

# General Certificate of Secondary Education 

 November 2010Mathematics
43053H
Higher
Module 3

## Final

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## The following abbreviations are used on the mark scheme:

M Method marks awarded for a correct method.
M dep $\quad$ A method mark which is dependent on a previous method mark being awarded.

A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
oe $\quad$ Or equivalent.

| 1 | $240 \div 100 \times 1.3(=3.12)$ | M1 | $240 \times 0.013$ or sight of 1.013 |
| :--- | :--- | :---: | :--- |
|  | $240+$ their 3.12 | M1 dep | $240 \times 1.013$ gets M2 |
|  | 243.12 | A1 |  |


| 2 a | $784 \times 0.425$ | M1 | $784 \times 42.5(=33320)$ |
| :---: | :--- | :---: | :--- |
|  | 333.20 | A1 | Do not accept 333.2 |
| 2 b | $154 \div$ their time | M1 |  |
|  | $154 \div 3.5$ or $154 \div 3 \frac{1}{2}$ | M1 | oe $154 \div 210 \times 60$ |
|  | 44 | A1 |  |


| 3 | $\frac{3}{4} \times 140$ | M1 | oe |
| :--- | :--- | :--- | :--- |
| $0.15 \times 8 \times 60$ | M1 | oe |  |
|  | A1 |  |  |
|  | 33 | A1 |  |


| 4a | $\left(x^{2}+\right) x^{2}+5 x$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $2 x^{2}+5 x$ | A1 | Condone $x(2 x+5)$ |
| 4b | $2 a(3 a+5)$ | B2 | B1 for $2\left(3 a^{2}+5 a\right)$ or $a(6 a+10)$ |


| 5 | $800 \div(2+7+11)$ | M1 | $800 \div 20(=40)$ |
| :---: | :--- | :---: | :--- |
|  | Any one of $2,7,11 \times$ their 40 | M1 dep |  |
|  | $80,280,440$ | A1 | SC2 correct answers in wrong order |


| 6 | $6 \times 12+5$ | M1 | 77 |
| :--- | :--- | :---: | :--- |
|  | their $77 \times 2.54$ | M1 dep |  |
|  | No and 1.955 or 1.9558 <br> or 1.956 or 1.96 or 195.5 <br> or 195.58 or 195.6 or 196 | A1 | SC2 No and 198 (.12) <br> Yes and 192.7 or 1.927 <br> Yes and 192.5 or 1.925 <br> SC1 one of these numbers with no <br> decision or incorrect decision |
| Alternative method |  |  |  |
| $6 \times 12+5$ | M1 | 77 |  |
| $195 \div 2.54$ | M1 |  |  |
| No and 77 and $76.7(\ldots)$ <br> or 76.8 | A1 |  |  |


| 7 | 0.51 or 0.03 | M1 |  |
| :--- | :--- | :---: | :--- |
|  | their $0.51+$ their 0.03 | M1 dep | $5.4 \times 10^{-1} \quad 0.54$ |
|  | $27 \div$ any mass | M1 |  |
|  | 50 | A 1 |  |


| 8a | $y=k x^{3}$ | M 1 | oe |
| :---: | :--- | :---: | :--- |
|  | $224 \div 4^{3}(=k)$ | M 1 | $224 \div 64(=3.5)$ <br> If this is first line award M2 |
|  | $y=3.5 x^{3}$ | A 1 | oe <br> Allow $k=3.5$ if first M1 awarded |
| 8b | $\frac{1792}{\text { their } 3.5}$ | M 1 | $\sqrt[3]{512}$ <br> $x^{3}=512$ |
|  | 8 | A 1 ft |  |


| 9 | 11.5 or 12.5 or 0.515 or 0.525 | B1 | Condone $12.4 \dot{9}$ or $12.499(\ldots)$ <br> or $0.524 \dot{9}$ or $0.52499(\ldots)$ |
| :--- | :---: | :---: | :--- |
|  | their min rail $\div$ their max dress | M1 | their max dress $\times 22$ |
| $11.5 \div 0.525$ <br> or $11.5 \div 0.524 \dot{9}$ <br> or $11.5 \div 0.52499(\ldots)$ | A1 | $0.525 \times 22$ <br> or $0.524 \dot{9} \times 22$ <br> or $0.52499(\ldots) \times 22$ |  |
| No with $21.9(\ldots)(<22)$ | A1 | No with 11.55 and 11.5 seen <br> For 11.55 accept in range <br> 11.549 to 11.55 |  |


