## Q. No. 1-5 Carry One Mark Each

1. Which of the following options is the closest in meaning to the word underlined in the sentence below?

In a democracy, everybody has the freedom to disagree with the government.
(A) dissent
(B) descent
(C) decent
(D) decadent

Answer: (A)
2. After the discussion, Tom said to me, 'Please revert!' He expects me to $\qquad$ .
(A) retract
(B) get back to him
(C) move in reverse
(D) retreat

Answer: (B)
3. While receiving the award, the scientist said, "I feel vindicated". Which of the following is closest in meaning to the word 'vindicated'?
(A) punished
(B) substantiated
(C) appreciated
(D) chastened


Answer: (B)

4. Let $f(x, y)=x^{n} y^{m}=P$. If $x$ is doubled and $y$ is halved, the hew value of $f$ is
(A) $2^{n-m} P$
(B) $2^{m-n} \mathrm{P}$
(C) $2(n-m) P$
(D) $2(\mathrm{~m}-\mathrm{n}) \mathrm{P}$

Answer: (A)
Exp. $\quad P^{\prime}=2^{n} X^{n}\left(\frac{1}{2}\right)^{m} y^{m}$

$$
=2^{\mathrm{n}-\mathrm{m}} X^{\mathrm{n}} Y^{m}=2^{\mathrm{n}-\mathrm{m}} P
$$

5. In a sequence of 12 consecutive odd numbers, the sum of the first 5 numbers is 425 . What is the sum of the last 5 numbers in the sequence?
Answer: 495
Exp. $8^{\text {th }}$ observation is $7 \times 2=14$ more than $1^{\text {st }}$ observation
$9^{\text {th }}$ observation is 14 more than $2^{\text {nd }}$ observation
$10^{\text {th }}$ observation is 14 more than $3^{\text {rd }}$ observation
$11^{\text {th }}$ observation 14 more than $4^{\text {th }}$ observation
$12^{\text {th }}$ observation 14 more than $5^{\text {th }}$ observation
Total $14 \times 5=70$
Sum of the first five numbers $=425$
Sum of last five numbers $=495$

## Q. No. 6 - 10 Carry Two Marks Each

6. Find the next term in the sequence: $13 \mathrm{M}, 17 \mathrm{Q}, 19 \mathrm{~S}$, $\qquad$
(A) 21 W
(B) 21 V
(C) 23 W
(D) 23 V

Answer: (C)
7. If 'KCLFTSB' stands for 'best of luck' and 'SHSWDG' stands for 'good wishes', which of the following indicates 'ace the exam'?
(A) MCHTX
(B) MXHTC
(C) XMHCT
(D) XMHTC

Answer: (B)
Exp. KCLFTSB: BST-Best, F-Of, LCK-Luck (Reverse order)
SHSWDG: GD-Good, WSHS-Wishes (Reverse order)
Similarly "ace the Exam'- C-Ace, T-The, XM-Exam
8. Industrial consumption of power doubled from 2000-2001 to 2010-2011. Find the annual rate of increase in percent assuming it to be uniform over the years.
(A) 5.6
(B) 7.2
(C) 10.0
(D) 12.2

Answer: (B)
9. A firm producing air purifiers sold 200 units in 2012. The following pie chart presents the share of raw material, labour, energy, plant \& machinery, and transportation costs in the total manufacturing cost of the firm in 2012. The expenditure on labour in 2012 is Rs. 4,50,000. In 2013, the raw material expenses increased by $30 \%$ and all other expenses increased by $20 \%$. What is the percentage increase in total cost for the company in 2013?

Answer: 22
Exp.


|  | 2012 | 2013 |
| :--- | :--- | :--- |
| Transport (10\%) | 300,000 | 360,000 |
| Labour (15\%) | 450,000 | 540,000 |
| Raw material (20\%) | 750,000 | 780,000 |
| Energy (25\%) | 750,000 | 900,000 |
| Plant and Machinery (30\%) | 900,000 | $1,080,000$ |
| Total | $\mathbf{3 , 0 0 0 , 0 0 0}$ | $\mathbf{3 , 6 6 0 , 0 0 0}$ |

Percentage increase in total cost $=22 \%$
10. A five digit number is formed using the digits $1,3,5,7$ and 9 without repeating any What is the sum of all such possible five digit numbers?
(A) 6666660
(B) 6666600
(C) 6666666
(D) 6666606

Answer: (B)
Exp. The digit in unit place is selected in 4! Ways
The digit in tens place is selected in 4 ! Ways
The digit in hundreds place is selected in 4! Ways
The digit in thousands place is selected in 4! Ways
The digit in ten thousands place is selected in 4! Ways
Sum of all values for 1

$$
\begin{aligned}
& 4!\times 1 \times\left(10^{0}+10^{1}+10^{2}+10^{3}+10^{4}\right) \\
& =4!\times 11111 \times 1
\end{aligned}
$$

Similarly for ' 3 ' $4!\times(11111) \times 3$


$$
=24 \times(11111) \times 25=6666600
$$

## Q. No. 1-25 Carry One Mark Each

1. Which one of the following equations is a correct identity for arbitrary $3 \times 3$ real matrices $\mathrm{P}, \mathrm{Q}$ and R ?
(A) $\mathrm{P}(\mathrm{Q}+\mathrm{R})=\mathrm{PQ}+\mathrm{RP}$
(B) $(\mathrm{P}-\mathrm{Q})^{2}=\mathrm{P}^{2}-2 \mathrm{PQ}+\mathrm{Q}^{2}$
(C) $\operatorname{det}(P+Q)=\operatorname{det} P+\operatorname{det} Q$
(D) $(\mathrm{P}+\mathrm{Q})^{2}=\mathrm{P}^{2}+\mathrm{PQ}+\mathrm{QP}+\mathrm{Q}^{2}$

Answer: (D)
2. The value of the integral $\int_{0}^{2} \frac{(x-1)^{2} \sin (x-1)}{(x-1)^{2}+\cos (x-1)} d x$ is
(A) 3
(B) 0
(C) -1
(D) -2

