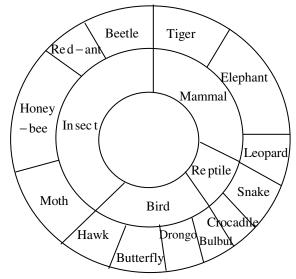
### Q. No. 1 – 5 Carry One Mark Each

				Stu	
G	ATEFORUM	EC-GATE-	2014 PAPER-03	WWW.	
		Q. No. 1 – 5 Car	rry One Mark Each	Boun	
1.	best supports the c (A) India is a unic (B) India has a po (C) India is home (D) The Indian cr	claim made in the above on of 28 states and 7 un pulation of over 1.1 bil	e sentence? ion territories. lion. s and thousands of diale	www. www. ch one of the following facts	1.com
Answ		0.1100			
Exp:	Diversity is show	n in terms of difference	language		
2.	Rupee has	·		ed to 60 last year. The Indian	
Answ	(A) Depressed	(B) Depreciated	(C) Appreciated	(D) Stabilized	
Allsw	сі. Б				
3.	'Advice' is				
	(A) a verb		(B) a noun		
	(C) an adjective		(D) both a verb and	a noun	
Answ	er: B	Engine	ering Suc	cess	
4.	The next term in t	he series 81, 54, 36, 24	is		
Answ	er: 16				
Exp:	81-54=27;27×	$\frac{2}{3} = 18$			
	54-36=18;18×				
	36-24=12;12×-	$\frac{2}{3} = 8$			
	$\therefore 24 - 8 = 16$	J			
5.	In which of the fo	llowing options will the	e expression P < M be d	efinitely true?	
	(A) $M < R > P > S$	S	(B) $M > S < P < F$		
	(C) $Q < M < F = 1$	P	(D) $P = A < R < M$		
Answ	er: D				
		Q. No. 6 – 10 Car	rry Two Marks Each		
6	Find the next term	in the sequence 70 1	1V 12M		
6.	(A) 15Q	n in the sequence: 7G, 1 (B) 17Q	(C) 15P	(D) 17P	
	(1) 10 X		$(\bigcirc)$ 151		

Answer: B

# www.StudentBounty.com Homework Help & Pastpapers

ve fores output com 7. The multi-level hierarchical pie chart shows the population of animals in a reserve fore. correct conclusions from this information are:



(i) Butterflies are birds

(ii) There are more tigers in this forest than red ants

(iii) All reptiles in this forest are either snakes or crocodiles

- (iv) Elephants are the largest mammals in this forest
- (i) (i), (ii), (iii) and (iv) (A) (i) and (ii) only
- (D) (i), (ii) and (iii) only (C) (i), (iii) and (iv) only

### Answer: D

### Exp: It is not mentioned that elephant is the largest animal

8. A man can row at 8 km per hour in still water. If it takes him thrice as long to row upstream, as to row downstream, then find the stream velocity in km per hour.

## Answer: 4

Exp: 4 km/hr.

> Speed of man=8 Left distance =d

Time taken=
$$\frac{d}{8}$$

Upstream:

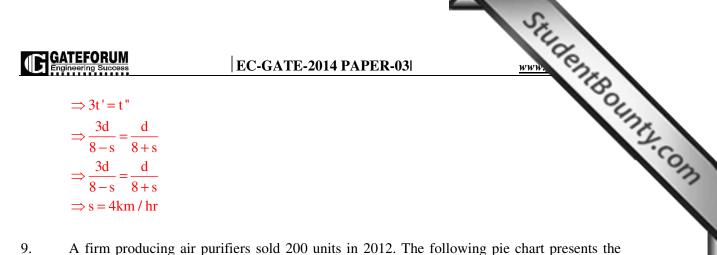
Speed of stream=s

 $\Rightarrow$  speed upstream = S' = (8 - s)

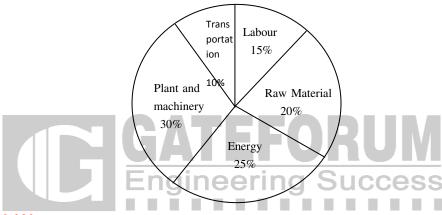
$$t' = \left(\frac{d}{8-s}\right)$$

Downstream:

Given speed downstream =  $t'' = \frac{d}{8+s}$ 



A first producing an purfilers sold 200 units in 2012. The following pie chart presents the share of raw material, labour, energy, plant & machinery, and transportation costs in the total manufacturing cost of the firm in 2012. The expenditure on labour in 2012 is Rs. 4,50,000. In 2013, the raw material expenses increased by 30% and all other expenses increased by 20%. If the company registered a profit of Rs. 10 lakhs in 2012, at what price (in Rs.) was each air purifier sold?



Answer: 20,000

Exp:

Total expenditure=
$$=\frac{15}{100}x = 4,50,000$$
  
 $x=3\times10^{6}$   
Profit=10 lakhs  
So, total selling price =40,00,000 ... (1)  
Total purifies=200 ... (2)  
S.P of each purifier=(1)/(2)=20,000

10. A batch of one hundred bulbs is inspected by testing four randomly chosen bulbs. The batch is rejected if even one of the bulbs is defective. A batch typically has five defective bulbs. The probability that the current batch is accepted is \_\_\_\_\_

.)

### Answer: 0.8145

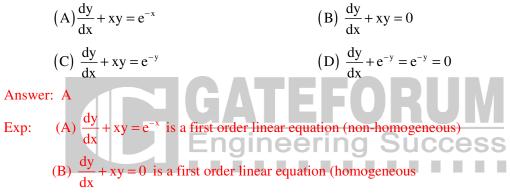
- Exp: Probability for one bulb to be non defective is  $\frac{95}{100}$ 
  - :. Probabilities that none of the bulbs is defectives  $\left(\frac{95}{100}\right)^4 = 0.8145$

### Q.No. 1 - 25 Carry One Mark Each

StudentBounty.com 1. The maximum value of the function  $f(x) = \ln(1 + x) - x$  (where x > -1) occurs at x =Answer: 0

 $f^{1}(x) = 0 \Rightarrow \frac{1}{1+x} - 1 = 0$ Exp:  $\Rightarrow \frac{-x}{1+x} = 0 \Rightarrow x = 0$ and  $f^{11}(x) = \frac{-1}{(1+x)^2} < 0$  at x = 0

2. Which ONE of the following is a linear non-homogeneous differential equation, where x and y are the independent and dependent variables respectively?



(C), (D) are non linear equations

### 3. Match the application to appropriate numerical method.

Application	Numerical  Method		
P1: Numerical integration	M1: Newton-Raphson Method		
P2: Solution to a transcendental equation	M2: Runge-Kutta Method		
P3: Solution to a system of linear equations	M3: Simpson's 1/3-rule		
P4: Solution to a differential equation	M4: Gauss Elimination Method		
.) P1—M3, P2—M2, P3—M4, P4—M1 (B) P1—M3, P2—M1, P3—M4, P4—M2			
(C) P1—M4, P2—M1, P3—M3, P4—M2 (D) P1—M2, P2—M1, P3—M3, P4—M4			

Answer: B

Exp: P1-M3, P2-M1, P3-M4, P4-M2

4. An unbiased coin is tossed an infinite number of times. The probability that the fourth head appears at the tenth toss is

```
(A) 0.067
                                            (C) 0.082
                                                                     (D) 0.091
                      (B) 0.073
```

# GATEFORUN

## EC-GATE-2014 PAPER-03

### Answer: C

www. and culture.com Exp: P[fourth head appears at the tenth toss] = P [getting 3 heads in the first 9 tosses andhead at tenth toss]

$$= \left[9_{C_3} \cdot \left(\frac{1}{2}\right)^9\right] \times \left[\frac{1}{2}\right] = \frac{21}{256} = 0.082$$

5. If 
$$z = xyln(xy)$$
, then

(A) 
$$x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = 0$$
  
(B)  $y \frac{\partial z}{\partial x} = x \frac{\partial z}{\partial y}$   
(C)  $x \frac{\partial z}{\partial x} = y \frac{\partial z}{\partial y}$   
(D)  $y \frac{\partial z}{\partial x} + x \frac{\partial z}{\partial y} = 0$ 

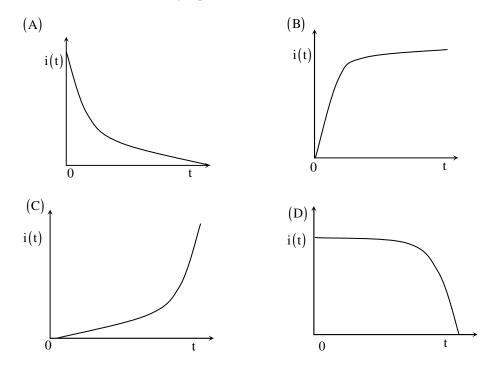
Answer: C

Exp: 
$$\frac{\partial z}{\partial x} = y \left[ x \times \frac{1}{xy} \times y + \ln xy \right] = y (1 + \ln xy)$$
  
and  $\frac{\partial z}{\partial y} = x (1 + \ln xy) \Longrightarrow x \frac{\partial z}{\partial x} = y \frac{\partial z}{\partial y}$ 

A series RC circuit is connected to a DC voltage source at time t = 0. The relation between 6. the source voltage  $V_s$ , the resistance R, the capacitance C, and the current i(t) is given below:

$$V_{e} = Ri(t) + \frac{1}{c} \int_{0}^{t} i(u) du$$

Which one of the following represents the current f(t)?



