 5 as the correct difference. However, the solution is then given as 16 11 6, omitting the second term.

Mark awarded = 1

Candidate R

8 (b) The numbers in this different sequence decrease by the same amount each time.

26 21 16 11 6

What are the **three** missing numbers?

~~20~~ ~~14~~

.....

.....

.....

.....

Answer 20 , 14 , 8 (2 marks)

This candidate shows a correct strategy and the correct answer. However, this is then replaced with an incorrect answer without any working for that shown. Consequently, this is not awarded any marks.

Mark awarded = 0

Question 11

- 11 I am thinking of a number.
Two-thirds of the number is 60.

What is $1\frac{1}{2}$ times the number? (3 marks)

Mark scheme:

11	$60 \times 3 \div 2$ or 90 seen	M1	oe
	their $90 \times 3 \div 2$	M1dep	oe
	135	A1	

This question was targeted at grade E and assessed AO3, which proved challenging for many candidates.

Common errors included working out two-thirds of 60 or multiplying 60 by $1\frac{1}{2}$, but then stopping at 90.

The mean mark was only 0.7 out of 3. Although 20% of candidates scored at least 2 marks, over half of the candidates failed to score.

Candidate S

11 I am thinking of a number.
Two-thirds of the number is 60.

What is $1\frac{1}{2}$ times the number?

$\frac{2}{3}$ of 90 is 60 & half of 90 =
~~45~~ \neq 90 ~~40~~ ~~90~~
 135

Answer 135 (3 marks)

This candidate gave a correct solution.

Mark awarded = 3

Candidate T

11 I am thinking of a number.
Two-thirds of the number is 60.

What is $1\frac{1}{2}$ times the number?

~~60~~ $\div 3 = 20 \times 2 = 40$ 90
~~40~~ $\times 1\frac{1}{2} = 80 + 10 = 90$ ~~90~~ $90 \times 1\frac{1}{2} =$
 180 + 45 = 225

Answer ~~90~~ 225 (3 marks)

This candidate states 90, but then writes the correct method, however the arithmetic of $90 \times 1\frac{1}{2}$ is incorrect.

Mark awarded = 2

Candidate U

11 I am thinking of a number.
Two-thirds of the number is 60.

What is $1\frac{1}{2}$ times the number?

$60 \div 3 = 20$ $\frac{2}{3} = 40$

$40 \times 1\frac{1}{2} = 40$

$40 + \frac{1}{2} = 20$

Answer 60 (3 marks)

This candidate appears to misread the question, using 60 as the original number.

$\frac{2}{3}$ of 60 is calculated then multiplied by $1\frac{1}{2}$ again to get back to 60.

Mark awarded = 0

Candidate V

11 I am thinking of a number.
Two-thirds of the number is 60.

What is $1\frac{1}{2}$ times the number?

$\frac{2}{3} = 60$ $\frac{3}{3} = 90$ $1\frac{1}{2} = 90 + 45 = 135$

Answer 135 (3 marks)

This candidate gives a fully correct solution. The working is very clear, showing $\frac{2}{3} = 60$, so $\frac{3}{3} = 90$ and $1\frac{1}{2} \times 90$.

Mark awarded = 3

Question 14

- 14** Two teachers and 18 students go the theatre.
 The cost of a student's ticket is half of the cost of a teacher's ticket.
 The total cost of the tickets is £132.

Work out the cost of one student's ticket. (3 marks)

Mark scheme:

14	$2x + 2x + 18x$ or $x + x + 9x$ (= 132)	M1	oe or for 1 st trial eg $2 \times 8 + 18 \times 4 = 88$
	$22x = 132$ or $11x = 132$	M1	oe or for 2 nd improved trial eg $2 \times 10 + 18 \times 5 = 110$
	6	A1	
	alternative method		
	$2 + 9$ or $4 + 18$	M1	
	$132 \div \text{their } 11$ or $132 \div \text{their } 22$	M1 dep	
	6	A1	

This question was targeted at grade D and assessed AO3. This proved to be a challenging question for many candidates.

The most common approach was to use trail and improvement. Using this method, candidates often used the same ticket price for both students and teachers, so division of 132 by 20 was seen.

Few candidates used an algebraic approach, which is probably the most efficient method.

The mean mark was only 0.54 out of 3 with only 17% of candidates scoring full marks.