Answer: (B)
Exp: Let $I=\frac{\int_{0}^{2}(x-1)^{2} \sin (x-1)}{(x-1)^{2}+\cos (x-1)} d x$
We know that, $\int_{0}^{2} \frac{(2-x-1)^{2} \sin (2-x-1)}{(2-x-1)^{2}+\cos (2-x-1)} d x$
$=\int_{0}^{2} \frac{(1-x)^{2} \sin (1-x)}{(1-x)^{2}+\cos (1-x)} d x$ ineering SUCCESS
$=-\int_{0}^{2} \frac{(x-1)^{2} \sin (x-1)}{(x-1)^{2}+\cos (x-1)} d x=-I$
$\Rightarrow \mathrm{I}+\mathrm{I}=0 \Rightarrow 2 \mathrm{I}=0 \Rightarrow \mathrm{I}=0$
3. The solution of the initial value problem $\frac{d y}{d x}=-2 x y ; y(0)=2$ is
(A) $1+\mathrm{e}^{-\mathrm{x}^{2}}$
(B) $2 e^{-x^{2}}$
(C) $1+e^{x^{2}}$
(D) $2 \mathrm{e}^{\mathrm{x}^{2}}$

Answer: (B)
Exp: Given $\frac{d y}{d x}=-2 x y, y(0)=2$ is
$\Rightarrow \frac{\mathrm{dy}}{\mathrm{dx}}+2 \mathrm{xy}=0$
comparing with $\frac{\mathrm{dy}}{\mathrm{dx}}+\mathrm{py}=\mathrm{Q}$
$\mathrm{P}=2 \mathrm{x} ; \mathrm{Q}=0$
I.F $=e^{\int p d x}=e^{\int 2 x d x}=e^{x^{2}}$

Solution is $y(I F)=\int Q(I P) d x+C$

$$
\begin{aligned}
& \mathrm{ye}^{\mathrm{x}^{2}}=0+\mathrm{C} \\
& \therefore \mathrm{y}=\mathrm{Ce}^{-\mathrm{x}^{2}}
\end{aligned}
$$

Given $y(0)=2 \Rightarrow 2=C$

$$
\therefore \mathrm{y}=2 \mathrm{e}^{-\mathrm{x}^{2}}
$$

4. A nationalized bank has found that the daily balance available in its savings accounts follows a normal distribution with a mean of Rs. 500 and a standard deviation of Rs. 50. The percentage of savings account holders, who maintain an average daily balance more than Rs 500 is $\qquad$
Answer: 49 to 51
Exp: Given $\mathrm{M}=500$
$\sigma=50$

$$
\mathrm{P}(\mathrm{X}>500)=?
$$

Where X follows normal distribution
We know that standard normal variable


$$
\begin{aligned}
& \mathrm{z}=\frac{\mathrm{x}-\mathrm{M}}{\sigma} \\
& \mathrm{z}=\frac{500-500}{50}=0 \\
& \therefore(\mathrm{X}>500)=\mathrm{P}(\mathrm{z}>0)=0.50 \text { (see figure) }
\end{aligned}
$$

5. Laplace transform of $\cos (\omega t)$ is $\frac{s}{s^{2}+\omega^{2}}$. The laplace transform of $e^{-2 t} \cos (4 t)$ is
(A) $\frac{s-2}{(s-2)^{2}+16}$
(B) $\frac{s+2}{(s-2)^{2}+16}$
(C) $\frac{\mathrm{s}-2}{(\mathrm{~s}+2)^{2}+16}$
(D) $\frac{\mathrm{s}+2}{(\mathrm{~s}+2)^{2}+16}$

Answer: (D)

Exp: We know that if $\mathrm{L}\{\mathrm{f}(\mathrm{t})\}=\mathrm{F}(\mathrm{s})$
Then $L\left\{e^{a t} f(t)\right\}=F(s-a)$

$$
\begin{aligned}
\therefore \mathrm{L}\left\{\mathrm{e}^{-2 \mathrm{t}} \cos 4 \mathrm{t}\right\} & =\frac{\mathrm{s}+2}{(\mathrm{~s}+2)^{2}+4^{2}} \\
& =\frac{\mathrm{s}+2}{(\mathrm{~s}+2)^{2}+16}
\end{aligned}
$$

6. In a statically determinate plane truss, the number of joints (j) and the number of mo (m) are related by
(A) $j=2 m-3$
(B) $m=2 j+1$
(C) $m=2 j-3$
(D) $\mathrm{m}=2 \mathrm{j}-1$

Answer: (C)
7. If the Poisson's ratio of an elastic material is 0.4 , the ratio of modulus of rigidity to Young's modulus is $\qquad$
Answer: 0.35 to 0.36
Exp: From $E=2 G(1+\mu)$

$$
\frac{G}{E}=\frac{1}{2(1+\mu)}=\frac{1}{2(1+0.4)}=0.357
$$

8. Which one of the following is used to convert a rotational motion into a translational motion?
(A) Bevel gears
(B) Double helical gears
(C) Worm gears
(D) Rack and pinion gears

Answer: (D)
9. The number of independent elastic constants required to define the stress-strain relationship for an isotropic elastic solid is
Answer: 1.9 to 2.1
10. A point mass is executing simple harmonic motion with an amplitude of 10 mm and frequency of 4 Hz . The maximum acceleration $\left(\mathrm{m} / \mathrm{s}^{2}\right)$ of the mass is $\qquad$
Answer: 6.3 to 6.4
Exp: Given $\mathrm{A}=10 \mathrm{~mm}=0.01 \mathrm{~m}$
$\mathrm{f}=4 \mathrm{~Hz}$
$\mathrm{x}=\mathrm{A} \cos \omega \mathrm{t}$
$\mathrm{v}=\frac{\mathrm{dx}}{\mathrm{dt}}=-\mathrm{A} \omega \sin \omega \mathrm{t}$
$\frac{d^{2} \mathrm{x}}{\mathrm{dt}^{2}}=\mathrm{a}=-\mathrm{A} \omega^{2} \cos \omega \mathrm{t}$
For maximum, $\mathrm{t}=0$

$$
\begin{aligned}
& \therefore \mathrm{a}=\mathrm{A} \omega^{2}=0.01(2 \pi \mathrm{f})^{2} \\
& \because \omega=2 \pi \mathrm{f}=0.01(2 \times \pi \times 4)^{2}=6.32 \mathrm{~m} / \mathrm{s}^{2}
\end{aligned}
$$

