

# General Certificate of Secondary Education 

## Mathematics 4307 Specification B

Module 5 Paper 2 Tier H 43055/2H

## Final

## Mark Scheme

2010 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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## The following abbreviations are used on the mark scheme:

M $\quad$ Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
E Marks awarded for an explanation.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
oe
Or equivalent.

MODULE 5 HIGHER TIER
43055/2H

| 1(a) | 16 | B1 |  |
| :---: | :--- | :---: | :--- |
| $1(\mathrm{~b})$ | $9.30+1(\mathrm{~h})(=10.30)$ | M1 | Point $(10.30,24)$ identified |
|  | $24 \div 12(=2)$ | M1 | Draws line of negative gradient <br> representing speed of $12 \mathrm{~km} / \mathrm{h}$ |
|  | 12.30 | A1 | oe SC2 11.30 |


| 2 | All 9 correct |  |  |
| :---: | :--- | :--- | :--- |
| $(\checkmark$ | $\times$ | $\checkmark$ |  |
| $\checkmark$ | $\checkmark$ | $\times$ |  |
| $\checkmark$ | $\times$ | $\checkmark$ | B3 |
| $\times$ | $\times$ | $\times$ | 6,7 or 8 correct B2 |
|  | 3,4 or 5 correct B1 |  |  |


| 3 | No and 6(.183) $(x=2.7)$ and <br> $7(.952)(x=2.8)$ | B2 | B1 for at least one correct <br> evaluation using $2.7 \leq x \leq 2.8$ |
| :---: | :--- | :---: | :--- |


| 4 | One correct area product seen | M1 | eg $12 \times 3(=36)$ or $10 \times 8(=80)$ |
| :---: | :--- | :--- | :--- |
|  | All rectangle calculations correct <br> and addition or subtraction shown <br> $12 \times 3+8 \times 2(=36+16)$ |  |  |
| $11 \times 2+10 \times 3(=22+30)$ | M1 | $12 \times 3+11 \times 2-3 \times 2$ <br> $(=36+22-6)$ <br> $10 \times 3+3 \times 2+8 \times 2$ <br> $(=30+6+16)$ |  |
| $12 \times 11-10 \times 8(=132-80)$ |  |  |  |
| 52 | A1 |  |  |


| $5(\mathrm{a})$ | Line from $(0,10)$ to $(2,10)$ | B1 | Allow if intention is clear |
| :---: | :--- | :--- | :--- |
| $5(\mathrm{~b})$ | Line from $(0,8)$ to $(2,0)$ | B1 | Allow if intention is clear |


| 6(a) | 37 | B1 |  |
| :---: | :--- | :---: | :--- |
|  | Alternate (angles) | B1 | Do not allow alternate segment |
| 6 6(b) | $180-79$ | M1 |  |
|  | 101 | A1 |  |


| 7 7(a)(i) | $180^{\circ}$ | B1 |  |
| :---: | :--- | :---: | :--- |
|  | (Centre) $P$ | B1 |  |
| 7 (a)(ii) | Correct line drawn | B1 | Allow if intention is clear |
| $7(\mathrm{~b})$ | Correct shape with vertices <br> $(4,6)(4,7)(3,7)(3,8)(6,8)$ <br> $(6,7)(5,7)(5,6)$ | B2 | B1 if $D$ is translated by $\binom{5}{-2}$ |


| 8 | 2 arcs, equal radii, centre $B$, <br> cutting $A B$ and $B C$ | M1 | 1 arc, centre $B$, cutting $A B$ and $B C$ |
| :---: | :--- | :---: | :--- |
|  | 2 arcs, equal radii, centres at <br> intersections of arc(s) with $A B$ <br> and $B C$ and bisector drawn | A1 |  |


