

General Certificate of Secondary Education

Mathematics 4307

Specification B

Module 3 Tier H 43053H

Mark Scheme

2007 examination - November series

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The following abbreviations are used on the mark scheme:

M Method marks awarded for a correct method.

A Accuracy marks awarded when following on from a correct method. It is not necessary always to see the method. This can be implied.

B Marks awarded independent of method.

M dep A method mark which is dependent on a previous method mark being

awarded.

ft Follow through marks. Marks awarded for correct working following a

mistake in an earlier step.

SC Special Case. Marks awarded for a common misinterpretation which has

some mathematical worth.

oe Or equivalent.

eeoo Each error or omission.

MODULE 3 HIGHER TIER

43053H

| 1(a) | 1.126582 or $\frac{89}{79}$ | B1 | or better |
|------|-----------------------------|-------|----------------------------------|
| 1(b) | 1.127 | B1 ft | ft if (a) given to at least 4 dp |

| 2 | 60×1.65 or $100 \div 1.65$ | M1 | |
|---|---------------------------------------|--------|---|
| | 99 or 60.60 | A1 | Allow 60.6, 60.60, 60.61, 60.606 or better |
| | 100 – their 99 or their 60.60 – 60 | M1 dep | May be implied |
| | England by €1 or by 60p/61p | A1 ft | Must have correct unit ft to nearest cent or penny rounded or truncated |

| 3 | 0.39 × 800 (= 312) | M1 | oe | or sight of 0.61 or 61% |
|---|--------------------|--------|----|-------------------------|
| | 800 – (their 312) | M1 dep | oe | 800 × 0.61 |
| | 488 | A1 | | |

| 4(a) | Actual increase is 1900 – 600 | M1 | $1.9 - 0.6 \qquad \frac{1900}{600} \times 100$ |
|------|-------------------------------------|--------|--|
| | their $\frac{1300}{600} \times 100$ | M1 dep | their $\frac{1.3}{0.6} \times 100$ their 316.(6)-100 |
| | 216.(6) | A1 | Accept 217, 220 |
| | 200 | B1 ft | ft any number ≥ 2 sf |
| 4(b) | 1.12×600 | M1 | 672 |
| | 0.9×1300 | M1 | 1170 |
| | their 672 + their 1170 | M1 dep | Dependent on both M1s |
| | 1842 | A1 | SC3 2382 |

| 5 | Any of 1, 2, 3, 4, 6, 9, 12, 18, 36 and 36 or 4 and 18 or 12 and 18 | A pair of factors of 36 which have a different LCM B1 eg 4 and 12, 6 and 6 |
|---|---|--|
| | or 4 and 9 or 9 and 12 | leg 4 and 12, 6 and 6 |

| 6(a) | 5(2x+3) | B1 | |
|------|---------|----|--|
| 6(b) | y(y-2) | B1 | |
| 6(c) | 6x - 8 | B1 | |

| 7 | Largest = 82 000 | B1 | oe |
|---|-------------------------------|----|---------|
| | $Smallest = 3 \times 10^{-2}$ | B1 | 0.03 oe |

| 8 | Even \times odd = even or odd \times even = even | B1 | |
|---|--|------|--|
| | Even \times odd = even and odd \times even = even | I KI | SC1 at least two correct examples shown with clear evidence of × |

| 9 | After 1 day = 64% left After 2 days = 0.64×0.64 (= 0.4096) left | M1 | Accept use of amount eg $0.64 \times 1000 (= 640)$ their $640 \times 0.64 (= 409.6)$ for M1 |
|---|--|----|---|
| | \times 0.64 3 more times = 0.107 | A1 | $0.64^5 = 0.107$ M1A1 |
| | No with either 10.7% or 89.2% seen | A1 | |

| 10 | \times by $\frac{\sqrt{6}}{\sqrt{6}}$ | B1 | Sight of $\frac{18\sqrt{6}}{\sqrt{6}\sqrt{6}}$ oe |
|----|---|----|---|
| | Sight of denominator of 6 | B1 | Remember answer was given, must convince SC1 $3\sqrt{6} \times \sqrt{6} = 18$ Allow $\frac{18\sqrt{6}}{6}$ for B2 |

| 11 | Sight of 8.5 or 9.5 or 7500 or 8500 | B1 | or 0.905 or 90.5 Accept 9.49 for 9.5 and 8499 (.99) for 8500 |
|----|--|----|---|
| | Chooses their max price and their max reduction | M1 | Max price > 8000 Max reduction >9 or >0.09 or <0.91 or <91 Sensible value |
| | $\frac{8500}{0.905}$ or $\frac{8500}{90.5} \times 100$ | M1 | oe |
| | £9392.27 or £9392(.00) | A1 | Sight of 9392.265(1) SC3 |