11. Ball bearings are rated by a manufacturer for a life of $10^{6}$ revolutions. The catalogue rating of a particular bearing is 16 kN . If the design load is 2 kN , the life of the bearing will be $\mathrm{p} \times 10^{6}$ revolutions, where $p$ is equal to $\qquad$
Answer: 500 to 540

Exp: $\quad \mathrm{L}=\left(\frac{\mathrm{c}}{\mathrm{w}}\right)^{\mathrm{k}} \times 10^{6} \quad \mathrm{k}=3$ (Ball bearing)
$=\left(\frac{16}{2}\right)^{3} \times 10^{6}=8^{3} \times 10^{6}=\mathrm{P} \times 10^{6}$

$$
\mathrm{P}=512
$$

12. As the temperature increases, the thermal conductivity of a gas
(A) increases
(B) decreases
(C) remains constant
(D) increases up to a certain temperature and then decreases

Answer: (A)
Exp: $K=\frac{n V \lambda C_{V}}{3 N_{A}}$
Where K is thermal conductivity
V is mean particle speed
$\lambda$ is mean free path
$\mathrm{C}_{\mathrm{V}}$ is molar head capacity
$\mathrm{N}_{\mathrm{A}}$ is Avogadro's number
n is particles per unit volume
Gases transfer heat by direct collisions between molecules. As the temperature increases, the thermal conductivity increases due to increase in speed, movement and collisions in the molecules. From the above expression, by increasing mean particle speed, the thermal conductivity increases.
13. A reversed Carnot cycle refrigerator maintains a temperature of $-5^{\circ} \mathrm{C}$. The ambient air temperature is $35^{\circ} \mathrm{C}$. The heat gained by the refrigerator at a continuous rate is $2.5 \mathrm{~kJ} / \mathrm{s}$. The power (in watt) required to pump this heat out continuously is $\qquad$
Answer: 370 to 375
Exp: $\frac{\mathrm{Q}_{1}}{268}=\frac{\mathrm{Q}_{2}}{308}$
$\mathrm{Q}_{2}=\frac{2.5 \times 308}{268}$
$\mathrm{Q}_{2}=2.873 \mathrm{kw}$
$\mathrm{w}=\mathrm{Q}_{2}-\mathrm{Q}_{1}=0.373 \mathrm{kw}=373.13 \mathrm{watt}$.
14. A flow field which has only convective acceleration is
(A) a steady uniform flow
(B) an unsteady uniform flow
(C) a steady non-uniform flow
(D) an unsteady non-uniform flow

Answer: (C)
Exp: Convective acceleration is the effect of time independent acceleration of fluid with respect to space that means flow is steady non-uniform flow.
15. Match Group A with Group B:

| Group A | Group B |
| :--- | :--- |
| P: Biot number | 1: Ratio of buoyancy to viscous force |
| Q: Grashof number | 2: Ratio of inertia force to viscous force |
| R: Prandtl number | 3: Ratio of momentum to thermal diffusivities |
| S: Reynolds number | 4: Ratio of internal thermal resistance to boundary layer <br> thermal resistance |

(A) P-4, Q-1, R-3, S-2
(B) P-4, Q-3, R-1, S-2
(C) P-3, Q-2, R-1, S-4
(D) P-2, Q-1, R-3, S-4

Answer: (A)
16. Kaplan water turbine is commonly used when the flow through its runner is
(A) axial and the head available is more than 100 m
(B) axial and the head available is less than 10 m
(C) radial and the head available is more than 100 m
(D) mixed and the head available is about 50 m

Answer: (B)
Exp: Kaplan turbine is an axial flow turbine and works at low heads ( $<50$ ).
17. Moist air at $35^{\circ} \mathrm{C}$ and $100 \%$ relative humidity is entering a psychometric device and leaving at $25^{\circ} \mathrm{C}$ and $100 \%$ relative humidity. The name of the device is
(A) Humidifier
(B) Dehumidifier
(C) Sensible heater
(D) Sensible cooler

Answer: (B)
Exp:


Since water content in moist air is reducing. The device is de-humidifier.
18. The total number of decision variables in the objective function of an assignment problem of size $n \times n$ ( $n$ jobs and n machines) is
(A) $n^{2}$
(B) $2 n$
(C) $2 n-1$
(D) $n$

Answer: (A)
Exp: A, $n \times n$ assignment problem, if it is solved as a LPP it will have $\mathrm{n}^{2}$ variables.
19. Demand during lead time with associated probabilities is shown below:

| Demand | 50 | 70 | 75 | 80 | 85 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Probability | 0.15 | 0.14 | 0.21 | 0.20 | 0.30 |

Expected demand during lead time is $\qquad$
Answer: 74 to 75
Exp: Probability

| $\mathrm{x}_{\mathrm{i}}$ | $\mathrm{f}_{\mathrm{i}}$ | $\mathrm{X}_{\mathrm{i}} \mathrm{f}_{\mathrm{i}}$ |
| :---: | :---: | :---: |
| 50 | 0.15 | 7.5 |
| 70 | 0.14 | 9.8 |
| 75 | 0.21 | 15.75 |
| 80 | 0.2 | 16 |
| 85 | 0.3 | 25.5 |

Expected demand during lead time $=74.55$.
20. Within the Heat Affected Zone (HAZ) in a fusion welding process, the work material undergoes
(A) microstructural changes but does not melt
(B) neither melting nor microstructural changes
(C) both melting and microstructural changes after solidification
(D) melting and retains the original microstructure after solidification

Answer: (A)
21. Two separate slab milling operations, 1 and 2, are performed with identical milling cutters. The depth of cut in operation 2 is twice that in operation 1 . The other cutting parameters are identical.
The ratio of maximum uncut chip thicknesses in operations 1 and 2 is $\qquad$
Answer: 0.70 to 0.72
Exp: $\quad$ Ratio of 1 and 2 is $=\frac{\sqrt{\mathrm{d}_{1}}}{\sqrt{\mathrm{~d}_{2}}} \therefore \mathrm{~d}_{2}=2 \mathrm{~d}_{1}$
$=\frac{\sqrt{\mathrm{d}_{1}}}{\sqrt{2 \mathrm{~d}_{1}}}$
$=\sqrt{\frac{1}{2}}=0.707$.
22. The principle of material removal in Electrochemical machining is
(A) Fick's law
(B) Faraday's laws
(C) Kirchhoff's laws
(D) Ohm's law

