

# General Certificate of Secondary Education 

## Mathematics 4307 Specification B

Module 3 Tier H 43053H

## Mark Scheme

2009 examination - March series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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## The following abbreviations are used on the mark scheme:

M $\quad$ Method marks awarded for a correct method.
A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.
M dep A method mark which is dependent on a previous method mark being awarded.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has some mathematical worth.
$\mathbf{0 e} \quad$ Or equivalent.
eeoo Each error or omission.

MODULE 3 HIGHER TIER
43053H

| $1(\mathrm{a})$ | $5 a+10$ | B1 |  |
| :--- | :--- | :--- | :--- |
| $1(\mathrm{~b})$ | $50(2 x-3)$ | B1 |  |
| $1(\mathrm{c})$ | $28(3 b-8)$ | B1 |  |


| $2(\mathrm{a})$ | $35 \div 7$ | M1 |  |  |
| :---: | :--- | :---: | :--- | :--- |
|  | 5 | A1 | $5: 35$ is M1A0 |  |
| $2(\mathrm{~b})$ | $2000-800(=1200)$ | M1 | $\frac{2000}{800}(=2.5)$ | Accept 250 <br> for M1 |
|  | $\frac{\text { their } 1200}{800} \times 100$ | M1 dep | their 2.5 <br> $\times 100-100$ <br> or their 250 -100 | (their 2.5-1) <br> $\times 100$ |
|  | 150 | A1 |  |  |


| 3 | $75-13.5(0)(=61.5(0))$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | their $61.5(0) \div 10.5(0)$ <br> $(=5.8 \ldots$ or 5.9$)$ | M1 dep | or their $61.5(0) \div 6(=10.25)$ |
|  | No $(£ 1.50$ short $)$ | A1 | No with no arithmetical errors seen |
|  | Alternate method | M1 | $(=76.5(0)$ or 66$)$ |
| $13.5(0)+6 \times 10.5(0)$ <br> or $13.5(0)+5 \times 10.5(0)$ | A1 |  |  |
| $76.5(0)$ | A1 ft | ft only from $6 \times 10.5(0)$ |  |
|  | No |  |  |


| 4 | $0.4 \times 1.8(0)$ or $0.2 \times 1.4(0)$ | M1 | oe $(0.72$ or 0.28$)$ <br> Allow use of pence |
| :---: | :--- | :---: | :--- |
|  | their $0.72+$ their 0.28 | M1 dep | $£ 1$ or 100 p |
|  | $2.00-$ (their $0.72+$ their 0.28$)$ | M1 dep |  |
|  | 500 | A1 |  |


| $5(\mathrm{a})$ | 667 | B1 |  |
| :---: | :--- | :---: | :--- |
| $5(\mathrm{~b})$ (i) | 1 | B1 |  |
| $5(\mathrm{~b})$ (ii) | 2 | B1 |  |


| $6(\mathrm{a})$ | $(x+a)(x+b)$ where $a b= \pm 20$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $(x+4)(x+5)$ | A1 | Either order |
| $6(\mathrm{~b})$ | $\frac{3-x}{x+5}$ | B1 ft |  |


| 7 | 9000000 | M1 | oe eg $0.9 \times 10^{7}, 9$ million |
| :--- | :--- | :---: | :--- |
|  | $9 \times 10^{6}$ | A1 |  |


| 8 8(a) | $T=\frac{k}{N}$ or $T \propto \frac{1}{N}$ | M1 | oe |
| :--- | :--- | :---: | :--- |
|  | $k=80 \times 4(=320)$ | M1 dep |  |
|  | $T=\frac{320}{N}$ | A1 | Accept $k=320$ after $T=\frac{k}{N}$ seen <br> oe |
| $8(\mathrm{~b})$ | $N=\frac{320}{16}$ | M1 | Watch out for incorrect methods |
|  | 20 | A1 ft | ft part (a) |


| 9(a) | Sight of 102 or 1.02 | B1 | oe |
| :---: | :--- | :---: | :--- |
|  | $\frac{54000000}{1.02}$ | M1 | oe $\frac{54000000}{102} \times 100$ |
|  | $52941176 .(\ldots)$ | A1 | To 2 significant figures or better <br> but if no method shown then to <br> 4 significant figures or better |
| $9(b)$ | $48000000 \times 1.047$ <br> $(=50256000)$ | M1 | oe |
| their $50256000 \times 1.047$ <br> $(=52618032)$ | M1 dep | $48000000 \times 1.047^{2}$ is M2 |  |
| $\frac{\text { their } 9(a)}{1.02}(=51903114)$ | Allow their rounded or full answer <br> from part (a) $\frac{54000000}{(1.02)^{2}}$ |  |  |
| Both answers correct and Lucy <br> correct $($ oe $)$ | A1 | At least 3 significant figures |  |


| 10 | $36000-3600$ | M1 | oe $\frac{90}{100} \times 36000$ |
| :---: | :--- | :---: | :--- |
|  | 32400 | A1 |  |
|  | 44000 | B1 |  |
|  | their $44000+$ their 32400 | M1 dep | dep on either M1 or B1 awarded |
| 76400 and yes | A1 ft | 75000 implied but if seen must be <br> correct |  |