| 12(a) | $\frac{6}{10}$ | B2 | oe fraction $\frac{4}{10}$ B1 |
|-------|--|----|---|
| | $ \begin{array}{c} 3 \times 50 \text{ or} \\ 6 \times 50 \end{array} $ | M1 | Also allow 4×50 for M1 if $\frac{4}{10}$ above |
| | Men = 150 | A1 | |
| | Children = 300 | A1 | |
| 12(b) | 3:1 | B1 | oe eg 150:50 or $\frac{3}{10}$: $\frac{1}{10}$ |

| 13(a) | $1\frac{2}{3} \times 2$ | M1 | $3\frac{1}{3}$ or $\frac{10}{3}$ or $2\frac{4}{3}$ oe Allow decimals ≥ 2 dp rounded or truncated $2 + 2 = 4$ or $2 \times 2 = 4$ M0A0 |
|-------|---|----|--|
| | 4 | A1 | |
| 13(b) | $1\frac{2}{3} + 1\frac{1}{4}$ | M1 | |
| | $(1)\frac{8}{12} (+) (1)\frac{3}{12}$ | M1 | oe Valid denominator, at least one correct numerator (1).66 (+) (1).25 |
| | $2\frac{11}{12}$ and some indication of yes | A1 | 2.91 or 2.92 and Yes oe |

| 14(a) | Attempts to multiply numerators and denominators | M1 | |
|-------|--|----|---------------------|
| | $\frac{6}{55}$ | A1 | oe |
| 14(b) | Shows intention to times by $\frac{1}{4}$ | M1 | oe 0.375 ÷ 4 3 ÷ 32 |
| | $\frac{3}{32}$ | A1 | 0.09375 |

| 15(a) | 16 (×) 9 | M1 | Must have both |
|-------|---|----|---|
| | 144 | A1 | |
| 15(b) | Correct method for 32 in index form $(= 2^5)$ | M1 | or lists factors of 32 and 144 with no more than 2 errors |
| | 16 or 2 ⁴ | A1 | |

| 16 All three correct Statement 1 matches Table B Statement 2 matches Table C Statement 3 matches Table A | B2 | B1 for one (or two) correct | |
|--|----|-----------------------------|--|
|--|----|-----------------------------|--|

| 17(a) | x coordinate 0.5 | B1 | Tolerance 0.1 |
|---------------|--------------------------------------|----|--|
| | y coordinate –12.25 | B1 | Tolerance 0.2 |
| 17(b) (i) | (x-4)(x+3) | B2 | B1 $(x + a)(x + b)$ where $ab = \pm 12$ |
| 17(b) (ii) | Cancels $(x + 3)$ | M1 | or multiply $(x^2 - x - 12)(x - 5)$ to give $x^3 - 5x^2 - x^2 - 12x - 5x + 60$ Allow one sign error and $(x^2 - 9x + 20)(x + 3)$ to give same Allow one sign error |
| | Convincing expansion of $(x-4)(x-5)$ | A1 | Must see 4 terms at one point or an explanation of the simplifying |

| 18 | Correct method for recurring decimal | M1 | eg let $x = 0.2$ then 10x = 2.2 and subtract so $9x = 2$ etc |
|----|---|--------|---|
| | $\frac{2}{9} \times \frac{9}{20}$ attempted | M1 dep | oe $\frac{2}{9} \times \frac{45}{100}$ attempted or $0.45 \div 9 \times 2$ attempted or 0.1 |
| | $\frac{1}{10}$ | A1 | oe fraction |

| 19(a) | $\frac{1}{\sqrt{5^2}}$ or $\left(\frac{1}{\sqrt{5}}\right)^2$ or $\frac{1^2}{\sqrt{5^2}}$ or 5^{-1} | M1 | |
|-------|---|----|--|
| | $\frac{1}{5}$ | A1 | oe |
| 19(b) | $\sqrt{5}\sqrt{45} = \sqrt{5 \times 45}$ | M1 | or $\frac{\sqrt{5} \times \sqrt{45}}{5} = \frac{\sqrt{45}}{\sqrt{5}}$ or $\sqrt{45} = \sqrt{9}\sqrt{5}$ |
| | $\sqrt{225} = 15 \div 5 \ (=3)$ | M1 | $\sqrt{9}$ (= 3) or $\frac{\sqrt{5}\sqrt{9}\sqrt{5}}{5} = \sqrt{9}$ (= 3) |
| | $\sqrt{3}$ | A1 | Allow $3^{\frac{1}{2}}$ |