Answer: (B)
23. Better surface finish is obtained with a large rake angle because
(A) the area of shear plane decreases resulting in the decrease in shear force and cutting for
(B) the tool becomes thinner and the cutting force is reduced
(C) less heat is accumulated in the cutting zone
(D) the friction between the chip and the tool is less

Answer: (A)
24. Match the heat treatment processes (Group A) and their associated effects on properties (Group B) of medium carbon steel:

| Group A | Group B |
| :--- | :--- |
| P: Tempering | I: Strengthening and grain refinement |
| Q: Quenching | II: Inducing toughness |
| R: Amealing | III: Hardening |
| S: Normalizing | IV: Softening |

(A) P-III, Q-IV, R-II, S-I
(B) P-II, Q-III, R-IV, S-I
(C) P-III, Q-II, R-IV, S-I
(D) P-II, Q-III, R-I, S-IV

## Answer: (B)

25. In a rolling process, the maximum possible draft, defined as the difference between the initial and the final thickness of the metal sheet, mainly depends on which pair of the following parameters
P: Strain
Q: Strength of the work material
R: Roll diameter
S: Roll velocity
T: Coefficient of friction between roll and work
(A) Q, S
(B) R, T
(C) $\mathrm{S}, \mathrm{T}$
(D) $\mathrm{P}, \mathrm{R}$

Answer: (B)

## Q. No. 26 - 55 Carry Two Marks Each

26. If z is a complex variable, the value of $\int_{5}^{3 i} \frac{\mathrm{dz}}{\mathrm{z}}$ is
(A) $-0.511-1.57 \mathrm{i}$
(B) $-0.511+1.57 \mathrm{i}$
(C) $0.511-1.57 \mathrm{i}$
(D) $0.511+1.57 \mathrm{i}$

Answer: (B)
Exp: $\quad \int_{5}^{3 i} \frac{d z}{z}=\left.\ln (\mathrm{z})\right|_{5} ^{3 \mathrm{i}}$

$$
\begin{aligned}
& =\ln 3 \mathrm{i}-\ln 5=\ln 3+\mathrm{i} \frac{\pi}{2}-(\ln 5+\mathrm{i} 0) \\
& {\left[\therefore \ln \mathrm{z}=\ln \mathrm{r}+\mathrm{i} \theta \text { where } \mathrm{r}=\sqrt{\mathrm{x}^{2}+\mathrm{y}^{2}}, \theta=\arg \mathrm{z}\right]} \\
& =\ln 3-\ln 5+\mathrm{i} \frac{22}{14}=-0.511+1.57 \mathrm{i}
\end{aligned}
$$

27. The value of integral $\int_{0}^{2} \int_{0}^{x} e^{x+y} d y d x$ is
(A) $\frac{1}{2}(\mathrm{e}-1)$
(B) $\frac{1}{2}\left(\mathrm{e}^{2}-1\right)^{2}$
(C) $\frac{1}{2}\left(\mathrm{e}^{2}-\mathrm{e}\right)$
(D) $\frac{1}{2}\left(\mathrm{e}-\frac{1}{\mathrm{e}}\right)^{2}$

Answer: (B)
Exp. $\quad \int_{0}^{2} \int_{0}^{x} e^{x+y} d y d x=\int_{0}^{2} e^{x}\left(\int_{0}^{x} e^{y} d y\right) d x$
$=\int_{0}^{2} e^{x}\left(e^{y}\right)_{0}^{x} d x=\int_{0}^{2} e^{x}\left(e^{x}-1\right) d x$
$=\int_{0}^{2}\left(e^{2 x}-e^{x}\right) d x=\left(\frac{e^{2 x}}{2}-e^{x}\right)_{0}^{2}$
$=\frac{e^{4}}{2}-e^{2}-\frac{1}{2}+1=\frac{e^{4}}{2}-e^{2}+\frac{1}{2} \square \square \square \square$
$=\frac{1}{2}\left(\mathrm{e}^{4}-2 \mathrm{e}^{2}+1\right)=\frac{1}{2}\left(\mathrm{e}^{2}-1\right)^{2}$ gineering Success
28. The number of accidents occurring in a plant in a month follows Poisson distribution with mean as 5.2 . The probability of occurrence of less than 2 accidents in the plant during a randomly selected month is
(A) 0.029
(B) 0.034
(C) 0.039
(D) 0.044

Answer: (B)
Exp: Given $\lambda=5.2$
Let x be random variable which follows Poisson's distribution

$$
\begin{aligned}
& P(x<2)=P(x=0)+P(x=1) \\
& =\frac{e^{-\lambda} \lambda^{0}}{0!}+\frac{e^{-\lambda}}{1!} \lambda^{1}=e^{-5.2}(6.2)=0.0055 \times 6.2=0.034
\end{aligned}
$$

29. Consider an ordinary differential equation. $\frac{\mathrm{dx}}{\mathrm{dt}}=4 \mathrm{t}+4$. If $x=x_{0}$ at $t=0$, the increment in x calculated using Runge-Kutta fourth order multi-step method with a step size of $\Delta \mathrm{t}=0.2$ is
(A) 0.22
(B) 0.44
(C) 0.66
(D) 0.88

Answer: (D)

Exp: Given $\frac{\mathrm{dx}}{\mathrm{dt}}=4 \mathrm{t}+4 \quad \mathrm{x}=\mathrm{x}_{\mathrm{o}}$ at $\mathrm{t}=0$

