

# General Certificate of Secondary Education 

## Mathematics 4307 Specification B

Module 1 Tier H 43051H

## Final

## Mark Scheme

2010 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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## The following abbreviations are used on the mark scheme:

M $\quad$ Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
E Marks awarded for an explanation.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
oe
Or equivalent.

| 1(a) | All 7 points plotted correctly <br> $(2,10.5)(3,10.2)(5,8.5)(6,8.1)$ <br> $(7,7)(9,6.1)(10,6.3)$ | B2 | B1 <br> for 5 or 6 plotted correctly $\pm \frac{1}{2} \mathrm{sq}$ <br> Ignore extras |
| :---: | :--- | :---: | :--- |
| 1(b) | The more time spent training, the <br> less time it took to complete the <br> test | B1 | Must mention 'training' and 'test' <br> oe |


| 2(a) | $1<w \leq 2$ | B1 |  |
| :--- | :--- | :---: | :--- |
| 2(b) | One correct midpoint used <br> leading to one correct $f x$ | B1 |  |
|  | $(10 \times 0.5)+(17 \times 1.5)$ <br> $+(3 \times 2.5)+(7 \times 3.5)$ <br> $+(3 \times 4.5)$ <br> or $5+25.5+7.5+24.5+13.5$ <br> or 76 | M1 | Attempt at $\sum f x$ with $x$ 's used on or <br> between the class boundaries for at <br> least 4 products |
|  | their $76 \div 40$ | M1 dep | dep on M1 <br> Accept incorrect $\sum f$ if clear evidence <br> shown of adding the values |
|  | 1.9 | A1 | Allow 2 from correct working seen |


| $3(\mathrm{a})$ | Plotted at upper class boundaries | B1 | Must be increasing graph |
| :--- | :--- | :---: | :--- |
| Heights correct <br> $12,35,56,72,80$ | B1 | $\pm \frac{1}{2}$ square <br> Must be increasing graph |  |
| Curve or straight lines through all <br> their points | B1 | Must be increasing graph <br> Must have at least 4 points to join <br> Ignore line to left of their first point |  |
| 3(b) | Reading off cf graph at 168 with <br> value eg '26' <br> or correct interpolation from table <br> giving <br> $12+14=26 \quad\left(12+\frac{3}{5} \times 23\right)$ | B1 | ft from an increasing graph |
|  | Girls $=40$ | B1 | M1 |
| $40-$ their 26 | A1 ft | Their 26 must be from increasing <br> graph with points joined and an <br> attempt at reading from 167 to 169 <br> inclusive |  |
| from 40 their reading subtracted |  |  |  |
|  | '12' |  |  |


| 4(a) | The numbers of pupils from each <br> year group in the sample are in <br> proportion to the total number of <br> pupils in the year group | B1 | oe |
| :---: | :--- | :--- | :--- |
| $4(b)$ | $(80 \div 10=8$ so $)$ yr $3=96 \div 8$ <br> or $\frac{96}{400} \times 50$ | M1 | or $\frac{96}{80} \times 10$ oe <br> M1 may be implied from one <br> correct answer or correct decimal <br> $(12.625$ or 15.375$)$ providing it is not <br> from a clearly incorrect method |
|  | 12,13 and 15 | A2 | A1 for one correct |


| 5 | $\frac{1}{2} \times \frac{1}{10}$ or $\frac{3}{10} \times \frac{1}{6}$ <br> or $\frac{1}{5} \times \frac{1}{12}$ <br> or $\frac{1}{20}$ or $\frac{3}{60}$ or $\frac{1}{60}$ | One correct product seen <br> Accept decimals <br> $\frac{1}{6}=0.16$ or 0.17 or better |
| :--- | :--- | :--- | :--- |
| $\frac{1}{2} \times \frac{1}{10}$ and $\frac{3}{10} \times \frac{1}{6}$ | M1 dep | $\frac{1}{12}=0.083$ or better <br> and $\frac{1}{5} \times \frac{1}{12}$ <br> or $\frac{1}{20}$ and $\frac{3}{60}$ and $\frac{1}{60}$ <br> or correct totals <br> Decimals <br> 0.05 and 0.05 and 0.016 or better |
| $\frac{1}{20}+\frac{3}{60}+\frac{1}{60}$ | M1 dep | oe Adding three correct products |
| $\frac{7}{60}$ | A1 | oe <br> Accept decimal that rounds to 0.117 <br> to 3 dp or $11.7 \%$ <br> SC2 for $\frac{53}{60}$ |
| or 0.883 arrives on time |  |  |$|$| Accept decimals |
| :--- |
| $\frac{5}{2} \times \frac{9}{10}$ or $\frac{3}{10} \times \frac{5}{6}$ |
| or $\frac{1}{5} \times \frac{11}{12}$ |