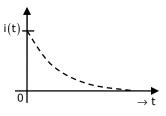
www.StudentBounty.com Help & Pas

### Answer: A

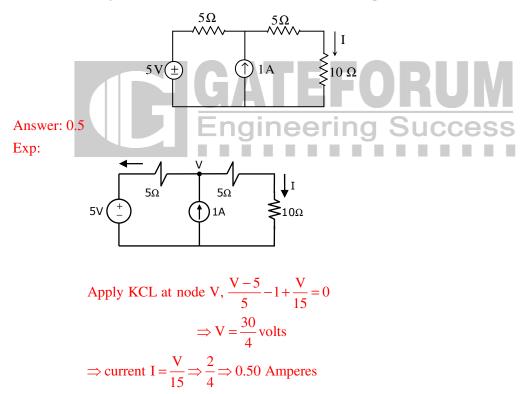
In a series RC circuit, Exp:

WWW REINBOUINTY.Com  $\rightarrow$  Initially at t = 0, capacitor charges with a current of  $\frac{V_s}{R}$  and in steady state at t =  $\infty$ , capacitor behaves like open circuit and no current flows through the circuit

 $\rightarrow$  So the current i(t) represents an exponential decay function



In the figure shown, the value of the current I (in Amperes) is \_\_\_\_\_ 7.



- 8. In MOSFET fabrication, the channel length is defined during the process of
  - (A) Isolation oxide growth
  - (B) Channel stop implantation
  - (C) Poly-silicon gate patterning
  - (D) Lithography step leading to the contact pads

Answer: C

## EC-GATE-2014 PAPER-03|

- vww. rates vrates 9. A thin P-type silicon sample is uniformly illuminated with light which generates carriers. The recombination rate is directly proportional to (A) The minority carrier mobility (B) The minority carrier recombination lifetime
  - (C) The majority carrier concentration
  - (D) The excess minority carrier concentration

### Answer: D

- Recombination rate,  $R = B(n_{n_{\alpha}} + n_{n}')(P_{n_{\alpha}} + P_{n}')$ Exp:
  - $n_{n_0} \& P_{n_0}$  = Electron and hole concentrations respectively under thermal equilibrium

 $n'_n \& p'_n = Excess$  elements and hole concentrations respectively

At T = 300 K, the hole mobility of a semiconductor  $\mu_{\rm p} = 500 \,{\rm cm}^2 \,/\,{\rm V} - {\rm s}$  and  $\frac{{\rm kT}}{a} = 26 \,{\rm mV}$ . 10.

The hole diffusion constant  $D_p$  in cm<sup>2</sup>/s is \_\_\_\_\_

### Answer: 13

From Einstein relation, Exp:

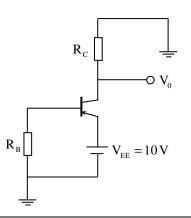
> $\Rightarrow$  D<sub>p</sub> = 26 mV × 500 cm<sup>2</sup> / Engineering S

- The desirable characteristics of a transconductance amplifier are 11.
  - (A) High input resistance and high output resistance
  - (B) High input resistance and low output resistance
  - (C) Low input resistance and high output resistance
  - (D) Low input resistance and low output resistance

### Answer: A

Transconductance amplifier must have  $z_i = \infty$  and  $z_0 = \infty$  ideally Exp:

In the circuit shown, the PNP transistor has  $|V_{BE}| = 0.7$  and  $\beta = 50$ . Assume that  $R_B = 100 k\Omega$ 12. For V<sub>0</sub> to be 5 V, the value of  $R_{c}(in k\Omega)$ 



### GATEFORUM Engineering Success

### EC-GATE-2014 PAPER-03

WWW CHIBOUNES.com

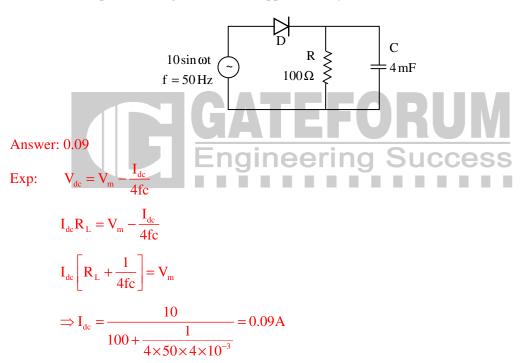
Answer: 1.075

Exp: KVL in base loop gives,

$$I_{B} = \frac{10 - 0.7}{100 \text{K}} = 93 \mu \text{A}$$
  
$$\Rightarrow I_{C} = \beta I_{B} = 50 \times 93 \mu \text{A} = 4.65 \text{ mA}$$
  
from figure,  $V_{0} = I_{C} R_{C}$ 

 $\Rightarrow R_c = \frac{V_0}{I_c} = \frac{5V}{4.65 \text{ mA}} = 1.075 \Omega$ 

13. The figure shows a half-wave rectifier. The diode D is ideal. The average steady-state current (in Amperes) through the diode is approximately \_\_\_\_\_.



14. An analog voltage in the range 0 to 8 V is divided in 16 equal intervals for conversion to 4-bit digital output. The maximum quantization error (in V) is \_\_\_\_\_

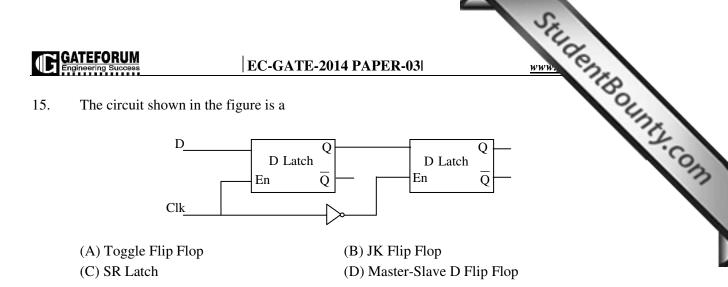
Answer: 0.25

Exp: Maximum quantization error is 
$$\frac{\text{step} - \text{size}}{2}$$

step - size = 
$$\frac{8-0}{16} = \frac{1}{2} = 0.5$$
V

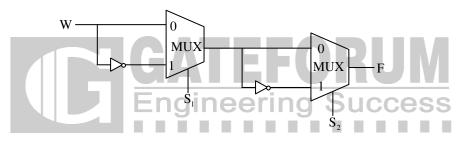
Quantization error = 0.25 V

### www.StudentBounty.com Homework Help & Pastpapers



Answer: D

- Exp: Latches are used to construct Flip-Flop. Latches are level triggered, so if you use two latches in cascaded with inverted clock, then one latch will behave as master and another latch which is having inverted clock will be used as a slave and combined it will behave as a flip-flop. So given circuit is implementing Master-Slave D flip-flop
- 16. Consider the multiplexer based logic circuit shown in the figure.



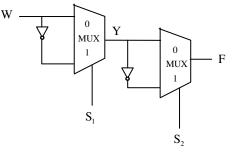
Which one of the following Boolean functions is realized by the circuit?

