

# General Certificate of Secondary Education 

## Mathematics 4307 Specification B

Module 3 Tier H 43053H

## Final

## Mark Scheme

2010 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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## The following abbreviations are used on the mark scheme:

M $\quad$ Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
E Marks awarded for an explanation.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.

ое
Or equivalent

MODULE 3 HIGHER TIER
43053H

| 1(a) | $948 \div 6$ | M1 |  |
| :--- | :--- | :--- | :--- |
| 1(b) | 158 | A1 | $158: 948$ M1 A0 |
|  |  | B2 | B1 their $\frac{158}{2}: 948$ <br> B1 $1: 12$ not in simplest form <br> eg $\frac{1}{2}: 6$ |


| 2 | $\frac{100}{7}$ | M1 | oe |
| :--- | :--- | :---: | :--- |
| 14.2 to 14.3 inclusive | A 1 | $14 \frac{2}{7}$ |  |
| their $14.2 \ldots / 0.44$ | M1 dep |  |  |
| 32 to 33 inclusive and yes | A 1 ft | oe to saying 'yes' |  |
| Alternative method 1 |  |  |  |
| $30 \times 0.44$ | M 1 |  |  |
| 13.2 | A 1 |  |  |
| $\frac{100}{7}$ | M 1 | oe |  |
| 14 to 14.3 inclusive and yes | A 1 ft | oe to saying 'yes' |  |
| Alternative method 2 |  |  |  |
| $30 \times 0.44$ | M 1 |  |  |
| 13.2 | A 1 |  |  |
| their $13.2 \times 7$ | M1 dep |  |  |
| 92.4 and yes | A1 ft | oe to saying 'yes' |  |


| 3 | $50(\times) 2$ or $25(\times) 2(\times) 2$ <br> or $10(\times) 5(\times) 2$ <br> or $5(\times) 5(\times) 4$ <br> or $5(\times) 20$ | M1 | Allow on factor trees or repeated <br> division <br> Condone use of $\times 1$ |
| :---: | :--- | :---: | :--- |
| $2(\times) 2(\times) 5(\times) 5$ | A1 | A1 ft | Allow dots for $\times$ but no other <br> alternatives <br> ft only with prime factors and after <br> M1 awarded |
| $2^{2} \times 5^{2}$ |  |  |  |


| 4(a) | $0.17 \times 800(=136)$ | M1 | oe |
| :---: | :--- | :---: | :--- |
|  | $800-$ their 136 | M1 dep | M2 $0.83 \times 800$ or $83 \times 8$ |
|  | 664 | A1 |  |
| 4(b)(i) | 265 | B1 |  |
| 4(b)(ii) | 274 | B1 | SC1 numbers wrong way around in <br> parts (b)(i) and (b)(ii) |


| $5($ a) | -11 (is wrong and) should be 30$11(x)$ (is wrong and) should <br> be $-11(x)$ | B1 | oe Accept should be 30 |
| :---: | :--- | :---: | :--- |
| $5(\mathrm{~b})$ | 5 and 6 have no common factors <br> and $x$ and $y$ have no common <br> factors | B1 | Must reference numbers and letters <br> oe |


| $6(\mathrm{a})$ | $4.35 \times 10^{8}$ | B1 |  |
| :---: | :--- | :---: | :--- |
| $6(\mathrm{~b})$ (i) | $757.69848 \ldots$ | B1 | 757.69849 |
| $6(\mathrm{~b})$ (ii) | 760 | B1 ft | ft figure having at least 3 sf <br> Correct or ft |


| 7(a)(i) | Greater than 5 | B1 | oe Accept (they are) increasing |
| :---: | :--- | :---: | :--- |
| 7 7(a)(ii) | Less than -7 | B 1 | oe |
| 7(b) | Smooth curve through points | B 1 |  |
| 7 7(c) | Attempts to subtract or difference <br> the two quadratics | M 1 | $(y=) \pm x \pm 2$ |
|  | Draws the line $y=x+2$ to at least <br> the two crossing points | A 1 |  |
|  | Reads off their two answers <br> $\left(+/-\frac{1}{2}\right.$ small square $)$ | A 1 ft | ft if M1 awarded but must have two <br> answers |


| 8 | $T=\frac{200}{N}$ <br> or $k=200$ and $T=\frac{k}{N}$ (oe) seen | B3 | oe <br> B2 for <br> $T \propto \frac{200}{N}$ or $k=200$ <br> but $\quad T=\frac{k}{N}$ (oe) not seen <br> or $k=25 \times 8$ or $\frac{k}{8}=25$ oe B1 for $T \propto \frac{1}{N}$ or $T=\frac{k}{N}$ oe or $25 \times 8$ or 200 or $k \propto 200$ |
| :---: | :---: | :---: | :---: |


| 9 | $28400 \div 0.48$ <br> $(=59166$ to 59167 inclusive $)$ | M1 | $0.48 \times 0.97(=0.4656)$ oe |
| :---: | :--- | :---: | :--- |
|  | their $59166.666 \ldots \div 0.97$ | M1 dep | $28400 \div$ their 0.4656 oe |
| $[60995,60997]$ | A1 | At least 5 sf shown and correct |  |
| 61000 or 60000 | B1 ft | Accept rounding to 1 sf, 2 sf or 3 sf <br> from previously shown value to at <br> least one more sf |  |