| $11(\mathrm{a})$ | 286900 | B1 |  |
| :--- | :--- | :--- | :--- |
| $11(\mathrm{~b})$ | 30.2 | B1 |  |
| $11(\mathrm{c})$ | 28690 | B1 |  |


| $12(\mathrm{a})$ | $\frac{1}{8}$ | B1 |  |
| :--- | :--- | :--- | :--- |
| $12(\mathrm{~b})$ | $\frac{3}{7} \times \frac{1}{8}$ | M1 |  |
|  | $\frac{3}{56}$ | A1 |  |
| $12(\mathrm{c})$ | Either $\frac{7}{2}$ or $\frac{13}{7}$ seen | M1 | (2) $\frac{7}{14}(-) \frac{12}{14}$ |
|  | their $\frac{49}{14}(-) \frac{26}{14}$ | M1 | Common denominator with at least <br> one numerator correct <br> $2-\frac{5}{14}$ or $1 \frac{21}{14}(-) \frac{12}{14}$ |
|  | $\frac{23}{14}$ | A1 | $1 \frac{9}{14}$ oe No decimals |


| 13(a) <br> (i) | $t(t-1)$ | B1 |  |
| :---: | :--- | :---: | :--- |
| 13(a) <br> (ii) | Takes out common factor <br> of $(x+2)$ | M1 | Put $t=x+2$ <br> Allow other errors |
|  | $(x+2)(x+2-1)$ | A1 |  |
|  | $=(x+2)(x+1)$ | A1 |  |
|  | Alternate method | M1 | Allow one error |
|  | $x^{2}+2 x+2 x+4-(x+2)$ | A1 |  |
|  | $x^{2}+3 x+2$ | A1 |  |
|  | $=(x+2)(x+1)$ | B1 | Could be on table |
| $13(b)$ <br> (i) | $(-3,-2)$ identified | B1 | $\pm \frac{1}{2}$ square |
| 13(b) <br> (ii) | $(-3,2)$ plotted |  |  |


| $14(\mathrm{a})$ | Sixteen million | B1 |  |
| :--- | :--- | :---: | :--- |
| $14(\mathrm{~b})$ | $7.53 \times 10^{-3}$ | B1 |  |


| $15(\mathrm{a})$ | 8.535 | B1 | Accept 853.5 cm |
| :--- | :--- | :---: | :--- |
| $15(\mathrm{~b})$ | Sight of 8.365 or 836.5 | B1 | or use of $499 \ldots$ |
|  | Their min for Carl - their max for <br> Mike | M1 | Max must be more than 8.36 (oe) <br> Min must be less than $8.54(\mathrm{oe})$ |
|  | 0.17 or 17 or $0.16 \dot{9}$ or $16 . \dot{9}$ | A1 | Ignore units this time |


| $16(\mathrm{a})$ | 0.08 and/or -0.08 | B2 | oe eg $\frac{2}{25}$ <br> B1 sight of $0.01 \quad$ (oe) 8 or -8 |
| :---: | :--- | :---: | :--- |
| $16(\mathrm{~b})$ <br> (i) | $x^{\frac{2}{3}}$ | B1 | Condone $\left(x^{2}\right)^{\frac{1}{3}}$ or $\left(x^{\frac{1}{3}}\right)^{2}$ or $x^{2 \times \frac{1}{3}}$ <br> or $x^{2 \cdot \frac{1}{3}}$ or $x^{\frac{1}{3} \times 2}$ or $x^{\frac{1}{3} \cdot 2}$ |
| $16(\mathrm{~b})$ <br> (ii) | 4 | B1 |  |


| 17(a) | $\frac{\sqrt{20} \sqrt{45}(-) \sqrt{20} \sqrt{5}}{\sqrt{45} \sqrt{5}}$ | M1 | ie common denominator (allow one numerator error) |
| :---: | :---: | :---: | :---: |
|  | $\frac{\sqrt{20 \times 45}(-) \sqrt{20 \times 5}}{\sqrt{45 \times 5}}$ | M1 dep | Allow one arithmetical error |
|  | $\frac{20}{15}\left(=\frac{4}{3}\right)$ | A1 |  |
|  | Alternate method |  |  |
|  | $\sqrt{20}=2 \sqrt{5}$ or $\sqrt{45}=3 \sqrt{5}$ | M1 | Allow other errors |
|  | $\frac{2 \sqrt{5}}{\sqrt{5}}-\frac{2 \sqrt{5}}{3 \sqrt{5}}$ | M1 dep |  |
|  | $2-\frac{2}{3}\left(=\frac{4}{3}\right)$ | A1 |  |
| 17(b) | $\frac{\sqrt{4}}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$ | M1 | $\sqrt{\frac{12}{9}}$ |
|  | $\frac{2 \sqrt{3}}{3}$ | A1 | $\text { Accept } \frac{\sqrt{12}}{3}$ |