(A)  $F = W\overline{S}_1 \overline{S}_2$  (B)  $F = WS_1 + WS_2 + S_1S_2$ 

(C) 
$$F = W + S_1 + S_2$$
 (D)  $F = W \oplus S_1 \oplus S_2$ 

Answer: D

Exp:



Output of first MUX =  $w\overline{s}_1 + \overline{w}s_1 = w \oplus s_1$ Let  $Y = w \oplus s_1$ 

Output of second MUX =  $Y\overline{s}_2 + \overline{Y}s_2$ 

$$= Y \oplus s_2$$
$$= w \oplus s_2 + z_2$$

$$= \mathbf{w} \oplus \mathbf{s}_1 + \mathbf{s}_2$$

StudentBounts.com 17. Let  $x(t) = cos(10\pi t) + cos(30\pi t)$  be sampled at 20 Hz and reconstructed using an idea pass filter with cut-off frequency of 20 Hz. The frequency/frequencies present in reconstructed signal is/are

(A) 5 Hz and 15 Hz only

(C) 5 Hz, 10 Hz and 15 Hz only

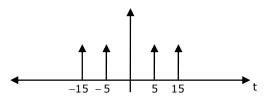
(B) 10 Hz and 15 Hz only

- (D) 5 Hz only

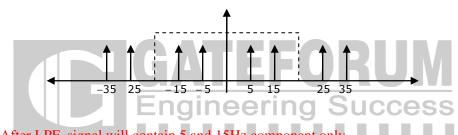
Answer: (A)

Explanation:  $x(t) = cos(10\pi t) + cos(30\pi t)$ ,  $F_{e} = 20Hz$ 

Spectrum of x(t)



Spectrum of sampled version of x(t)



After LPF, signal will contain 5 and 15Hz component only

system  $H(z) = \frac{(z^{-1} - b)}{(1 - az^{-1})}$ , where  $|H(e^{-j\omega})| = 1$ , for all 18. all-pass For ω.If an  $\operatorname{Re}(a) \neq 0$ ,  $\operatorname{Im}(a) \neq 0$ , then b equals (A) a (B) a\* (C) 1/a\* (D) 1/a Answer: (B) For an all pass system, pole =  $\frac{1}{\text{zero}^*}$  or zero =  $\frac{1}{\text{pole}^*}$ Exp: pole = azero – 1

$$\Rightarrow \frac{1}{b} = \frac{1}{a^*} \text{ or } b = a^*$$

19. A modulated signal is  $y(t) = m.(t)\cos(40000 \pi t)$ , where the baseband signal m(t) has frequency components less than 5 kHz only. The minimum required rate (in kHz) at which y(t) should be sampled to recover m(t) is \_\_\_\_\_\_.

GATEFORUM

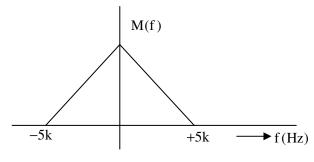
f

m(t) —

► M(f)

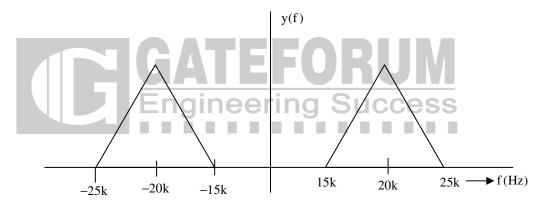
Answer: 10 KHz.

www. reads Exp: Since m(t) is a base band signal with maximum frequency 5 KHz, assumed spread follows:



∴ y(t) = m(t) cos(40000 π t) 
$$\xrightarrow{7}$$
 m(f)  $\stackrel{*1}{2}$  [δ(f - 20k) + δ(f + 20k)]  
∴ y(f) =  $\frac{1}{2}$  [M(f - 20k) + M(f + 20k)]

Thus the spectrum of the modulated signal is as follows:

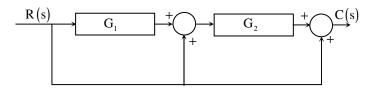


If y(t) is sampled with a sampling frequency 'f<sub>s</sub>' then the resultant signal is a periodic extension of successive replica of y(f) with a period 'fs'.

It is observed that 10 KHz and 20 KHz are the two sampling frequencies which causes a replica of M(f) which can be filtered out by a LPF.

Thus the minimum sampling frequency  $(f_s)$  which extracts m(t) from g(f) is 10 KHz.

20. Consider the following block diagram in the figure.



The transfer function  $\frac{C(s)}{R(s)}$  is

(A) 
$$\frac{G_1G_2}{1+G_1G_2}$$
 (B)  $G_1G_2+G_1+1$  (C)  $G_1G_2+G_2+1$  (D)  $\frac{G_1}{1+G_1G_2}$ 

GATEFORUM

NOR COMPANY COM

### Answer: C

Exp: By drawing the signal flow graph for the given block diagram

Number of parallel paths are three Gains  $P_1 = G_1G_2, P_2 = G_2, P_3 = 1$ 

By mason's gain formula,

$$\frac{\mathbf{C(s)}}{\mathbf{R(s)}} = \mathbf{P}_1 + \mathbf{P}_2 + \mathbf{P}_3$$
$$\Rightarrow \mathbf{G}_1 \mathbf{G}_2 + \mathbf{G}_2 + \mathbf{1}$$

The input  $-3e^{2t}u(t)$ , where u(t) is the unit step function, is applied to a system with transfer 21. function .  $\frac{s-2}{s+3}$ . If the initial value of the output is -2, then the value of the output at steady state is\_

Answer: 0  
Exp: 1  

$$\frac{Y(s)}{X(s)} = \frac{s-2}{s+3}$$
  
Engineering Success  
 $\Rightarrow$  SY(s)+3Y(s)=S×(s)-2X(s)  
Due to initial condition, we can write above equation as  
 $Sy(s)-y(0)+3y(s)=sx(s)-x(0^{-})-2x(s)$   
 $y(0^{-})=-2, x(0^{-})=0$  [ $x(t)=3e^{2t}u(t)$ ]  
 $\Rightarrow$  Sy(s)+2+3y(s)=(s-2)( $\frac{-3}{s-2}$ )  
 $(s+3)y(s)=-3-2\Rightarrow y(s)=\frac{-5}{5+3}$   
 $\Rightarrow y(t)=-5e^{-3t}u(t)$   
 $y(\infty)(steady sate)=0$   
Exp: 2  
 $H(s)=\frac{s-2}{s+3}; X(t)=-3e^{2t}.u(t)$   
 $\therefore X(s)=\frac{-3}{3}\Rightarrow Y(s)=\frac{-3}{3}$ 

$$s-2 \qquad s+3$$

$$y(t)\Big|_{at\ t=\infty} \Rightarrow y(\infty) = \lim_{s \to 0} S.y(s) = \lim_{s \to 0} \frac{-3s}{s+3}$$

$$y(\infty) = 0$$

### EC-GATE-2014 PAPER-03

22. The phase response of a passband waveform at the receiver is given by

$$\phi(f) = -2\pi\alpha(f - f_c) - 2\pi\beta f_c$$

<u>WWW3</u> WWW3 REPAILSOUTHT,COM Where  $f_c$  is the centre frequency, and  $\alpha$  and  $\beta$  are positive constants. The actual signal propagation delay from the transmitter to receiver is

(A) 
$$\frac{\alpha - \beta}{\alpha + \beta}$$
 (B)  $\frac{\alpha \beta}{\alpha + \beta}$  (C)  $\alpha$  (D)  $\beta$ 

Answer: C

Phase response of pass band waveform Exp:

$$\phi(f) = -2\pi\alpha(f - f_c) - 2\pi\beta f_c$$
  
Group delay  $t_y = \frac{-d\phi(f)}{2\pi} df = \alpha$ 

Thus ' $\alpha$ ' is actual signal propagation delay from transmitter to receiver

Consider an FM signal  $f(t) = \cos[2\pi f_c t + \beta_1 \sin 2\pi f_1 t + \beta_2 \sin 2\pi f_2 t_1]$ . The maximum 23. deviation of the instantaneous frequency from the carrier frequency  $f_c$  is

(A) 
$$\beta_1 f_1 + \beta_2 f_2$$
  
Answer: A  
Exp: Instantaneous phase  $\phi_i(t) = 2\pi f_c t + \beta_1 \sin 2\pi f_1 + \beta_2 \sin 2\pi f_2 t$   
Instantaneous frequency  $f_i(t) = \frac{d}{dt} \phi_i(t) \times \frac{1}{2\pi}$   
 $= f_c + \beta_1 f_1 \cos 2\pi f_1 t + \beta_2 f_2 \cos 2\pi f_2 t$   
Instantaneous frequency deviation  $= \beta_1 f_1 \cos 2\pi f_1 t + \beta_2 f_2 \cos 2\pi f_2 t$ 

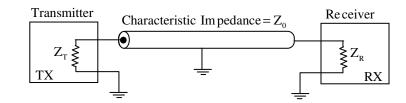
Maximum  $\Delta f = \beta_1 f_1 + \beta_2 f_2$ 

24. Consider an air filled rectangular waveguide with a cross-section of 5 cm  $\times$  3 cm. For this waveguide, the cut-off frequency (in MHz) of TE<sub>21</sub> mode is \_\_\_\_\_\_

Answer: 7810MHz.