$$
\mathrm{n}=0.2
$$

Calculate $\mathrm{x}(0.2)$ value
$\mathrm{K}_{1}=\mathrm{f}\left(\mathrm{t}_{0}, \mathrm{x}_{0}\right)=\mathrm{f}\left(0, \mathrm{x}_{0}\right)=4$
$\mathrm{K}_{2}=\mathrm{f}\left(\mathrm{t}_{0}+\frac{\mathrm{h}}{2}, \mathrm{x}_{0}+\frac{1}{2} \mathrm{~K}_{1} \mathrm{~h}\right)$
$=\mathrm{f}\left(0+0.1, \mathrm{x}_{0}+0.4\right)=\mathrm{f}\left(001, \mathrm{x}_{0}+0.4\right)=4(0.1)+4=4.4$
$\mathrm{K}_{3}=\mathrm{f}\left(\mathrm{x}_{0}+\frac{\mathrm{h}}{2}, \mathrm{x}_{0}+\frac{\mathrm{K}_{2} \mathrm{~h}}{2}\right)$
$=f\left(t_{0}+0.1, x_{0}+(2.2)(0.2)\right)=f\left(0.1, x_{0}+0.44\right)=4(0.1)+4=4.4$
$\mathrm{K}_{4}=\mathrm{f}\left(\mathrm{t}_{0}+\mathrm{h}, \mathrm{x}_{0}+\mathrm{K}_{3} \mathrm{~h}\right)$
$=\mathrm{f}\left(0+0.2, \mathrm{x}_{0}+0.88\right)=\mathrm{f}\left(0.2, \mathrm{x}_{0}+0.88\right)=4(0.2)+4=4.8$
$x(0.2)=x_{1}=x_{0}+\frac{h}{6}\left(K_{1}+2 K_{2}+2 K_{3}+K_{4}\right)$
$=x_{0}+\frac{0.2}{6}(4+2(4.4)+2(4.4)+(4.8))$
$=x_{0}+\frac{0.2}{6}(4+2(4.4)+2(4.4) \pm(4.8))$ eering Success
$=\mathrm{x}_{0}+\frac{0.2}{6}(4+8.8+8.8+4.8)=\mathrm{x}_{0}+0.88$
Increment as $\mathrm{x}=\mathrm{x}_{1}-\mathrm{x}_{0}=\mathrm{x}_{0}+0.88-\mathrm{x}_{0}=0.88$
30. A shaft is subjected to pure torsional moment. The maximum shear stress developed in the shaft is 100 MPa . The yield and ultimate strengths of the shaft material in tension are 300 MPa and 450 MPa , respectively. The factor of safety using maximum distortion energy (vonMises) theory is $\qquad$
Answer: 1.7 to 1.8
Exp: $\quad \tau_{\text {max }}=\frac{\sigma_{u}}{2 \mathrm{FOS}}$
$\Rightarrow \mathrm{FOS}=\frac{300}{2 \times 100}=1.5$
31. A thin gas cylinder with an internal radius of 100 mm is subject to an internal pressure of 10 MPa . The maximum permissible working stress is restricted to 100 MPa . The minimum cylinder wall thickness (in mm ) for safe design must be $\qquad$
Answer: 9.8 to 10.6
Exp: $\quad \sigma_{1}=\frac{\mathrm{pd}}{2 \mathrm{t}} \Rightarrow 100=\frac{10 \times 2 \times 100}{2 \times \mathrm{t}} \Rightarrow \mathrm{t}=10 \mathrm{~mm}$
32. For the truss shown in the figure, the forces F1 and F2 are 9 kN and 3 kN , respective force (in kN ) in the member QS is

(A) 11.25 tension
(B) 11.25 compression
(C) 13.5 tension
(D) 13.5 compression

Answer: (A)
Exp: By method of sections

$\Rightarrow \mathrm{F}_{\mathrm{QS}}=11.25(\mathrm{~T})$
33. It is desired to avoid interference in a pair of spur gears having a $20^{\circ}$ pressure angle. With increase in pinion to gear speed ratio, the minimum number of teeth on the pinion
(A) increases
(B) decreases
(C) first increases and then decreases
(D) remains unchanged

Answer: (A)
34. A uniform slender rod ( 8 m length and 3 kg mass) rotates in a vertical plane about a horizontal axis 1 m from its end as shown in the figure. The magnitude of the angular acceleration (in rad $/ \mathrm{s}^{2}$ ) of the rod at the position shown is $\qquad$


Answer: 1.9 to 2.1
35. A bolt of major diameter 12 mm is required to clamp two steel plates. Cross sectional the threaded portion of the bolt is $84.3 \mathrm{~mm}^{2}$. The length of the threaded portion in grip mm , while the length of the unthreaded portion in grip is 8 mm . Young's modulus of materim is 200 GPa . The effective stiffness ( $\mathrm{in} \mathrm{MN} / \mathrm{m}$ ) of the bolt in the clamped zone is $\qquad$
Answer: 460 to 470
Exp: $\mathrm{d}_{1}=12 \mathrm{~mm}$;
$\mathrm{l}_{1}=8 \mathrm{~mm}$
$\mathrm{A}_{2}=84.33 \mathrm{~mm}^{2}$
$\mathrm{A}_{1}=\frac{\pi}{4}\left(\mathrm{~d}_{1}\right)^{2}$
$\mathrm{A}_{2}=84.33 \mathrm{~mm}^{2}$
$1_{2}=30 \mathrm{~mm}$
$\mathrm{K}_{1}=\frac{\mathrm{A}_{1} \mathrm{E}_{1}}{\mathrm{l}_{1}} ; \mathrm{K}_{2}=\frac{\mathrm{A}_{2} \mathrm{E}_{2}}{\mathrm{l}_{2}}=\frac{84.33 \times 200}{30}=562.2$
$=\frac{\frac{\pi}{4}(12)^{2} \times 200}{8}=2827.4$

36. A frame is subjected to a load P as shown in the figure. The frame has a constant flexural rigidity EI. The effect of axial load is neglected. The deflection at point A due to the applied load P is

(A) $\frac{1}{3} \frac{\mathrm{PL}^{3}}{\mathrm{EI}}$
(B) $\frac{2}{3} \frac{\mathrm{PL}^{3}}{\mathrm{EI}}$
(C) $\frac{\mathrm{PL}^{3}}{\mathrm{EI}}$
(D) $\frac{4}{3} \frac{\mathrm{PL}^{3}}{\mathrm{EI}}$

Answer: (D)

