AQA

A S S E S S M E N T and
Q U A L I F I C A T I O N S
A L L I A N C E

Free-Standing Mathematics Qualification

Working with Algebraic and Graphical Techniques 6991/2

Mark Scheme

2007 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available to download from the AQA Website: www.aqa.org.uk

Key to mark scheme and abbreviations used in marking

M	mark is for method		
m or dM	mark is dependent on one or more M marks and is for method		
A	mark is dependent on M or m marks and is for accuracy		
B	mark is independent of M or m marks and is for method and accuracy		
E	mark is for explanation		
√or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
$-x$ EE	deduct x marks for each error	G	graph
NMS	no method shown	c	candidate
PI	possibly implied	sf	significant figure(s)
SCA	substantially correct approach	dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

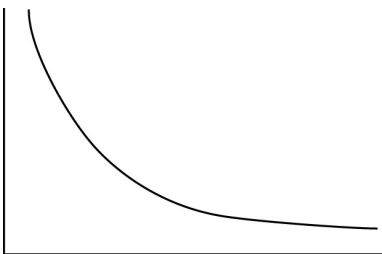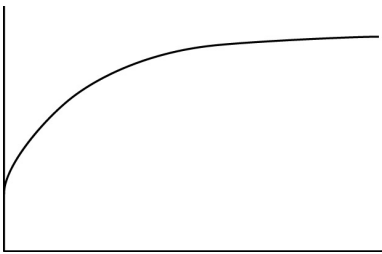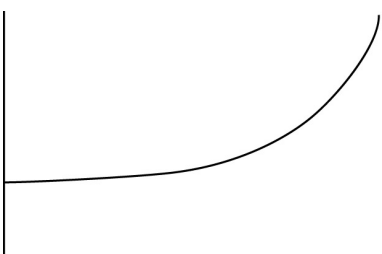**Otherwise we require evidence of a correct method for any marks to be awarded.**

June 07

Free-Standing Mathematics Qualification

Advanced Level – Working with Algebraic and Graphical Techniques (6991/2)

Answers and Marking Scheme - June 2007

Question 1

(a)	$(\pm40, 67.4)$ $(\pm30, 59.8)$ $(\pm20, 54.3)$ $(\pm10, 51.1)$ $(0, 50)$ 9 correct plots to $\frac{1}{2}$ square accuracy Smooth correct curve to $\frac{1}{2}$ square accuracy	**B3** **B1**	B2 7 correct plots B1 5 correct plots
(b)	50	**B1**	Accept (0, 50)
(c)	65.7	**B1**	65.69… Do not accept 66 etc.
(d)	Stretch (parallel to) y axis (scale) factor $\frac{1}{92}$	**B1**	
	y translate (or translation) 50	**B1**	$\begin{pmatrix} 0 \\ 50 \end{pmatrix}$
	TOTAL	**8**	

Question 2

(a)	Sub $x = 40$ 315.(…) and (385 or 384.6..)	**M1** **A1**	
(b)	350	**B1**	
(c)	Can not find $\sqrt{}$ of a negative number	**B1**	oe
(d)	$370 = 350 \pm \sqrt{(120(x-30))}$ 33.3 (…)	**M1** **A1**	
	TOTAL	**6**	

Question 3

(a)(i)	Line between (6,115) and (16,169) to $\frac{1}{2}$ square accuracy	**B1**	
(a)(ii)	141 to 143	**B1**	
(b)	$h = \frac{A}{x} + B$ correct curvature	**B1**	Any graphs in other quadrants must be correct
	$h = A\sqrt{x} + B$ correct curvature	**B1**	
	Crosses h axis at a positive value	**B1**	
	$h = Ae^x + B$ correct curvature	**B1**	
	$h = A\sqrt{x} + B$ is best	**B1**	
(c)	0 to 2, 0 and 1	**B1**	Accept 0
(d)	Height decreases	**B1**	$\sin 90 = 1$ max **OE** B0 they stop growing B0 the height will not continue to increase
(e)	$h =$ constant or height $=$ constant	**B1**	Or $h = 178$ **OE**
	TOTAL	**10**	

Question 4

(a)(i)	$\ln P = \ln\left(A e^{kt}\right)$	**M1**	Or $\ln P = \ln A + \ln\left(e^{kt}\right)$
	$\ln P = \ln A + kt$	**A1**	
(a)(ii)	3.59, 3.63, 3.69, 3.78, 3.83, 3.89	**B2**	B1 4 correct B1 if greater than 3 significant figures B1 if use log
(a)(iii)	Correct plots to $\frac{1}{2}$ square accuracy	**B2**	B1 3 correct
	Line of best fit through points	**B1ft**	
(a)(iv)	$A = 36$ to 36.3	**B1**	
	$k = $ gradient and attempt seen	**M1**	Or substituting into $\ln P = \ln A + kt$
	$k = 0.0045$ to 0.0055	**A1**	
(b)(i)	Population in 1981	**B1**	Or population at the start
(b)(ii)	Sub. $t = 30$	**M1**	
	52.1(36...)	**A1**	No Working, 52 **SC1**
(b)(iii)	$55 \div 49.1 = e^{0.002t}$		
		M1	$\ln 55 = \ln 49.1 + 0.002t$
	$\ln\left(55 \div 49.1\right) = 0.002t$	**M1**	$\ln 55 - \ln 49.1 = 0.002t$
	2038 or 2037	**A1**	M2 $t = 56.7\ldots$
(b)(iv)	51.1(038...)	**B1**	
	$(52 - \text{their } 51.1) \div 52 \times 100$	**M1**	Or reversed
	1.7(2...)%	**A1**	Ignore – signs 1.76% B1 only **SC1** 1.92 % seen
	TOTAL	**19**	

Question 5

(a)	$(10,17.2)$ $(12,13.7)$ $(14,8.31)$ $(16,3.57)$ $(18,1.7)$ $(20,3.57)$ 6 correct plots to $\frac{1}{2}$ square accuracy Smooth correct curve to $\frac{1}{2}$ square accuracy	**B3** **B1**	B2 5 correct plots B1 4 correct plots Must include $(9, 17.7)$
(b)(i)	17.7	**B1**	
(b)(ii)	9	**B1**	No Working, 9, or **FT**
(c)(i)	Tangent drawn at t = 7 1.6 to 2	**M1** **A1**	No tangent M0A0 unless calculus seen
(c)(ii)	m/s or ms^{-1} or e.g. 1.8 m/s	**B1**	Metres per second
(c)(iii)	Rate of change of height	**B1**	Speed or velocity; how quickly "you" are going up
(d)(i)	Amplitude = 8	**B1**	Not – 8
(d)(ii)	Period = 18	**B1**	
(e)(i)	4.5 22.5 or 13.5	**B1** **B1**	
(e)(ii)	$t = 0$ $h = 1.7$ $h = 17.7$	**B1** **B1** **B1**	Can be implied by correct answers Or **FT** their (b)(i)
	TOTAL	**17**	
	TOTAL MARK FOR PAPER	**60**	