Exp: 
$$f_{c}(TE_{21}) = \frac{C}{2} \sqrt{\left(\frac{2}{9}\right)^{2} + \left(\frac{1}{b}\right)^{2}}$$
  
 $= \frac{3 \times 10^{10}}{2} \sqrt{\left(\frac{2}{5}\right)^{2} + \left(\frac{1}{3}\right)^{2}}$   
 $= 1.5 \times 10^{10} \sqrt{0.16 + 0.111}$   
 $= 0.52 \times 1.5 \times 10^{10}$   
 $= 7.81 \text{ GHz}$   
 $= 7810 \text{ MHz}.$ 

StudentBounts.com 25. In the following figure, the transmitter Tx sends a wideband modulated RF signal coaxial cable to the receiver Rx. The output impedance  $Z_T$  of Tx, the characteristic impedance  $Z_0$  of the cable and the input impedance  $Z_R$  of Rx are all real.



Which one of the following statements is TRUE about the distortion of the received signal due to impedance mismatch?

- (A) The signal gets distorted if  $Z_R \neq Z_0$ , irrespective of the value of  $Z_T$
- (B) The signal gets distorted if  $Z_T \neq Z_0$ , irrespective of the value of  $Z_R$
- (C) Signal distortion implies impedance mismatch at both ends:  $Z_T \neq Z_0$  and  $Z_R \neq Z_0$
- (D) Impedance mismatches do NOT result in signal distortion but reduce power transfer efficiency

Answer: C

Signal distortion implies impedance mismatch at both ends. i.e Exp:  $Z_T \neq Z_0$  $Z_{R} \neq Z_{0}$ 

### Q. No. 26 - 55 Carry Two Marks Each

The maximum value of  $f(x)=2x^3-9x^2+12x-3$  in the interval  $0 \le x \le 3$  is \_\_\_\_\_. 26.

Answer: 6

 $f^{1}(x) = 6x^{2} - 18x + 12 = 0 \implies x = 1, 2 \in [0,3]$ Exp:

Now f(0) = -3; f(3) = 6 and f(1) = 2; f(2) = 1

Hence, f(x) is maximum at x = 3 and the maximum value is 6

27. Which one of the following statements is NOT true for a square matrix?

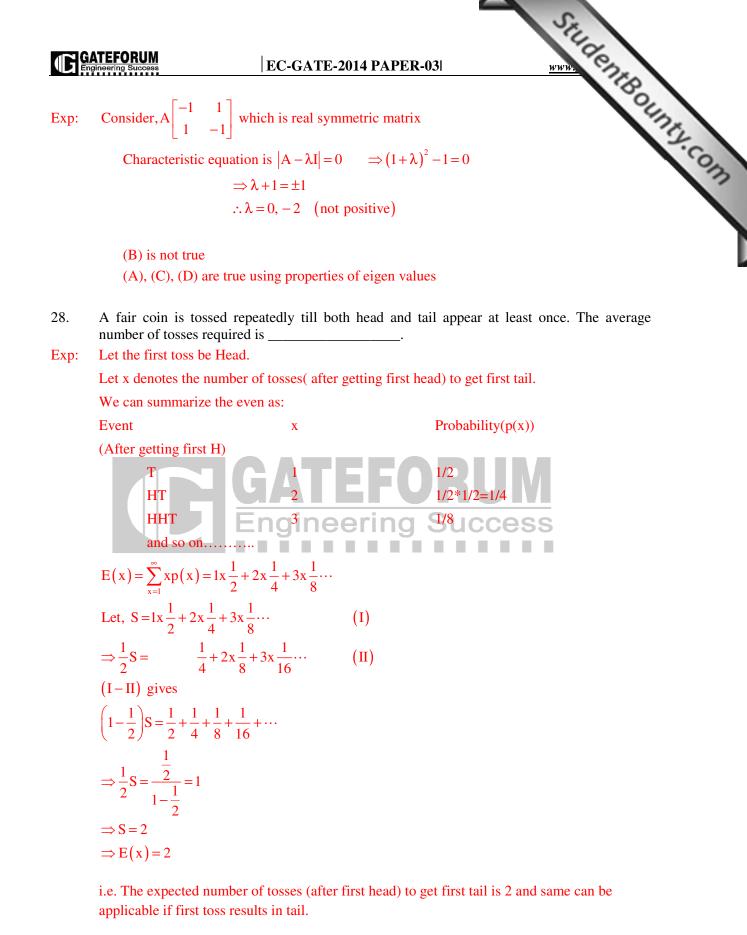
(A) If A is upper triangular, the eigenvalues of A are the diagonal elements of it

(B) If A is real symmetric, the eigenvalues of A are always real and positive

(C) If A is real, the eigenvalues of A and  $A^{T}$  are always the same

(D) If all the principal minors of A are positive, all the eigenvalues of A are also positive

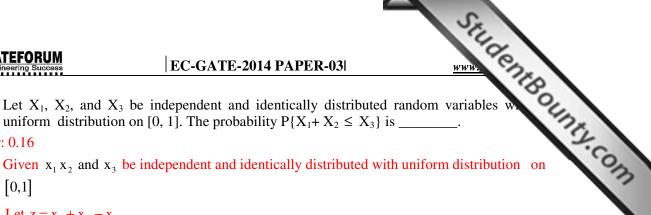
Answer: B



Hence the average number of tosses is 1+2 = 3.

### www.StudentBounty.com Homework Help & Pastpapers

### EC-GATE-2014 PAPER-03|



### Answer: 0.16

29.

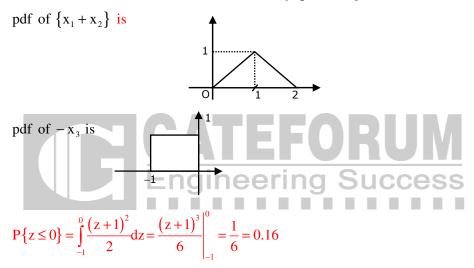
Exp: Given  $x_1 x_2$  and  $x_3$  be independent and identically distributed with uniform distribution on [0,1]

Let 
$$z = x_1 + x_2 - x_3$$
  
 $\Rightarrow P\{x_1 + x_2 \le x_3\} = P\{x_1 + x_2 - x_3 \le 0\}$   
 $= P\{z \le 0\}$ 

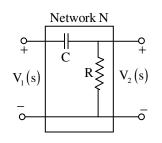
Let us find probability density function of random variable z.

Since Z is summation of three random variable  $x_1, x_2$  and  $-x_3$ 

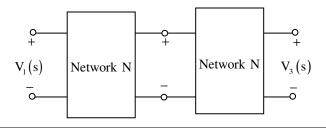
Overall pdf of z is convolution of the pdf of  $x_1 x_2$  and  $-x_3$ 



30. Consider the building block called 'Network N' shown in the figure. Let C = 100 $\mu$ F and R = 10k $\Omega$ 



Two such blocks are connected in cascade, as shown in the figure.



StudentBounty.com

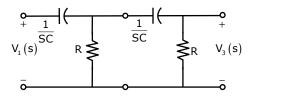
(D)  $\frac{s}{2+s}$ 

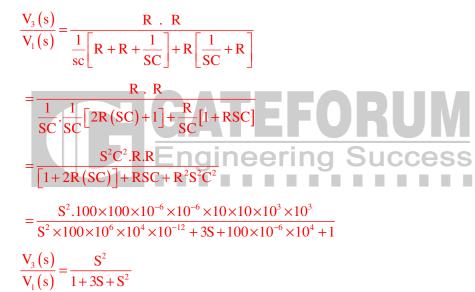
The transfer function  $\frac{v_3(s)}{v_1(s)}$  of the cascaded network is

(A) 
$$\frac{s}{1+s}$$
 (B)  $\frac{s^2}{1+3s+s^2}$  (C)  $\left(\frac{s}{1+s}\right)^2$ 