Exp: $\quad$ Strain energy $(E)=\int_{0}^{L} \frac{M_{x}^{2} d x}{2 E I}+\int_{0}^{L} \frac{M_{y}^{2} d x}{2 E I}$

$$
\begin{aligned}
& \mathrm{M}_{\mathrm{X}}=\mathrm{PX} \quad \mathrm{M}_{\mathrm{Y}}=\mathrm{PL} \\
& \frac{1}{2} \mathrm{P} \delta=\int_{0}^{\mathrm{L}} \frac{(\mathrm{PX})^{2} \mathrm{dx}}{2 \mathrm{EI}}+\int_{0}^{\mathrm{L}(\mathrm{PL})^{2} \mathrm{dx}} \\
& 2 \mathrm{EI}
\end{aligned} \mathrm{P}^{2}\left[\frac{\mathrm{X}^{3}}{6}\right]_{0}^{\mathrm{L}}+\frac{\mathrm{P}^{2} \mathrm{~L}^{2}}{2 \mathrm{EI}}[\mathrm{X}]_{0}^{\mathrm{L}}=\frac{2}{3} \frac{\mathrm{P}^{2} \mathrm{~L}^{3}}{\mathrm{EI}}=\frac{1}{2} \times \mathrm{P} \times \frac{4}{3} \frac{\mathrm{PL}^{3}}{\mathrm{EI}} .
$$

37. A wardrobe (mass 100 kg , height 4 m , width 2 m , depth 1 m ), symmetric about the $\mathrm{Y}-\mathrm{Y}$ axis, stands on a rough level floor as shown in the figure. A force P is applied at mid-height on the wardrobe so as to tip it about point Q without slipping. What are the minimum values of the force (in Newton) and the static coefficient of friction $\mu$ between the floor and the wardrobe, respectively?

(A) 490.5 and 0.5
(B) 981 and 0.5
(C) 1000.5 and 0.15
(D) 1000.5 and 0.25

Answer: (A)
Exp: Taking moments about $\mathrm{Q}, \sum \mathrm{M}_{\mathrm{Q}}=0$
$\Rightarrow \mathrm{W} \times 1 \mathrm{~m}=\mathrm{P} \times 2 \mathrm{~m}$
$\Rightarrow \mathrm{P}=\frac{100 \times 9.81}{2}=490.5 \mathrm{~N}$
$\sum \mathrm{H}=0$
$\Rightarrow \mathrm{F}_{\mathrm{F}}=\mathrm{P}=490.5 \mathrm{~N}$
$\sum \mathrm{V}=0 \Rightarrow \mathrm{R}_{\mathrm{N}}=\mathrm{mg}=981 \mathrm{~N}$
Friction Force $=\mu R_{N}$
$\mu=\frac{490.5}{981}=0.5$
38. Torque and angular speed data over one cycle for a shaft carrying a flywheel are showi figures. The moment of inertia (in $\mathrm{kg} . \mathrm{m}^{2}$ ) of the flywheel is $\qquad$


Angular speed


Answer: 30 to 32
Exp: $\omega=\frac{\omega_{\max }+\omega_{\min }}{2}=\frac{20+0}{2}=10$
$\mathrm{C}_{\mathrm{s}}=\frac{\omega_{\text {max }}-\omega_{\text {min }}}{\omega}=\frac{20-0}{10}=2$
$\Delta \overline{\mathrm{E}}=$ Area of T - $\theta$ diagram $=\frac{\pi}{2} \times 3000+1500 \times \pi=3000 \pi$
$\Delta \mathrm{E}=\mathrm{I} \omega^{2} \mathrm{C}_{\mathrm{s}}$
$\Rightarrow 3000 \pi=\mathrm{I}(10)^{2} \times 2$ Engineering SUCCESS
$\Rightarrow \mathrm{I}=47.12$
39. A single degree of freedom system has a mass of 2 kg , stiffness $8 \mathrm{~N} / \mathrm{m}$ and viscous damping ratio 0.02 . The dynamic magnification factor at an excitation frequency of $1.5 \mathrm{rad} / \mathrm{s}$ is

Answer: 2.0 to 2.4
Exp: Damping ratio $=0.02=\frac{C}{2 \mathrm{~m} \omega_{\mathrm{n}}}=\frac{C}{2 \times 8 \times \sqrt{\frac{\mathrm{S}}{\mathrm{m}}}}$

$$
\Rightarrow \mathrm{C}=0.02 \times 2 \times 8 \times \sqrt{\frac{8}{8}}=0.32
$$

$$
\text { Dynamic magnification factor }=\frac{1}{\sqrt{\frac{c^{2} \omega^{2}}{s^{2}}+\left(1-\frac{\omega^{2}}{\omega_{\mathrm{n}}^{2}}\right)^{2}}}
$$

$$
=\frac{1}{\sqrt{\frac{(0.32)^{2} \times(1.5)^{2}}{(8)^{2}}+\left[1-\frac{(1.5)^{2}}{(1)^{2}}\right]}}=0.799
$$

40. A ladder $A B$ of length 5 m and weight $(W) 600 \mathrm{~N}$ is resting against a wall. Ass frictionless contact at the floor $(B)$ and the wall $(A)$, the magnitude of the force P (in New required to maintain equilibrium of the ladder is $\qquad$


Exp: Taking moments about B

$$
\sum \mathrm{M}_{\mathrm{B}}=0
$$

$\Rightarrow \mathrm{W} \times 2=\mathrm{R}_{\mathrm{A}} \times 3$
$\Rightarrow \mathrm{R}_{\mathrm{A}}=\frac{600 \times 2}{3}=400$
$\sum \mathrm{H}=0 \Rightarrow \mathrm{R}_{\mathrm{A}}=\mathrm{P}=400 \mathrm{~N}$
41. A closed system contains 10 kg of saturated liquid ammonia at $10^{\circ} \mathrm{C}$. Heat addition required to convert the entire liquid into saturated vapour at a constant pressure is 16.2 MJ. If the entropy of the saturated liquid is $0.88 \mathrm{~kJ} / \mathrm{kg} . \mathrm{K}$, the entropy (in $\mathrm{kJ} / \mathrm{kg} . \mathrm{K}$ ) of saturated vapour is