| $10(\mathrm{a})$ | 4 | B1 |  |
| :---: | :--- | :---: | :--- |
| $10(\mathrm{~b})$ <br> (i) | -487 | B1 |  |
| $10(\mathrm{~b})$ <br> (ii) | -24350 | B2 | B1 a negative number with the <br> digits 2435 in right order <br> B1 24350 |


| 11 | At least two of 4, 2 and 0.5 | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $5^{3}$ | A1 |  |
|  | 125 | A1 ft | ft any value over 5 correctly cubed if <br> M1 awarded <br> SC1 27 no working |


| 12(a) | $3 h-12$ | B1 |  |
| :--- | :--- | :---: | :--- |
| $12(\mathrm{~b})$ | $x^{3}+3 x^{2}$ | M1 |  |
|  | $-x^{3}+3 x$ | M1 | Allow one sign error or $-\left(x^{3}-3 x\right)$ |
|  | $3 x^{2}+3 x$ and factorised | A1 | or simplify LHS to $3 x^{2}+3 x$ <br> and multiply out RHS convincingly <br> to same |
| $12(\mathrm{c})$ | $m(m-1)$ | B1 |  |


| $13(\mathrm{a})$ | Appropriate common <br> denominator with at least one <br> correct numerator | M1 | $\frac{6}{15}(-) \frac{5}{15}$ oe |
| :--- | :--- | :--- | :--- |
| $\frac{1}{15}$ | A1 | oe |  |
| $13(b)$ | $\frac{7}{4} \times \frac{7}{5}$ or $1 \frac{3}{4} \times \frac{7}{5}$ | M1 | oe |
|  | $\frac{49}{20}$ | A1 | oe eg $2 \frac{9}{20}$ |


| 14 | $450-400(=50)$ | M1 | $\frac{450}{400}-1(=0.125)$ <br> or $\frac{450}{400} \times 100(=112.5)$ |
| :--- | :--- | :---: | :--- |
|  | $\frac{\text { their } 50}{400} \times 100$ | M1 dep | oe eg $\frac{50}{4}$ <br> their $0.125 \times 100$ <br> or their $112.5-100$ |
| 12.5 | A1 | SC1 sight of or answer of $\frac{1}{8}$ |  |


| $15(\mathrm{a})$ | 1 | B1 |  |
| :---: | :--- | :---: | :--- |
| $15(\mathrm{~b})$ | 2 | B1 ft | $2 \times$ their (a) or correct |
| $15(\mathrm{c})$ | 2 | B1 |  |


| $16(a)$ | $\frac{10}{3} \times \frac{10}{3}$ | B1 | Allow $\left(\frac{10}{3}\right)^{2}$ or $\frac{10^{2}}{3^{2}}$ |
| :--- | :--- | :---: | :--- |
|  | $\frac{100}{9}$ | B1 ft | ft their improper fractions correctly <br> squared |
| $11 \frac{1}{9}$ | B1 ft | ft their improper fraction if either B1 <br> awarded and correct mixed number <br> obtained <br> $\left(11 \frac{1}{9}\right.$ implies B3, $\frac{100}{9}$ implies B2) |  |
|  | M1 | eg $\sqrt{3} \sqrt{2}=\sqrt{3 \times 2}$ or $\sqrt{6}$ <br> Ignore further work in deciding this <br> mark <br> M1 $k=\frac{n^{2}}{2}$ |  |
|  | Any two correct answers and no <br> incorrect answer | A2 | $\frac{1}{2}, 2, \frac{9}{2}, 8, \frac{25}{2} \quad 18, \frac{49}{2} 32, \ldots$ <br> M1 A1 any one correct answer |


| 17(a) | Numerator $=12(\mathrm{and} /$ or -12$)$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $\sqrt[3]{27^{2}}$ or $(\sqrt[3]{27})^{2}$ or $3^{2}$ or 9 | M1 |  |
|  | $\frac{12}{9}$ or $1 \frac{3}{9}$ or $1 \frac{1}{3}$ or $\frac{4}{3}$ | A1 |  |
|  | $1 . \dot{3}$ or $1.3 \ldots$ | B1 ft | SC2 1.3, 1.33 etc no working |
| 17(b) | $3 . \dot{5} \dot{3} \times \frac{1}{10}(=0.3 \dot{5} \dot{3})$ | M1 | oe |
|  | Let $x=0 . \dot{3} \dot{5}$ <br> $100 x=35 . \dot{3} 5$ and attempt to subtract | M1 dep |  |
|  | $\frac{35}{99}$ | A1 | oe |
|  | Alternative method |  |  |
|  | Let $x=3 . \dot{5} \dot{3}$ $100 x=353.5 \dot{3}$ and attempt to subtract | M1 | oe |
|  | $\begin{aligned} & (99 x=350) \\ & x=\frac{350}{99}(\div 10) \end{aligned}$ | M1 dep | oe |
|  | $\frac{350}{990}$ | A1 | oe |