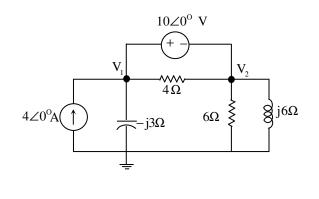
Answer: B

Exp: Two blocks are connected in cascade, Represent in s-domain,





31. In the circuit shown in the figure, the value of node voltage V<sub>2</sub> is



(A) 22 + j 2 V(B) 2 + j 22 V (C) 22 - j 2 V (D) 2 - j 22 V

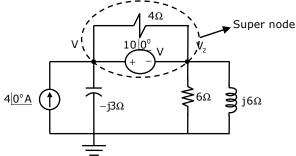
www.Student	Bounty.com
<ul> <li>Homework Help</li> </ul>	p & Pastpapers

GATEFORUM

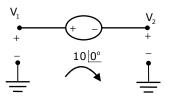
WWW Chilbounty.com

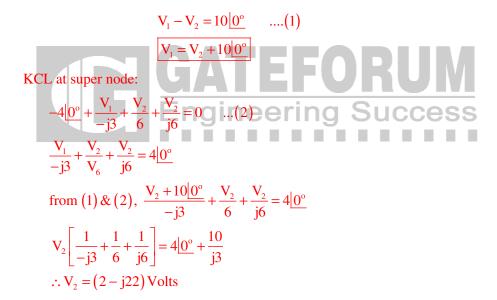


Exp:

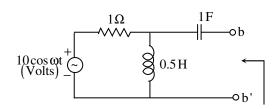


KVL for  $V_1 \& V_2$ :



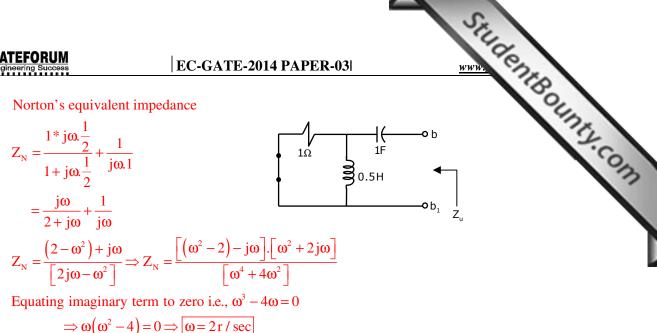


32. In the circuit shown in the figure, the angular frequency  $\omega$  (in rad/s), at which the Norton equivalent impedance as seen from terminals b-b' is purely resistive, is

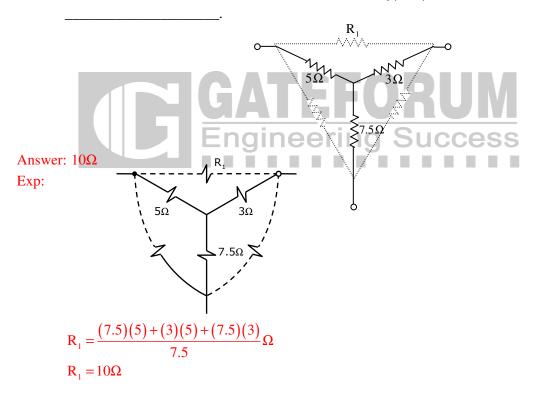


Answer: 2 r/sec

Exp: Norton's equivalent impedance



For the Y-network shown in the figure, the value of  $R_1(in\Omega)$  in the equivalent  $\Delta$ -network is 33.



The donor and accepter impurities in an abrupt junction silicon diode are  $1 \times 10^{16}$  cm<sup>-3</sup> and 5 34. x  $10^{18}$  cm<sup>-3</sup>, respectively. Assume that the intrinsic carrier concentration in silicon  $n_i = 1.5$  x  $10^{10}$  cm<sup>-3</sup> at 300 K,  $\frac{kT}{q} = 26 \text{ mV}$  and the permittivity of silicon  $\varepsilon_{si} = 1.04 \times 10^{-12}$  F/cm. The built-in potential and the depletion width of the diode under thermal equilibrium conditions, respectively, are (A) 0.7 V and 1 x  $10^{-4}$  cm (B) 0.86 V and 1 x  $10^{-4}$  cm (C) 0.7 V and 3.3 x  $10^{-5}$  cm (D) 0.86 V and 3.3 x  $10^{-5}$  cm

StudentBounty.com

Answer: D

Exp: 
$$V_{bi} = V_T \ln \frac{N_A N_D}{n_i^2} = 26 \text{ mv} \ln \left[ \frac{5 \times 10^{18} \times 1 \times 10^{16}}{(1.5 \times 10^{10})^2} \right]$$
  
= 0.859V  
 $W = \sqrt{\frac{2\epsilon_S V_{bi}}{q} \left[ \frac{N_A + N_D}{N_A N_D} \right]} = 3.34 \times 10^{-5} \text{ cm}$ 

35. The slope of the  $I_D$  vs  $V_{GS}$  curve of an n-channel MOSFET in linear regime is  $10^{-3}\Omega^{-1}$  at  $V_{DS} = 0.1$  V.. For the same device, neglecting channel length modulation, the slope of the  $\sqrt{I_D}$  vs  $V_{GS}$  curve (in  $\sqrt{A}/V$ ) under saturation regime is approximately \_\_\_\_\_.

### Answer: 0.07

Exp: In linear region, 
$$I_D = k \left[ (V_{GS} - V_T) V_{DS} - \frac{V_{DS}^2}{2} \right]$$
  
 $\frac{\partial I_D}{\partial V_{GS}} = 10^{-3} = k V_{DS}$   
 $\Rightarrow K = \frac{10^{-3}}{0.1} = 0.01$   
In saturation region,  $I_D = \frac{1}{2} k (V_{GS} - V_T)^2$   
 $\sqrt{I_D} = \sqrt{\frac{k}{2}} (V_{GS} - V_T)$   
 $\frac{\partial \sqrt{I_D}}{\partial V_{GS}} = \sqrt{\frac{k}{2}} = \sqrt{\frac{0.01}{2}} = 0.07$ 

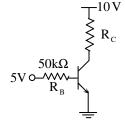
36. An ideal MOS capacitor has boron doping-concentration of  $10^{15}$  cm<sup>-3</sup> in the substrate. When a gate voltage is applied, a depletion region of width 0.5 µm is formed with a surface (channel) potential of 0.2 V. Given that  $\varepsilon_0 = 8.854 \times 10^{14}$  F/cm and the relative permittivities of silicon and silicon dioxide are 12 and 4, respectively, the peak electric field (in V/µm) in the oxide region is \_\_\_\_\_\_.

Answer: 2.4

Exp: 
$$E_s = \frac{2 \times 0.2}{0.5} = 0.8 \text{ v} / \mu \text{m}$$
  
 $E_{ox} = \frac{E_s}{E_{ox}} E_s = 2.4 \text{ v} / \mu \text{m}$ 

### EC-GATE-2014 PAPER-03

WWW "sat) = UIIIII "sat) = UIIIIII Common State Sta In the circuit shown, the silicon BJT has  $\beta = 50$ . Assume  $V_{BE} = 0.7$  V and  $V_{CE(sat)} =$ 37. Which one of the following statements is correct?



- (A) For  $R_C = 1 \text{ k}\Omega$ , the BJT operates in the saturation region
- (B) For  $R_C = 3 \text{ k}\Omega$ , the BJT operates in the saturation region
- (C) For  $R_c = 20 \text{ k}\Omega$ , the BJT operates in the cut-off region
- (D) For  $R_c = 20 \text{ k}\Omega$ , the BJT operates in the linear region

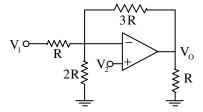
### Answer: B

Exp:

KVL in base loop,  

$$5-I_B(50k)-0.7=0$$
  
 $I_B = \frac{5-0.7}{50k} = 80\mu A$   
⇒  $I_C = βI_B = 50 \times 86\mu A = 4.3 mA$   
∴  $R_C = \frac{10-V_{CE}(sat)}{I_C} = \frac{10-0.2}{4.3 mA}$   
R<sub>C</sub> = 2279Ω and the BJT is in saturation

### 38. Assuming that the Op-amp in the circuit shown is ideal, Vo is given by



(A) 
$$\frac{5}{2}V_1 - 3V_2$$
 (B)  $ZV_1 - \frac{5}{2}V_2$  (C)  $-\frac{3}{2}V_1 + \frac{7}{2}V_2$  (D)  $-3V_1 + \frac{11}{2}V_2$ 