Answer: 6.4 to 6.7
Exp: $\quad$ Tds $=\mathrm{du}+\mathrm{pdv}($ closed system $)$
$283.15 \times 10\left(\mathrm{~S}_{2}-\mathrm{S}_{1}\right)=16.2 \times 10^{3}$
$\therefore \mathrm{S}_{2}=0.88+\frac{16.2 \times 10^{3}}{283.15 \times 10}=6.6013 \mathrm{~kJ} / \mathrm{kg}$
42. A plane wall has a thermal conductivity of $1.15 \mathrm{~W} / \mathrm{m}$. K . If the inner surface is at $1100^{\circ} \mathrm{C}$ and the outer surface is at $350^{\circ} \mathrm{C}$, then the design thickness (in meter) of the wall to maintain a steady heat flux of $2500 \mathrm{~W} / \mathrm{m}^{2}$ should be $\qquad$
Answer: 0.33 to 0.35
Exp: $Q=K A \frac{d T}{d x}$
$\mathrm{q}=\frac{\mathrm{Q}}{\mathrm{A}}=2500 \mathrm{~W} / \mathrm{m}^{2}$
$2500=\mathrm{K} \frac{\mathrm{dT}}{\mathrm{dx}}$
$2500=1.15 \times \frac{(1100-350)}{x}$
$\mathrm{x}=0.345 \mathrm{~m}$.
43. Consider the following statements regarding streamline(s):
(i) It is a continuous line such that the tangent at any point on it shows the velocity vecto that point
(ii) There is no flow across streamlines
(iii) $\frac{\mathrm{dx}}{\mathrm{u}}=\frac{\mathrm{dy}}{\mathrm{v}}=\frac{\mathrm{dz}}{\mathrm{w}}$ is the differential equation of a streamline, where $u, v$ and w are velocities in directions $x, y$ and $z$, respectively
(iv) In an unsteady flow, the path of a particle is a streamline

Which one of the following combinations of the statements is true?
(A) (i), (ii), (iv)
(B) (ii), (iii), (iv)
(C) (i), (iii), (iv)
(D) (i), (ii), (iii)

Answer: (D)
44. Consider a velocity field $\overrightarrow{\mathrm{V}}=\mathrm{K}(y \hat{i}+x \hat{\mathrm{k}})$, where K is a constant. The vorticity, $\Omega_{z}$, is
(A) -K
(B) K
(C) $-\mathrm{K} / 2$
(D) K /2

Answer: (A)
Exp: $\Omega_{z}=\frac{\partial v}{\partial x}-\frac{\partial u}{\partial y}$


45 Water flows through a tube of diameter 25 mm at an average velocity of $1.0 \mathrm{~m} / \mathrm{s}$. The properties of water $\rho=1000 \mathrm{~kg} / \mathrm{m}^{3}, \mu=7.25 \times 10^{-4} \mathrm{~N} . \mathrm{s} / \mathrm{m}^{2}, \mathrm{k}=0.625 \mathrm{~W} / \mathrm{mK}, \operatorname{Pr}=4.85$. Using $\mathrm{Nu}=0.023 \mathrm{Re}^{0.8} \mathrm{Pr}^{0.4}$, the convective heat transfer coefficient (in $\mathrm{W} / \mathrm{m}^{2} . \mathrm{K}$ ) is $\qquad$
Answer: 4600 to 4625
Exp: $\quad \operatorname{Re}=\frac{\rho V D}{\mu}=\frac{1000 \times 1 \times 25 \times 10^{-3}}{7.25 \times 10^{-4}}=34482.758$
$\operatorname{Pr}=4.85$
$\mathrm{Nu}=0.023 \quad \mathrm{Re}^{0.8} \mathrm{Pr}^{0.4}=184.5466=\frac{\mathrm{hD}}{\mathrm{k}}$
$\therefore \mathrm{h}=\frac{184.5466 \times 0.625}{25 \times 10^{-3}}=4613.6659 \mathrm{~W} / \mathrm{m}^{2} \mathrm{k}$.
46. Two identical metal blocks L and M (specific heat $=0.4 \mathrm{~kJ} / \mathrm{kg} . \mathrm{K}$ ), each having a mass of 5 kg , are initially at 313 K . A reversible refrigerator extracts heat from block L and rejects heat to block M until the temperature of block L reaches 293 K . The final temperature (in K) of block M is $\qquad$
Answer: 333 to 335
Exp: Given $\mathrm{m}_{1}=\mathrm{m}_{2}=5 \mathrm{Kg}$

$$
\begin{aligned}
& \mathrm{c}_{1}=\mathrm{c}_{2}=0.4 \mathrm{KJ} / \mathrm{Kg} \cdot \mathrm{~K} \\
& \mathrm{~T}_{\mathrm{L}, \mathrm{i}}=\mathrm{T}_{\mathrm{M}, \mathrm{i}}=313 \mathrm{~K} \\
& \mathrm{~T}_{\mathrm{M}, \mathrm{f}}=293 \mathrm{~K}, \mathrm{~T}_{\mathrm{L}, \mathrm{f}}=? \\
& \mathrm{~m}_{1} \mathrm{c}_{1} \Delta \mathrm{~T}_{1}=\mathrm{m}_{2} \mathrm{c}_{2} \Delta \mathrm{~T}_{2} \\
& \Delta \mathrm{~T}_{1}=\Delta \mathrm{T}_{2} \\
& \mathrm{~T}_{\mathrm{L}, \mathrm{i}}-\mathrm{T}_{\mathrm{L}, \mathrm{f}}=\mathrm{T}_{\mathrm{M}, \mathrm{i}}-\mathrm{T}_{\mathrm{M}, \mathrm{f}} \\
& 313-\mathrm{T}_{\mathrm{L}, \mathrm{f}}=313-293 \\
& \mathrm{~T}_{\mathrm{L}, \mathrm{f}}=333 \mathrm{k}
\end{aligned}
$$

47. Steam with specific enthalpy (h) $3214 \mathrm{~kJ} / \mathrm{kg}$ enters an adiabatic turbine operating at steady state with a flow rate $10 \mathrm{~kg} / \mathrm{s}$. As it expands, at a point where h is $2920 \mathrm{~kJ} / \mathrm{kg}, 1.5 \mathrm{~kg} / \mathrm{s}$ is extracted for heating purposes. The remaining $8.5 \mathrm{~kg} / \mathrm{s}$ further expands to the turbine exit, where $h=2374 \mathrm{~kJ} / \mathrm{kg}$. Neglecting changes in kinetic and potential energies, the net power output (in kW ) of the turbine is $\qquad$
Answer: 7580 to 7582

Exp:

48. Two infinite parallel plates are placed at a certain distance apart. An infinite radiation shield is inserted between the plates without touching any of them to reduce heat exchange between the plates. Assume that the emissivities of plates and radiation shield are equal. The ratio of the net heat exchange between the plates with and without the shield is
(A) $1 / 2$
(B) $1 / 3$
(C) $1 / 4$
(D) $1 / 8$