| 9(a) | $3(2 a+3)$ | B1 | $1(6 a+9)$ is B0 |
| :---: | :--- | :---: | :--- |
| $9(\mathrm{~b})$ | $8 p+4+6-3 p$ | M1 | 4 terms with 3 correct including <br> signs |
|  | $5 p+10$ | A1 |  |
| 9(c)(i) | -2 | B1 |  |
| 9(c)(ii) | 4 | B1 |  |
| 9(d) | $m^{2}+2 m+2 m+4\left(-m^{2}-4\right)$ | M1 | oe |
|  | $4 m$ | A1 |  |


| $10(\mathrm{a})$ | $12 y \div 4(=3 y)$ | M1 | oe |
| :---: | :--- | :---: | :--- |
|  | $9 y^{2}$ or $(3 y)^{2}$ or $3 y \times 3 y$ | A1 | Penalise further work by subtracting <br> 1 mark |
| $10(\mathrm{~b})$ | $2 g+\frac{79}{100} h$ or $2 g+0.79 h$ <br> or $\frac{200 g+79 h}{100}$ | B2 | B1 for one term correct or <br> B1 for $200 g+79 h$ |
| $10(\mathrm{c})$ | $6 a^{4} b^{3}$ | B2 | B1 for 2 out of 3 parts correct <br> Must be 3 components <br> SC1 $a^{4} b^{3}$ |
| $10(\mathrm{~d})$ | $(6 x)^{2}=2 w+y$ | M1 | Condone invisible brackets |
|  | their $(6 x)^{2}-y(=2 w)$ | M1 dep | oe |
|  | $\frac{36 x^{2}-y}{2}=w$ | oe eg $\frac{(6 x)^{2}-y}{2}=w$ |  |
| or $w=18 x^{2}-\frac{1}{2} y$ |  |  |  |
| Must have $=w$ or $w=$ |  |  |  |


| 11 | $7.8 \div 1.2(=6.5)$ | M1 | $1.2 \div 7.8(=0.15(\ldots))$ |
| :---: | :--- | :---: | :--- |
|  | $16.9 \div$ their 6.5 | M1 dep | their $0.15(\ldots) \times 16.9$ |
|  | 2.6 | A1 |  |
|  | Alternative method |  |  |
| $16.9 \div 7.8$ <br> $(=2.16(\ldots)$ or 2.17 or 2.2$)$ | M1 | $7.8 \div 16.9(=0.46(\ldots))$ |  |
| their $2.16(\ldots) \times 1.2$ | M1 dep | $1.2 \div$ their $0.46(\ldots)$ |  |
|  | 2.6 | A1 |  |


| 12(a) | Evidence of attempt to find <br> gradient | M1 | eg <br> triangles on graph or $2: 1$ or $\frac{4}{2}$ |
| :--- | :--- | :---: | :--- |
|  | (gradient of) -2 | A1 | A1 |
|  |  | oe eg $y+2 x=-1$ or $y+2 x+1=0$ <br> Must be an equation <br> SC2 $-2 x-1$ <br> SC2 $y=-m x-1 \quad(m>0)$ <br> SC1 $y=m x-1 \quad(m>0)$ |  |
| $12(b)$ | $\frac{1}{2}$ | oe <br> Correct or ft <br> Must be a numerical answer, not an <br> equation <br> ft their gradient in (a) <br> Condone $\frac{1}{8}$ |  |


| $13(\mathrm{a})$ | $4^{2}+7.5^{2}(=16+56.25=72.25)$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $\sqrt{\text { their } 72.25}$ | M1 dep |  |
|  | 8.5 | A1 | oe |
| $3(\mathrm{~b})$ | $\pi \times 4 \times$ their 8.5 | M1 | 106.76 to 106.828 inclusive |
|  | 106.8 or 110 or 107 or $34 \pi$ | A1 ft | ft their 8.5 to 1 dp or 2 sf or 3 sf |