Answer: D

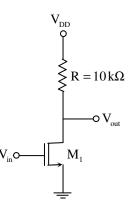
Exp: Virtual ground and KCL at inverting terminal gives

$$\frac{V_2 - V_1}{R} + \frac{V_2}{2R} + \frac{V_2 - V_0}{3R} = 0$$

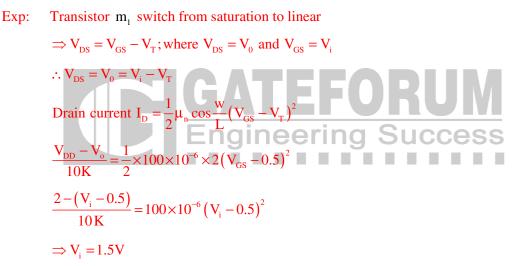
$$\frac{V_0}{3R} = \frac{V_2}{R} + \frac{V_2}{3R} + \frac{V_2}{2R} - \frac{V_1}{R}$$

$$V_0 = -3V_1 + \frac{11}{2}V_2$$

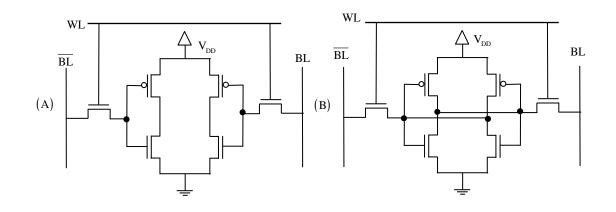
- 100µs - hen For the MOSFET M<sub>1</sub> shown in the figure, assume W/L = 2,  $V_{DD} = 2.0 \text{ V}$ ,  $\mu_n C_{ox} = 100 \mu M$ 39. and  $V_{TH} = 0.5$  V. The transistor  $M_1$  switches from saturation region to linear region when (in Volts) is\_

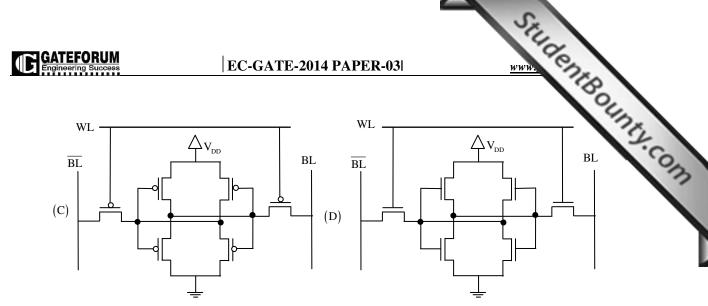


### Answer: 1.5



### 40. If WL is the Word Line and BL the Bit Line, an SRAM cell is shown in

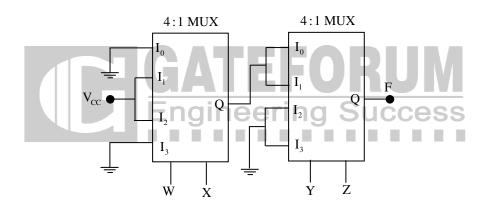




### Answer: B

Exp: For an SRAM construction four MOSFETs are required (2-PMOS and 2-NMOS) with interchanged outputs connected to each CMOS inverter. So option (B) is correct.

41. In the circuit shown, W and Y are MSBs of the control inputs. The output F is given by

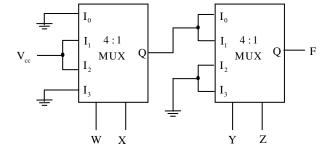


(A) 
$$F = W \overline{X} + \overline{W}X + \overline{Y}\overline{Z}$$
 (B)  $F = W \overline{X} + \overline{W}X + \overline{Y}Z$ 

 $(C) F = W\overline{X}\overline{Y} + \overline{W}X\overline{Y}$ 

(D)  $F = (\overline{W} + \overline{X})\overline{Y}Z$ 

Answer: C Exp:



The output of the first MUX =  $\overline{W} \times V_{cc} + W\overline{X} \cdot V_{cc}$  $\overline{W}X + W\overline{X}$  (::  $V_{cc} = \log ic1$ )  $= W \oplus X$ 

Let  $Q = W \oplus X$ 



WWW CHIBOUNES.com

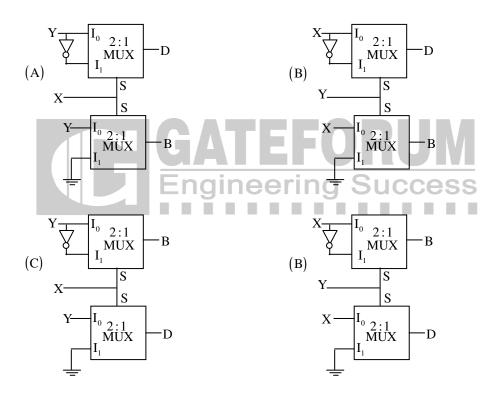
The output of the second MUX =  $Q.\overline{Y}\overline{Z} + Q.\overline{Y}Z$ 

 $= Q.\overline{Y}(\overline{Z}+Z)$ = Q. $\overline{Y}$ .1 = Q. $\overline{Y}$ Put the value of Q in above expression =  $(\overline{W}X + W\overline{X}).\overline{Y}$ =  $\overline{W}X.\overline{Y} + W\overline{X}.\overline{Y}$ 

42.

If X and Y are inputs and the Difference (D = X - Y) and the Borrow (B) are the outputs, which

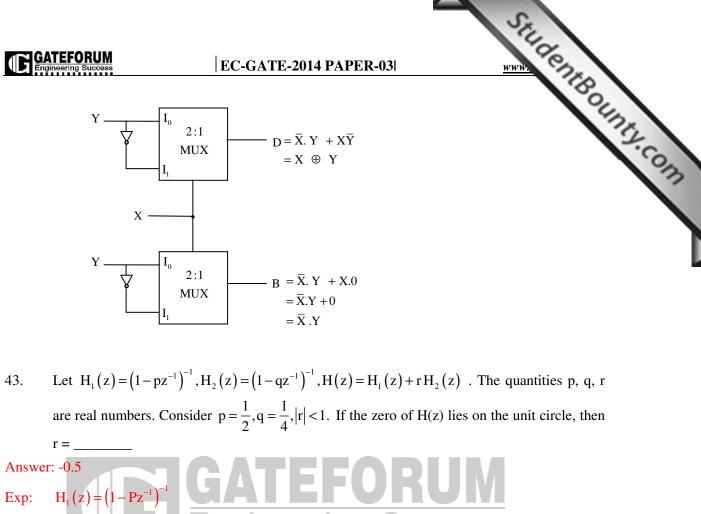
one of the following diagrams implements a half-subtractor?



Answer: A

Exp:

X	Y	D	В	
0	0	0	0	
0	1	1	1	
1	0	1	0	
1	1	0	0	
50, D =	= X ⊕ Y	$= \overline{X}Y +$	$\overline{X}\overline{Y}$ and	$B = \overline{X}$ .



Answer: -0.5  
Exp: H<sub>1</sub>(z) = (1-Pz<sup>-1</sup>)<sup>-1</sup>  
H<sub>2</sub>(z) = (1-qz<sup>-1</sup>)<sup>-1</sup>  
H(z) = 
$$\frac{1}{1-Pz^{-1}} + r\frac{1}{(1-qz^{-1})} = \frac{1-qz^{-1} + r(1-Pz^{-1})}{(1-Pz^{-1})(1-Pz^{-1})} = \frac{(1+r) - (q+rp)z^{-1}}{(1-Pz^{-1})(1-Pz^{-1})}$$
  
zero of H(z) =  $\frac{q+rp}{1+r}$   
Since zero is existing on unit circle  
 $\Rightarrow \frac{q+rp}{1+r} = 1 \text{ or } \frac{q+rp}{1+r} = -1$   
 $-\frac{1}{4} + \frac{r}{2} = 1 \text{ or } \frac{-\frac{1}{4} + \frac{r}{2}}{1+r} = -1$   
 $-\frac{1}{4} + \frac{r}{2} = 1 + r$  or  $-\frac{1}{4} + \frac{r}{2} = -1 - r$   
 $\Rightarrow r = -\frac{5}{2} \Rightarrow \frac{r}{2} = -\frac{5}{4}$  or  $\frac{3}{4} = -\frac{3r}{2}$   $r = -\frac{1}{2} \Rightarrow r = -0.5$   
 $r = -\frac{5}{2}$  is not possible

GATEFORUM

1 . Comunity.com Let h(t) denote the impulse response of a causal system with transfer function -44.

the following three statements.

S1: The system is stable.

S2: 
$$\frac{h(t+1)}{h(t)}$$
 is independent of t for t 0.

S3: A non-causal system with the same transfer function is stable.

