

# General Certificate of Secondary Education 

## Mathematics 4307 Specification B

Module 5 Paper 1 Tier H 43055/1H

## Mark Scheme

2009 examination - November series

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## The following abbreviations are used on the mark scheme:

M $\quad$ Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
$\mathbf{0 e} \quad$ Or equivalent.
eeoo Each error or omission.

| 1 (a) | $5 \times 3 \times 2$ | M1 | $50 \times 30 \times 20$ seen in (a) or (b) |
| :---: | :--- | :---: | :--- |
|  | 30 | A1 |  |
| $1(b)$ | 30000 | B1 ft | $\mathrm{ft}(\mathrm{a}) \times 1000$ |


| 2(a) | Sphere | B1 |  |
| :---: | :--- | :---: | :--- |
| 2(b) | Cuboid <br> Prism <br> Cube | B2 | B1 for 2 or 3 correct <br> (and one incorrect) <br> or B1 for 1 correct <br> (and none incorrect) |


| 3(a) | $2 \pi r$ | B 1 | oe |
| :---: | :--- | :---: | :--- |
| 3 3(b) | $2 \times 3.14 \times 3$ | M 1 | Must be 3.14 |
|  | $18.8(4)$ | A 1 |  |
| 3 (c)(i) | their $18.8(4) \div 4(=4.7(1))$ | M 1 |  |
|  | their $4.7(1)+12$ | M 1 dep | oe <br> their $18.8(4) \div 4+12$ |
|  | $16.7(1)$ | A 1 ft | $1.5 \pi+12$ oe |
| 3(c)(ii) | 90 or 60 seen | B 1 | May be on diagram |
|  | $360-90-60-60$ | M 1 |  |
|  | 150 | A 1 |  |
|  | 30 | A 1 ft | $\mathrm{ft} 180-$ their 150 |


| 4(a) | $\begin{aligned} & \begin{array}{l} \text { length }=) 4 \text { seen } \\ \text { or }(\text { height }=) 8 \text { seen } \end{array} \\ & \hline \end{aligned}$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $4 \times 8$ | M1 dep | $10 \times 8-2 \times 0.5 \times 6 \times 8$ |
|  | 32 | A1 |  |
| 4(b) | $8^{2}+6^{2}$ | M1 |  |
|  | $\sqrt{8^{2}+6^{2}}$ or $\sqrt{100}$ | M1 dep |  |
|  | $10(+10+4+4)$ | A1 |  |
|  | 28 | A1 | SC1 $8+8+3.2+3.2$ or 22.4 |


| 5 5(a) | $5 \times 0.4(-) 4 \times 2.5$ or $2(-) 10$ | M1 | 8 implies M1 |
| :---: | :--- | :---: | :--- |
|  | -8 | A1 |  |
| $5(b)$ | $4 x-28$ | B1 |  |
|  | $7 x-4 x=-28-11$ | M1 | oe <br> for collecting their terms |
|  | -13 | A1 |  |


| 6(a) | Straight sloping line | B1 |  |
| :---: | :--- | :---: | :--- |
| 6(b) | Valid coordinates | B1 | eg $(0,-1)(1,1)(2,3)(3,5)$ |
|  | Different valid coordinates | B1 |  |
| 6 6(c)(i) | $(2.8+1) \div 2$ <br> or $2 x=3.8$ | M1 |  |
|  | 1.9 | A1 | Embedded answer M1A0 |
| 6(c)(ii) | $x<1.9$ | B1 ft |  |


| 7 | Measurement of M to V [2.4, 2.6] and <br> Measurement of V to N [5.9, 6.1] | B1 | $\begin{aligned} & \mathrm{M} \text { to } \mathrm{V}=2.5 \mathrm{~cm} \\ & \mathrm{~V} \text { to } \mathrm{N}=6 \mathrm{~cm} \end{aligned}$ |
| :---: | :---: | :---: | :---: |
|  | their $6 \div$ their 2.5 <br> or their $2.5 \div$ their 6 <br> or $1 \mathrm{~cm}=120(\mathrm{~km})$ | M1 |  |
|  | $300 \times$ their $6 \div$ their 2.5 | M1 dep |  |
|  | [680, 765] | A1 | 720 |
|  | Alternative method |  |  |
|  | M to V ( 2.5 cm ) <br> V to F ( 2 cm ) and F to R ( 2.8 cm ) and R to $\mathrm{N}(2.2 \mathrm{~cm})$ | B1 | V to F ( 2 cm ) and F to $\mathrm{N}(4.8 \mathrm{~cm})$ <br> tolerances as above |
|  | their $7 \div$ their 2.5 or their $2.5 \div$ their 7 or $1 \mathrm{~cm}=120(\mathrm{~km})$ | M1 |  |
|  | Attempt to multiply by scale factor $\begin{aligned} & 300 \times \text { their }[6.6,7.3] \\ & \div \text { their }[2.4,2.6] \end{aligned}$ | M1 dep |  |
|  | [760, 920] | A1 | 840 or 884 |