| 6 | Teenagers text $=24$ | B1 |  |
| :---: | :--- | :---: | :--- |
|  | Adults text $=6$ | B1 |  |
|  | $60-(30+$ their $6+9)$ | M1 | their 6 must be an integer |
|  | 15 | A1 ft | for integer value only and with <br> telephone $=30$ |


| 7 | $1,2,6,7$ and 9 <br> or 0, 4, 6, 7, 8 in any order | B2 | B1 for 2 conditions met with <br> different single digit numbers <br> eg 1, 3, 6, 7, 9 (mean incorrect) <br> or all conditions met but repeated <br> digit <br> eg 1, 3, 6, 6, 9 |
| :--- | :--- | :--- | :--- |


| 8(a) | $0.15+0.25$ or 0.4 seen (provided no contradiction in box for $p(4)$ ) | M1 | or $15 \%+25 \%$ or $40 \%$ |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 1-(0.15+0.25+0.08+\text { their } \\ & 0.4) \text { or } 1-\text { their } 0.88 \end{aligned}$ | M1 dep | $100-(15+25+8+\text { their } 40)=12$ <br> is awarded M1 M0 A0 |
|  | 0.12 | A1 | If answer 12 must be $12 \%$ $\rightarrow$ M1 M1 A1 |
| 8(b) | 'All equally likely' circled | M1 |  |
|  | Explains that every result is equally likely each throw/or throws independent/or starts again each throw/random | A1 | oe |


| 9(a) | SecondaryDaniel did not collect the data <br> himself/someone else collected <br> the original data | A1 | Not 'He got it off the internet' |
| :---: | :--- | :---: | :--- |
| 9(b) | A hypothesis/question referring to <br> the change in the elephant <br> population numbers | eg Have the number of elephants <br> decreased/increased/stayed the | B1 |
| same (over the last 50 years)? <br> Are the number of elephants <br> decreasing/increasing? <br> Are there more/less elephants <br> now? |  |  |  |


| 10(a) | $\frac{2}{3}$ | B1 |  |
| :---: | :---: | :---: | :---: |
| 10(b) | $\frac{1}{3}$ labelled on all branches where <br> A wins | B1 | oe decimals to 2 dp or better |
|  | $\frac{2}{3}$ labelled on all branches where D wins | B1 | oe |
| 10(c) | $\begin{aligned} & \frac{2}{3} \times \frac{1}{3} \times \frac{2}{3} \text { or } \frac{1}{3} \times \frac{2}{3} \times \frac{2}{3} \\ & \text { or } \frac{4}{27} \end{aligned}$ | M1 |  |
|  | $\begin{aligned} & \left(\frac{2}{3} \times \frac{1}{3} \times \frac{2}{3}\right)+\left(\frac{1}{3} \times \frac{2}{3} \times \frac{2}{3}\right) \\ & \text { or } \frac{4}{27}+\frac{4}{27} \text { or } \frac{4}{27} \times 2 \end{aligned}$ | M1 dep | Allow $\left(\frac{2}{3} \times \frac{1}{3} \times \frac{2}{3}\right) \times 2$ in any order for M2 |
|  | $\frac{8}{27}$ or 0.296 | A1 |  |


| 11 | $1 \mathrm{~cm}^{2}=10$ tomatoes or 1 box $=10$ | M1 | oe $5 \frac{1}{2}+1 \frac{1}{2}=70$ |
| :---: | :---: | :---: | :---: |
|  | $\begin{array}{\|l\|} \hline \text { Over } 130 \\ 3.6 \mathrm{~cm}^{2} \times 10 \end{array}$ | M1 |  |
|  | 36 | A1 |  |
|  | Alternative method 1 |  |  |
|  | 175 small squares $=70$ tomatoes or 2.5 small squares $=1$ tomato | M1 |  |
|  | Over 130 $90 \div 2.5 \text { or } 90 \times \frac{70}{175}$ | M1 |  |
|  | 36 | A1 |  |
|  | Alternative method 2 |  |  |
|  | 1 row of $5=2$ tomatoes | M1 | oe |
|  | $\begin{aligned} & \text { Over } 130 \\ & 18 \times 2 \end{aligned}$ | M1 |  |
|  | 36 | A1 |  |
|  | Alternative method 3 |  |  |
|  | Frequency density every $2 \mathrm{~cm}=1$ oe | M1 | May be marked on axis |
|  | $\begin{aligned} & 20 \times 1.3+50 \times 0.2 \text { or } 26+10 \\ & \text { oe } \end{aligned}$ | M1 |  |
|  | 36 | A1 |  |
|  | Alternative method 4 |  |  |
|  | One bar or part bar correctly labelled with area <br> eg 13 on 130-140 <br> or 2 on 150-160 | M1 |  |
|  | $13+13+2+4+4$ | M1 | oe |
|  | 36 | A1 |  |