For the above system,

(B) only S2 and S3 are true

(A) Only S1 and S2 are true (C) Only S1 and S3 are true

(D) S1, S2 and S3 are true

Answer: A

Exp: 
$$h(t) \leftrightarrow H(s) = \frac{1}{s+1} \Rightarrow h(t) = e^{-t}u(t)$$

 $S_1$ : System is stable (TRUE)

Because h(t) absolutely integrable

S<sub>2</sub>: 
$$\frac{h(t+1)}{h(t)}$$
 is independent of time (TRUE)  
 $\frac{e^{-(t+1)}}{e^{-t}}$  ⇒  $e^{-1}$  (independent of time)  
S<sub>3</sub>: A non-causal system with same transfer function is stable  
 $\frac{1}{s+1}$  ↔  $-e^{-t}u(-t)$  (a non-causal system) but this is not absolutely integrable thus unstable.

Only  $S_1$  and  $S_2$  are TRUE

The z-transform of the sequence x[n] is given by  $X(z) = \frac{1}{(1-2z^{-1})^2}$ , with the region of 45.

convergence |z| > 2. Then, x[2] is \_\_\_\_\_.

Answer: 12

$$X(z) = \frac{1}{(1 - 2z^{-1})^2} = \frac{1}{(1 - 2z^{-1})} \frac{1}{(1 - 2z^{-1})}$$
$$x[n] = 2^n u[n] * 2^n u[n]$$
$$x[n] = \sum_{k=0}^n 2^k \cdot 2^{(n-k)}$$
$$\Rightarrow x[2] = \sum_{k=0}^2 2^k \cdot 2^{(2-k)} = 2^0 \cdot 2^2 + 2^1 \cdot 2^1 + 2^2 \cdot 2^0 = 4 + 4 + 4 = 12$$

EC-GATE-2014 PAPER-03

Exp(2):

EC-GATE-2014 PAPER-03  

$$X(z) = \frac{1}{(1-2Z^{-1})^2} = \frac{Z^2}{(Z-2)^2}$$

$$X(n) = Z^{-1} \left[ \frac{Z}{Z-2} \cdot \frac{Z}{Z-2} \right]$$

$$= \sum_{n=0}^{n} u_n \cdot V_{n-n} \text{ (using conduction theorem and } u_n = 2^n; v_n = 2^n \text{ )}$$

$$= \sum_{m=0}^{n} 2^m \cdot 2^{n-m} = 2^n \text{ (n+1)}$$

$$\therefore x(2) = 12$$

The steady state error of the system shown in the figure for a unit step input is \_\_\_\_\_. 46.

$$\begin{array}{c} R(s) + & E(s) \\ \hline r(t) & e(t) \end{array} \xrightarrow{K=4} & 1 \\ \hline c(s) \\ \hline s+2 \\ \hline c(t) \\ \hline cess \\ cess \\ \hline cess \\ cess \\ \hline cess \\ cess \\ cess \\ \hline cess \\ cess \\$$

Answer: 0.5

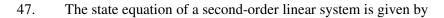
Exp: Given 
$$G(s) = \frac{4}{s+2}$$
;  $H(s) = \frac{2}{s+4}$   
For unit step input,  
 $k_p = \lim_{s \to 0} G(s)H(s)$   
 $k_p = \lim_{s \to 0} \left(\frac{4}{s+2}\right) \left(\frac{2}{s+4}\right)$   
 $\boxed{k_p = 1}$   
Steady state error  $e_{ss} = \frac{A}{1+k_p}$   
 $e_{ss} = \frac{1}{1+1}$ 

$$e_{ss} = \frac{1}{2} \Longrightarrow 0.50$$

GATEFORUM Engineering Success

### EC-GATE-2014 PAPER-03

WWW COMBOUND COM



$$\dot{x}(t) = Ax(t), \ x(0) = x_{0}$$
For  $x_{0} = \begin{bmatrix} \frac{1}{-1} \end{bmatrix}, \ x(t) = \begin{bmatrix} e^{-t} \\ -e^{-t} \end{bmatrix}$  and for  $x_{0} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}, \ x(t) = \begin{bmatrix} e^{-t} - e^{-2t} \\ -e^{-t} + 2e^{-2t} \end{bmatrix}$ 
when  $x_{0} = \begin{bmatrix} 3 \\ 5 \end{bmatrix}, \ x(t)$  is
$$(A) \begin{bmatrix} -8e^{-t} + 11e^{-2t} \\ 8e^{-t} - 22e^{-2t} \end{bmatrix} \qquad (B) \begin{bmatrix} 11e^{-t} - 8e^{-2t} \\ -11e^{-t} + 16e^{-2t} \end{bmatrix}$$

$$(C) \begin{bmatrix} 3e^{-t} - 5e^{-2t} \\ -3e^{-t} + 10e^{-2t} \end{bmatrix} \qquad (D) \begin{bmatrix} 5e^{-t} - 3e^{-2t} \\ -5e^{-t} + 6e^{-2t} \end{bmatrix}$$

Answer: B

Exp: Apply linearity principle,

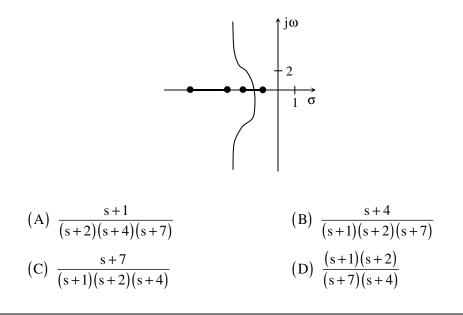
$$\begin{bmatrix} 3\\5 \end{bmatrix} = a \begin{bmatrix} 1\\-1 \end{bmatrix} + b \begin{bmatrix} 0\\1 \end{bmatrix} s$$
  

$$a = 3; b = 8$$
  

$$\Rightarrow x(t) = 3 \begin{bmatrix} e^{-t}\\-e^{-t} \end{bmatrix} + \begin{bmatrix} e^{-t} - e^{-2t}\\-e^{-t} + 2e^{-2t} \end{bmatrix} \text{ recipe Success}$$
  

$$\Rightarrow x(t) = \begin{bmatrix} 11e^{-t} - 8e^{-2t}\\-11e^{-t} + 16e^{-2t} \end{bmatrix}$$

48. In the root locus plot shown in the figure, the pole/zero marks and the arrows have been removed. Which one of the following transfer functions has this root locus?



### GATEFORUM Engineering Success

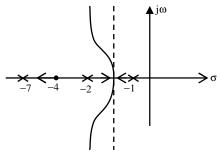
### EC-GATE-2014 PAPER-03

WWW REINBOUINTY.Com

Answer: B

Exp:: For transfer function 
$$\frac{(s+4)}{(s+1)(s+2)(s+3)}$$

From pole zero plot



49. Let X(t) be a wide sense stationary (WSS) random process with power spectral density  $S_X(f)$ . If Y(t) is the process defined as Y(t) = X(2t-1), the power spectral density  $S_Y(f)$  is

(A) 
$$S_{Y}(f) = \frac{1}{2}S_{X}\left(\frac{f}{2}\right)e^{-j\pi f}$$
  
(B)  $S_{Y}(f) = \frac{1}{2}S_{X}\left(\frac{f}{2}\right)e^{-j\pi f/2}$   
(C)  $S_{Y}(f) = \frac{1}{2}S_{X}\left(\frac{f}{2}\right)$   
(D)  $S_{Y}(f) = \frac{1}{2}S_{X}\left(\frac{f}{2}\right)e^{-j2\pi f}$   
(C)  $S_{Y}(f) = \frac{1}{2}S_{X}\left(\frac{f}{2}\right)e^{-j2\pi f}$ 

Answer: C

Exp: Shifting in time domain does not change PSD. Since PSD is Fourier transform of autocorrelation function of WSS process, autocorrelation function depends on time difference.

$$X(t) \leftrightarrow R_{x}(z) \leftrightarrow S_{x}(f)$$
$$Y(t) = X(2t-1) \leftrightarrow R_{y}(2\zeta) \leftrightarrow \frac{1}{2}S_{x}\left(\frac{f}{2}\right)$$

[time scaling property of Fourier transform]

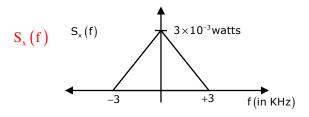
50. A real band-limited random process X(t) has two-sided power spectral density

$$\mathbf{S}_{x}(\mathbf{f}) = \begin{cases} 10^{-6} (3000 - |\mathbf{f}|) \text{ Watts / Hz} & \text{for } |\mathbf{f}| \le 3 \text{ kHz} \\ 0 & \text{otherwise} \end{cases}$$

Where f is the frequency expressed in Hz. The signal X(t)modulates a carrier  $\cos 16000 \pi t$  and the resultant signal is passed through an ideal band-pass filter of unity gain with centre frequency of 8 kHz and band-width of 2 kHz. The output power (in Watts) is \_\_\_\_\_.