Candidate W

14 Two teachers and 18 students go to the theatre.
 The cost of a student's ticket is half of the cost of a teacher's ticket.
 The total cost of the tickets is £132.

Work out the cost of one student's ticket.

2 teachers = £24 = £12 per teacher
 18 = 6

6	50	48	= £108
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£24 + £108 = £132

Answer £ 6 (3 marks)

This candidate gives a fully correct answer. The method appears to be trial and improvement, with the first trial being successful.

Mark awarded = 3

Candidate X

14 Two teachers and 18 students go to the theatre.
 The cost of a student's ticket is half of the cost of a teacher's ticket.
 The total cost of the tickets is £132.
 Work out the cost of one student's ticket.

.....

..... $18 = S$ $2 = T$ $£132$

..... $132 \div 20 = 6 \text{ r } 12$

.....

..... 130 $1 \rightarrow 20$ $2 \rightarrow 30$ $3 \rightarrow 40$ $4 \rightarrow 50$ $5 \rightarrow 60$ $6 \rightarrow 70$ $7 \rightarrow 80$ $8 \rightarrow 90$ $9 \rightarrow 100$ $10 \rightarrow 110$ $11 \rightarrow 120$ $12 \rightarrow 130$

..... $£6.12$ $120 - 18 = 132$

.....

..... Answer £ 6.12 (3 marks)

This candidate incorrectly used the same price for all tickets, working out $132 \div 20$. This was a common error.

Mark awarded = 0

Candidate Y

14 Two teachers and 18 students go to the theatre.
 The cost of a student's ticket is half of the cost of a teacher's ticket.
 The total cost of the tickets is £132.

Work out the cost of one student's ticket.

$20 \div 132 = 13.20 \div 2 = \cancel{67.10} 6.60$

Two teachers equal 4 students.

$4 + 18 = 22$ student prices.

$22 \ 132 \cancel{7} \div 22 = \cancel{7}$

$132 \div 2 = 66 \ .66 \div 11 = 33 \div 5.5 = \ 86$

$33 \cancel{7} - 1.15 = 2.15 \times 4 = 8.60 \times 22 =$

Answer £ 8.60 (3 marks)

This candidate used the strategy that 2 teachers = 4 students, 4 + 18 = 22 student prices. The correct method of $132 \div 22$ is then shown and a method of reducing the calculation, effectively by cancelling fractions, is used. Errors are then made with the arithmetic.

Mark awarded = 2

Candidate Z

14 *make that = 4 students* Two teachers and 18 students go to the theatre.
 The cost of a student's ticket is half of the cost of a teacher's ticket.
 The total cost of the tickets is £132.

Work out the cost of one student's ticket.

$\frac{132}{22}$ $22 \overline{)132}$ 22, 44, 66, 88, 100, 122,
 £6 Per student | 12, 24, 36, 48, 60, ~~72~~, 84,
 £12 Per teacher | 96, 108, 120, 132.
 6, 12, 18, 24, 30, 36, 42, 48,
 54, 60, 66, 72, ~~78~~, 84, 90,
 96, 102, 108, 114, 120, 124
 132.

Answer £ 6 (3 marks)

This candidate uses the same strategy as in the previous example of 2 teachers = 4 students. The candidate lists multiples of 22 to work out $132 \div 22$ and obtains the correct answer from a correct method.

Mark awarded = 3

Candidate AA

14 Two teachers and 18 students go to the theatre.
 The cost of a student's ticket is half of the cost of a teacher's ticket.
 The total cost of the tickets is £132.

$$\begin{array}{r} 006 \\ 22 \overline{) 132} \end{array}$$

Work out the cost of one student's ticket.

$$\begin{array}{r} 132 \\ - 22 \\ \hline 110 \\ \times 10 \\ \hline 1100 \\ - 022 \\ \hline 088 \end{array}$$

$18 + 2 = 20$, teachers pay double
 $20 + 2 = 22$.
 $132 \div 22 = 6$ $6 \times 2 = 12$.

22 £12.00 = teacher
 66 £6.00 = student.

22

$$\begin{array}{r} 44 \\ - 22 \\ \hline 22 \end{array}$$

Answer £ 6.00 (3 marks)

2 2

This candidate also uses the same strategy as on previous examples of 2 teachers = 4 students.

$132 \div 22$ is worked out at the top right of the page and is then checked by continued subtraction on the left hand side. This is an answer that is clearly worthy of the full 3 marks.

Mark awarded = 3