Answer: (A)
Exp: $\quad \frac{\mathrm{q}_{\text {with sheilds }}}{\mathrm{q}_{\text {without sheilds }}}=\frac{1}{\mathrm{n}+1}$
here, $\mathrm{n}=1$
$\therefore \frac{\mathrm{q}}{\mathrm{q}_{\text {without }}}=\frac{1}{2}$.
49. In a compression ignition engine, the inlet air pressure is 1 bar and the pressure at the end of isentropic compression is 32.42 bar. The expansion ratio is 8 . Assuming ratio of specific heats $(\gamma)$ as 1.4 , the air standard efficiency (in percent) is $\qquad$
Answer: 59 to 61

Exp: compression ratio, $\mathrm{r}_{\mathrm{k}}=\frac{\mathrm{v}_{1}}{\mathrm{v}_{2}}=\left(\frac{\mathrm{p}_{2}}{\mathrm{p}_{1}}\right)^{\frac{1}{\gamma}}=(32.42)^{\frac{1}{1.4}}=11.999 .9 \simeq 12$
cutoff ratio, $\mathrm{r}_{\mathrm{k}}=\frac{\text { compression ratio }}{\text { expansion ratio }}=\frac{12}{8}=1.5$

$$
\begin{aligned}
& \eta=1-\frac{1}{r_{k}^{\gamma-1}}\left(\frac{r_{e}^{\gamma}-1}{\gamma\left(r_{c}-1\right)}\right) \\
& =1-\frac{1}{12^{0.4}}\left(\frac{(1.5)^{1.4}-1}{1.4(1.5-1)}\right) \\
& \eta=59.599 \% .
\end{aligned}
$$

50. The precedence relations and duration (in days) of activities of a project network are given in the table. The total float (in days) of activities e and $f$, respectively, are

| Activity | Predecessors | Duration (days) |
| :---: | :---: | :---: |
| a | - | 2 |
| b | - | 4 |
| c | a | 2 |
| d | E | bincering |
| e | b | 3 |
| f | c | 2 |
| g | $\mathrm{~d}, \mathrm{e}$ | 4 |

(A) 0 and 4
(B) 1 and 4
(C) 2 and 3
(D) 3 and 1

Answer: (B)
Exp:

$(T F)_{e}=\left(L_{j}-E_{i}\right)-T_{i j}=(7-4)-2=1$
$(\mathrm{TF})_{\mathrm{f}}=(8-0)-4=4$
51. At a work station, 5 jobs arrive every minute. The mean time spent on each job in th station is $1 / 8$ minute. The mean steady state number of jobs in the system is $\qquad$
Answer: 1.62 to 1.70
52. A GO-No GO plug gauge is to be designed for measuring a hole of nominal diameter 25 mm with a hole tolerance of $\pm 0.015 \mathrm{~mm}$. Considering $10 \%$ of work tolerance to be the gauge tolerance and no wear condition, the dimension (in mm ) of the GO plug gauge as per the unilateral tolerance system is
(A) $24.985_{-0.003}^{+0.003}$
(B) $25.015_{-0.006}^{+0.000}$
(C) $24.985_{-0.003}^{+0.003}$
(D) $24.985_{-0.000}^{+0.003}$

Answer: (D)
Exp: $25 \pm 0.015$
$\mathrm{G}_{\mathrm{o}}$-Gauge
$\mathrm{U} . \mathrm{L}=24.988$
L. $\mathrm{L}=24.985$
$24.985_{-0.000}^{+0.003}$

24.985
53. A cylindrical riser of 6 cm diameter and 6 cm height has to be designed for a sand casting mould for producing a steel rectangular plate casting of $7 \mathrm{~cm} \times 10 \mathrm{~cm} \times 2 \mathrm{~cm}$ dimensions having the total solidification time of 1.36 minute. The total solidification time (in minute) of the riser is $\qquad$
Answer: 2.5 to 4.5
54. A cast iron block of 200 mm length is being shaped in a shaping machine with a depth of cut of 4 mm , feed of $0.25 \mathrm{~mm} /$ stroke and the tool principal cutting edge angle of $30^{\circ}$. Number of cutting strokes per minute is 60 . Using specific energy for cutting as $1.49 \mathrm{~J} / \mathrm{mm}^{3}$, the average power consumption (in watt) is $\qquad$
Answer: 295 to 305
Exp: $\quad$ Specific cutting energy $=\frac{\mathrm{F}_{\mathrm{C}}}{\mathrm{b} \times \mathrm{t}_{1}}=1.49 \mathrm{~J} / \mathrm{mm}^{3}=\frac{\mathrm{F}_{\mathrm{C}}}{4 \times 0.25}$
$\mathrm{F}_{\mathrm{C}}=1.49 \mathrm{~J} / \mathrm{mm}$. stroke
$\mathrm{F}_{\mathrm{C}}=1.49 \mathrm{~J} / \mathrm{mm} \times \frac{60}{\min }$
$\mathrm{F}_{\mathrm{C}}=89.4 \mathrm{~J} / \mathrm{mm} . \mathrm{min}$
Power $=\mathrm{F}_{\mathrm{C}} . \mathrm{l}=89.4 \times 200 \mathrm{~mm} \mathrm{~J} / \mathrm{mm} \cdot \mathrm{min}=17880 \mathrm{~J} / \mathrm{min}$
Power $=298 \mathrm{~J} / \mathrm{S}$ or $(\mathrm{W})$.
55. A butt weld joint is developed on steel plates having yield and ultimate tensile strength MPa and 700 MPa , respectively. The thickness of the plates is 8 mm and width is 20 Improper selection of welding parameters caused an undercut of 3 mm depth along the welo The maximum transverse tensile load (in kN ) carrying capacity of the developed weld joint is

Answer: 68 to 72
Exp: $\quad t=8 \mathrm{~mm}$
$\mathrm{b}=20 \mathrm{~mm}$
$\mathrm{d}=3 \mathrm{~mm}$
maximum transverse tensile load $=$ yield strength $\times(b-d) t$

$$
\begin{aligned}
& =500 \mathrm{~N} / \mathrm{mm}^{2} \times(20-3) \times 5 \mathrm{~mm}^{2} \\
& =68,000 \mathrm{~N} \\
& =68 \mathrm{kN} .
\end{aligned}
$$