Answer: 2.5

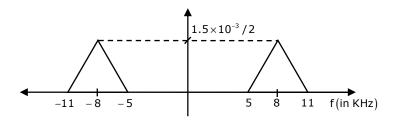
Exp:



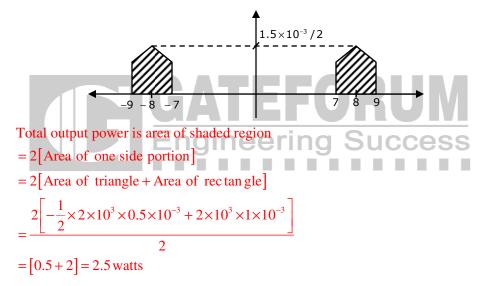
After modulation with  $\cos(16000\pi t)$ 

$$S_{y}(f) = \frac{1}{4} [S_{x}(f - f_{c}) + S_{x}(f + f_{c})]$$

WWW REINBOUINTY.Com This is obtain the power spectral density Random process y(t), we shift the given power spectral density random process x(t) to the right by  $f_c$  shift it to be the left by  $f_c$  and the two shifted power spectral and divide by 4.



After band pass filter of center frequency 8 KHz and BW of 2 kHz



In a PCM system, the signal  $m(t) = {\sin(100\pi t) + \cos(100\pi t)}$  V is sampled at the Nyquist 51. rate. The samples are processed by a uniform quantizer with step size 0.75 V. The minimum data rate of the PCM system in bits per second is \_\_\_\_\_.

Answer: 200

Exp: Nyquist rate =  $2 \times 50$  Hz

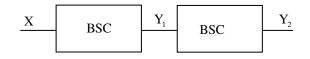
=100 samples / sec

$$\Delta = \frac{m(t)_{max} - m(t)_{min}}{L} \Rightarrow L = \frac{\sqrt{2} - (-\sqrt{2})}{0.75}$$
$$L = \frac{2\sqrt{2}}{0.75} = 3.77 = 4$$

No. of bits required to encode '4' levels = 2 bits/levelThus data rate  $= 2 \times 100 = 200$  bits / sec

### EC-GATE-2014 PAPER-03|

\* to a c robab. 52. A binary random variable X takes the value of 1 with probability 1/3. X is input to a C of 2 independent identical binary symmetric channels (BSCs) each with crossover probable 1/2. The outputs of BSCs are the random variables  $Y_1$  and  $Y_2$  as shown in the figure.



The value of  $H(Y_1) + H(Y_2)$  in bits is\_ Answer ?

Exp: Let 
$$P\{x = 2\} = \frac{1}{3}$$
,  $P\{x = 0\} = \frac{2}{3}$   
to find  $H(Y_1)$  we need to know  $P\{y_1 = 0\}$  and  $P\{y_2 = 1\}$   
 $P\{Y_1 = 0\} = P\{Y_1 = 0 / x_1 = 0\} P\{x_1 = 0\} + P\{y_1 = 0 / x_1 = 1\} P\{x_1 = 1\}$   
 $= \frac{1}{2} \cdot \frac{1}{3} + \frac{1}{2} \times \frac{2}{3} = \frac{1}{2}$   
 $P\{y_1 = 1\} = \frac{1}{2}$   
 $\Rightarrow H(y_1) = \frac{1}{2} \log_2^2 + \frac{1}{2} \log_2^2 = 1$  evening Success  
Similarly  
 $P\{y_2 = 0\} = \frac{1}{2}$  and  $P\{y_2 = 1\} = \frac{1}{2}$   
 $\Rightarrow H\{y_2\} = 1$   
 $\Rightarrow H\{y_1\} + H\{y_2\} = 2$  bits

Given the vector  $A = (\cos x)(\sin y)\hat{a}_x + (\sin x)(\cos y)\hat{a}_y$ , where  $\hat{a}_x, \hat{a}_y$  denote unit vectors 53. along x,y directions, respectively. The magnitude of curl of A is \_\_\_\_\_

Answer: 0

Exp (1):

Curl 
$$\vec{A} = \begin{vmatrix} \hat{a}_x & \hat{a}_y & \hat{a}_z \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ \cos x \sin y & \sin x \cos y & 0 \end{vmatrix}$$
  
=  $\vec{0}$   
∴ |Curl  $\vec{A}$ | = 0

GATEFORUM Engineering Success

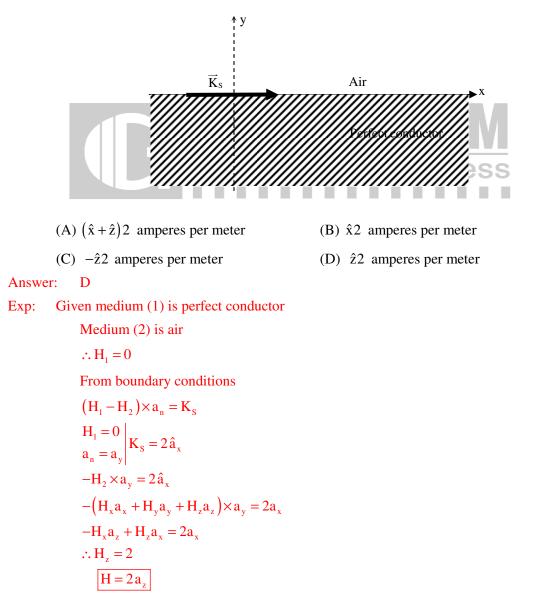
### EC-GATE-2014 PAPER-03

Exp(2):

Given  $A = \cos x \sin y \hat{a}_x + \sin x \cos y \hat{a}_y$ 

$$\nabla \times \mathbf{A} = \begin{vmatrix} \mathbf{a}_{x} & \mathbf{a}_{y} & \mathbf{a}_{z} \\ \partial / \partial x & \partial / \partial y & \partial / \partial z \\ \cos x \sin y & \sin x \cos y & 0 \end{vmatrix}$$
$$= \mathbf{a}_{x} (0) - \mathbf{a}_{y} (0) + \mathbf{a}_{z} (\cos x \cos y - \cos x \cos y) = 0$$
$$\therefore |\nabla \times \mathbf{A}| = 0$$

54. A region shown below contains a perfect conducting half-space and air. The surface current  $\overrightarrow{K_s}$  on the surface of the perfect conductor is  $\overrightarrow{K_s} = \hat{x}2$  amperes per meter. The tangential  $\overrightarrow{H}$  field in the air just above the perfect conductor is



### EC-GATE-2014 PAPER-03

www. www. ) ây regio. regio. Assume that a plane wave in air with an electric field  $\vec{E} = 10\cos(\omega t - 3x - \sqrt{3z})\hat{a}_{y}$ 55. incident on a non-magnetic dielectric slab of relative permittivity 3 which covers the region Z > 0 The angle of transmission in the dielectric slab is \_

### Answer: 30

Exp: Given 
$$E = 10\cos(\omega t - 3x - \sqrt{3}z)a_y$$
  
 $E = E_0 e^{-i\beta(x\cos\theta_x + y\cos\theta_y + z\cos\theta_z)}$   
So,  $\beta_x = \beta\cos\theta_x = 3$   
 $\beta_y = \beta\cos\theta_y = 0$   
 $\beta_z = \beta\cos\theta_z = \sqrt{3}$   
 $\beta_x^2 + \beta_y^2 + \beta_z^2 = \beta^2$   
 $9 + 3 = \beta^2 \Rightarrow \beta = \sqrt{13}$   
 $\beta\cos\theta_z = \sqrt{3} \Rightarrow \cos\theta_z = \sqrt{\frac{3}{13}} \Rightarrow \theta_z = 61.28 = \theta_i$   
 $\frac{\sin\theta_i}{\sin\theta_t} = \sqrt{\frac{E_2}{E_1}} \Rightarrow \frac{\sin 61.28}{\sin\theta_t} = \sqrt{\frac{3}{1}} \Rightarrow \frac{0.8769}{\sqrt{3}} = \sin\theta_t$   
 $\theta_t = 30.4 \Rightarrow \theta_t \approx 30^\circ$