| 8(a) | $4(5 x-3)$ | B1 |  |
| :---: | :--- | :---: | :--- |
| $8(\mathrm{~b})(\mathrm{i})$ | $(x+3)(x+4)$ | B2 | B1 for $(x+a)(x+b)$ <br> where $a b= \pm 12$ |
| $8(\mathrm{~b})$ (ii) | 0 | B1 |  |
| 8 8(c) | $3(x+3)+2(2 x-1)(=42)$ | M1 |  |
|  | $3(x+3)+2(2 x-1)=42$ <br> or <br> $3 x+9+4 x-2(=42)$ | M1 dep |  |
|  | $3 x+4 x=42-9+2$ <br> or <br> $7 x=35$ | M1 dep | oe |
|  | 5 | A1 |  |


| $9(\mathrm{a})$ | 1.5 or $\frac{2}{3}$ seen in (a) or (b) <br> or $\frac{15}{12}$ or $\frac{5}{4}$ | M1 | $\frac{z}{15}=\frac{8}{12}$ oe <br> 0.66 or 0.67 or better |
| :--- | :--- | :--- | :--- |
|  | $15 \div 1.5$ <br> or $15 \times \frac{2}{3}$ <br> or $8 \times \frac{15}{12}$ <br> or $8 \div \frac{12}{15}$ | M1 | oe |
|  | 10 | A1 |  |
| $9(b)$ | $y=1.5 x$ | B1 | oe eg $2 y=3 x \quad y=\frac{3 x}{2}$ |


| $10(\mathrm{a})$ | $360-80$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | 280 | A1 | Check diagram |
| $10(\mathrm{~b})$ | 50 | B1 | Check diagram |


| 11 | D | B1 | Accept $y=-x^{2}$ | Need to accept <br> $y=-x^{2}$ for D |
| :---: | :--- | :---: | :--- | :--- |
|  | A | B1 | Accept $y=x^{3}$ | and <br> $y=-x^{3}$ for A |


| 12 | $x^{2}+2 b x+b^{2}$ <br> or $2 b=12$ <br> or $(x+6)^{2}+a-36$ | M1 | $x^{2}+b x+b x+b^{2}$ <br> $(x+6)^{2}+a=(x+b)^{2}+36$ <br> $(x+6)^{2}=x^{2}+12 x+36$ |
| :---: | :--- | :---: | :--- |
|  | $b=6$ | A1 |  |
|  | A1 |  |  |


| 13(a) | $\frac{1}{3} \times 15 \times 16$ | M1 |  |
| :---: | :--- | :---: | :--- |
| 13(b) <br> (i) | $\frac{1}{8}$ | A1 |  |
| 13(b) <br> (ii) | their $80 \div 8 \times 7$ | B2 | B1 for unsimplified fraction <br> equivalent |
|  | M1 | oe their $80 \times$ their $\frac{7}{8}$ <br> oe their $80 \times\left(1-\right.$ their $\left.\frac{1}{8}\right)$ <br> Note: If volume used, must use $\frac{15}{4}$ <br> for area of base of small cone |  |


| 14(a) <br> (i) | $12 x^{2}-8 x y+3 x y-2 y^{2}$ | B1 | Fully correct |
| :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { 14(a) } \\ \text { (ii) } \\ \hline \end{gathered}$ | 1 | B1 |  |
| 14(b) | Use of $12 x^{2}-5 x y-2 y^{2}$ State that first or last term is even | M1 | Can also use the factorised form |
|  | Middle term $(x)$ is a multiple of 2 | M1 |  |
|  | Even + even + even | A1 |  |
|  | = even | A1 |  |
|  | Alternative method |  |  |
|  | If $y$ is odd $(4 x+y)$ is odd $(3 x-2 y)$ is even | M1 | Even + odd = odd and <br> Even - even $=$ even |
|  | Odd $\times$ even $=$ even | A1 |  |
|  | If $y$ is even $(4 x+y)$ is even $(3 x-2 y)$ is even | M1 | Even + even = even and <br> Even - even $=$ even |
|  | Even $\times$ even $=$ even | A1 |  |
|  | Alternative method 2 |  |  |
|  | If $y$ is odd ( $3 x-2 y$ ) is even | M1 |  |
|  | If $y$ is even $(4 x+y)$ is even | M1 |  |
|  | Even $\times$ anything or Anything $\times$ even | A1 |  |
|  | Even | A1 |  |