$\left.\begin{array}{|l|l|l|l|}\hline 14(\mathrm{a}) & \frac{1}{2}(2 x+4)(x+2+2 x-3) & \text { M1 } & \begin{array}{l}\frac{1}{2}(2 x+4)(3 x-1) \\ \text { or }(x+2)(3 x-1) \\ \text { or }\left(\frac{3 x}{2}-\frac{1}{2}\right)(2 x+4) \\ \text { Condone missing brackets }\end{array} \\ \hline & \begin{array}{l}\text { Expands their brackets obtaining } \\ 4 \text { terms with at least } 3 \text { correct } \\ \left.\text { (one term must be in } x^{2}\right)\end{array} & \text { M1 } & \begin{array}{l}\text { If correct } \frac{1}{2}\left(6 x^{2}-2 x+12 x-4\right) \\ \text { or } 3 x^{2}-x+6 x-2\end{array} \\ \hline \begin{array}{l}3 x^{2}-x+6 x-2=20 \\ \text { or } \frac{1}{2}\left(6 x^{2}-2 x+12 x-4\right)=20\end{array} & \text { A1 } & \begin{array}{l}\text { All } 4 \text { terms of the expansion correct } \\ \text { and made into a correct equation } \\ \text { Do not accept the printed equation } \\ \text { without seeing where it came from }\end{array} \\ \hline 14(b) & \text { M1 } & \begin{array}{l}-5 \pm \sqrt{5^{2}-4 \times 3 \times-22} \\ 2 \times 3\end{array} \\ \hline(3 x+11)(x-2) & \text { A1 } & \begin{array}{l}\text { Allow one numerical or sign error } \\ \text { for M1 } \\ \text { Fully correct for A1 }\end{array} \\ \hline & \text { A1 } & \text { with } a b=22 & \text { B1 ft }\end{array} \begin{array}{l}\text { ft } 10 x+6 \text { evaluated correctly for } \\ \text { their positive value of } x \\ \text { SC1 } 10 x+6 \text { seen if M1 not } \\ \text { awarded }\end{array}\right]$

| $15(\mathrm{a})$ | $4 \mathbf{a}$ | B1 | $\frac{2}{3}(6 \mathbf{a})$ is B0 |
| :--- | :--- | :---: | :--- |
| $15(\mathrm{~b})$ | $-3 \mathbf{a}+\mathbf{b}+\ldots$ or $-3 \mathbf{a}+\mathbf{b}-\ldots$ | M1 | $(\overrightarrow{A N}=) \frac{1}{2}$ their 4a <br> Must be processed to $k \mathbf{a}$ where $k$ is a <br> number |
|  | $-3 \mathbf{a}+\mathbf{b}+\frac{1}{2}$ their $4 \mathbf{a}$ | M1 dep | $\frac{1}{2}$ their $4 \mathbf{a}$ must be processed to $k \mathbf{a}$ <br> where $k$ is a number |
|  | $-\mathbf{a}+\mathbf{b}$ | A1 ft | ft their 4a <br> SC1 Answer only $5 \mathbf{a}+\mathbf{b}$ |


| 16(a) | $\frac{17}{6}$ or $2.83(\ldots)$ | B1 | oe $17 \div 6$ is B 0 |
| :---: | :---: | :---: | :---: |
| 16(b) | $(x=) 70.6$ or 71 | B1 | $(A=) 19.4$ or 19 |
|  | $\begin{array}{r} (B D C=) 180-45-\text { their } 70.6 \\ (=64.4) \end{array}$ | M1 | $\begin{array}{r} (B D A=) 180-45-\text { their } 19.4 \\ (=115.6) \\ \hline \end{array}$ |
|  | $\frac{B D}{\sin \text { their } 70.6}=\frac{6}{\sin \text { their } 64.4}$ | M1 dep | $\frac{B D}{\sin \text { their } 19.4}=\frac{17}{\sin \text { their } 115.6}$ |
|  | $B D=\frac{6 \times \sin \text { their } 70.6}{\sin \text { their } 64.4}$ | M1 dep | $B D=\frac{17 \times \sin \text { their } 19.4}{\sin \text { their } 115.6}$ |
|  | 6.15 to 6.32 inclusive | A1 |  |