| 10 | Any two of 40,5 and 20 | M1 | $\frac{200}{20}$ |
| :---: | :--- | :---: | :---: |
|  | 10 or 10.2 or 10.25 or 10.3 | A1 | oe |


| 11 | $4.6 \times 1.7$ seen or attempted | M1 | $46 \times 17$ seen |
| :---: | :--- | :---: | :--- |
|  | 7.82 | A1 |  |
|  | 11.02 | A1 ft | SC2 13.26 <br> SC1 digits 1326 |


| 12a | 0 | B1 |  |
| :---: | :--- | :---: | :--- |
| 12 b | All their points plotted $\pm \frac{1}{2}$ square | B1 ft | If table blank, mark on 6 given <br> points |
|  | Points plotted within $\frac{1}{2}$ square <br> joined by smooth curve | B1 | At least 6 points |


| 13 a | $7^{9}$ | B1 |  |
| :--- | :--- | :--- | :--- |
| 13 b | $7^{6}$ | B1 |  |


| $14 a$ | 17 and 71 or 37 and 73 <br> or 79 and 97 | B1 |  |
| :---: | :--- | :---: | :--- |
| 14 b | 7 or 13 is a factor of 91 | B1 | $7 \times 13=91$ <br> Do not accept '91 has other factors' |


| 15 | $3 \frac{2}{5} \times 2 \frac{3}{4}$ | M 1 |  |
| :---: | :--- | :---: | :--- |
|  | $\frac{17}{5}$ and $\frac{11}{4}$ attempted with at <br> least 1 correct with both improper | M1 | 3.4 and 2.75 <br> Conversion to decimals with at least <br> 1 correct |
| $\frac{187}{20}$ | A1 | 9.35 oe |  |
| $9 \frac{7}{20}$ | A1 ft | oe ft mixed number from improper <br> fraction <br> dep on M2 |  |


| 16a | $x^{2}-5 x+3 x-15$ | M1 | Allow one error <br> Must see $x^{2}$ and have four terms |
| :---: | :--- | :---: | :--- |
|  | $x^{2}-2 x-15$ | A1 |  |
| 16 b | $(x-3)(x+3)$ | B1 | Either order |


| 17 | $4 \div 11=0.3 \ldots$ | M1 |  |
| :---: | :--- | :--- | :--- |
|  | $0 . \dot{3} \dot{6}$ | A1 |  |


| 18 a | $2(\times) 210$ | M1 | Product with at least 1 prime |
| :---: | :--- | :---: | :--- |
|  | $2(\times) 2(\times) 3(\times) 5(\times) 7$ | A1 | Can be on factor tree |
|  | $2^{2} \times 3 \times 5 \times 7$ <br> A1 and 210 <br> or 30 and 140 <br> or 60 and 70 | B2 | 20 and 30 <br> or 20 and 70 <br> or 30 and 70 <br> B1 |


| 19a | $\sqrt{60}$ | M1 | $\begin{aligned} & \sqrt{2}(\times) \sqrt{5}(\times) \sqrt{2}(\times) \sqrt{3} \\ & \text { or } 4(\times) \sqrt{3}(\times) \sqrt{5} \text { or } \sqrt{4 \times 15} \\ & \text { or } 2(\times) \sqrt{5}(\times) \sqrt{3} \\ & \text { or } \sqrt{4}(\times) \sqrt{15} \end{aligned}$ |
| :---: | :---: | :---: | :---: |
|  | $2 \sqrt{15}$ | A1 |  |
| 19b | $\frac{3 \sqrt{2}}{2}$ | B1 | Accept 1.5 $\sqrt{2}$ |
| 19c | $\sqrt{13}$ | B1 |  |
|  | $(7 \times 2)^{\frac{1}{2}}$ or $14^{\frac{1}{2}}$ | M1 | Indicates $8^{\frac{1}{3}}=2$ |
|  | $\sqrt{13}$ and $\sqrt{14}$ and B | A1 |  |
| 19d | $2^{-6}$ | B3 | B2 $\left(2^{4}\right)^{-\frac{3}{2}}$ or $\left(2^{-2}\right)^{3}$ or $\left(2^{-12}\right)^{\frac{1}{2}}$ or $2^{6}$ <br> B1 $16=2^{4}$ or $(16)^{-\frac{3}{2}}$ or $4^{-3}$ or $2^{12}$ or $2^{-12}$ or changes denominator to $4^{3}$ or 64 or $\sqrt{4096}$ or $16^{\frac{3}{2}}$ |

