

FEDERAL PUBLIC SERVICE COMMISS """ POTTITIVE EXAMINATION FOR "" POSTS IN BS-17 """ 2011

STATISTICS

TIME ALLOWED:		: (PART	(PART-I MCQs)		30 MINUTES			MAXIMUM MARKS: 20			
TH	REE HOURS	(PART	-II)	t) 2 HOURS & 30 MINUTES			MAXIMUM MARKS: 80				
NO	TE: (1) First minut	attempt P A tes.	ART-I (MCQS)	on separ	ate Answer Shee	t which	shall be	taken baci	x after 30		
	(ii) Over	writing/cu	tting of the op	tions/ans	wers will not be	given o	credit.				
	(iii) Statis	stical Table	es will be prov	ided if re	quired.						
	(\mathbf{IV}) Use 0	1 Scienting		anoweu.							
			(PART-I	MCQs)	(COMPULSOR	<u>Y)</u>					
Q.1	• Select the bes	st option/ar	nswer and fill ir	the appr	opriate box on th	e Answ	er Sheet.	. (1	x 20=20)		
(i)	The mean of X	, following	a Binomial dis	tribution	with parameter n	and p i	s `	variance o	f x.		
	(a) Equal to the	ne (b)	Less than the	(c)	Greater than the	e					
	(d) Equal to the	ne square ro	oot of the	(e)	None of these						
(ii)	$(A \cap B) \cup (A \cap$	B')=									
	(a) A	(b)	В	(c)	A'	(d)	B'	(e)	None of these		
(iii)	Four candidates	s are seekin	g a vacancy on	a college	board. If A is tw	vice as I	ikelv to	be elected	as B. and B		
()	and C are given that C will be e	about the lected?	same chance of	being ele	ected, while C is	twice a	s likely a	s D, what	are the chances		
	(a) 1	(b)	2	(c)	1	(d)	4	(e)	None of these		
	$\overline{2}$		9		3		9				
(iv)	For married cou 0.21, the probat and wife will w TV program?	uple in a ce bility that th atch that T	rtain locality th he wife will wa V program is 0	e probabi tch that T .15. What	lity that the husb V program is 0.2 t is the probabilit	and wil 28 and t y that a	l watch a he proba t least on	a specific 7 bility that le of them	IV program is both husband will watch that		
	(a) 0.49	(b)	0.64	(c)	0.34	(d)	0.36	(e)	None of these		
(v)	The value of k a joint probabil	that will ma ity distribu	ake the function tion is:	h, f(x, y)	= kxy for $x = 1$,	2, 3 and	d y = 1, 2	2, 3			
	(a) 1	(b)	1	(c)	1	(d)	1	(e)	None of these		
	$\overline{9}$		$\overline{3}$		$\overline{2}$		36				
(vi)	If the joint prob elsewhere, then	bability den $P(x < 1/2)$	sity function of $2, y < 1/2$ =	X and Y	is given by $f(x, y)$	(y) = 2	for x>0 a	and y>0 ar	nd zero		
	(a) 1	(b)	1	(c)	3	(d)	2	(e)	None of these		
	$\overline{2}$		4		$\overline{4}$		$\overline{3}$				
(vii)) If $V(x)=19$ then	n V(2x –5)	=								
	(a) 19	(b)	38	(c)	33	(d)	76	(e)	None of these		
(viii)) Assume that the	e fitted reg	ression betweer	\mathbf{x} and \mathbf{v}	is. $v = \beta_1 + \beta_2 x a$	and the	regressio	n fitted be	tween		
	z and w is $z = 1$	$\beta_3 + \beta_4 x$. (Given that $z = 3$	By and w	= 2x, then:		0				
	(a) $\beta_{i} = \beta_{2}$	1		(b)	$\beta_{\star} = (3/2)\beta_{\star}$						
	(c) $\beta_{1} = (2/3)^{2}$	β_{α}		(d)	$\beta_{4} = 4\beta_{2}$			(e)	None of these		

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(ix)	Wh norr (a)	ile applying analy nality and Consistency	vsis of must (b)	variance to test th hold, Unbiasedness	e equa	ality of means, thre	e con	ditions namel	ly,	Bounty
	(c)	Homogeneity of	popu	lation variances	(d)	Efficient estimato	ors		(e)	None Co.
(x)	In t	raditional samplir	ng the	ory the finite popu	lation	correction factor is	s deno	oted by		3
	(a)	(N - n)/(N - 1)			(b)	(N - n)/N				
	(c)	N/(N - 1)			(d)	n/(N - 1)			(e)	None of these
(xi)	A ra	andom sample of	size n	is drawn from a p	opulat	tion following expo	onenti	al distribution	n witl	n probability
	den	sity function, $f(x)$	$x) = \frac{1}{\lambda}$	$e^{-x/\lambda}$, for x>0.	Then	the maximum likel	ihood	estimator of	λisg	iven by
	(a)	$\frac{1}{x}$	(b)	$1/\overline{x}$	(c)	$\sum_{i=1}^{n} x_i$	(d)	$\sum_{i=1}^{n} x_i^2$	(e)	None of these
(xii)	An	estimator $\hat{\theta}$ is said	d to be	e consistent if						
	(a)	$E(\hat{\theta}) = \theta$			(b)	$E\left(\hat{ heta} ight) = V\left(\hat{ heta} ight)$				
	(c)	$V(\hat{\theta}) \rightarrow 0$ as $n -$	$\rightarrow \infty$		(d)	$V(\hat{\theta}) = [E(\hat{\theta})]^2$			(e)	None of these
(xiii)	If b	is constant and th	ne mo	ment generating fu	inction	n of x is $M_x(t)$ then	M_{x+x}	$_{b}\left(t ight) =$		
	(a)	$M_x(t)$ (b)	M	(bt) (c)	M _x ((t) + b (d)	e^{bt}	M (t)	(e)	None of these
(xiv)	If th	e random variabl	e x is	distributed normal	lly, N((105,36) then $w = ($	(x - 1)	05)/6 will foll	low a	normal
	(a)	N (105, 1)	(b)	N (0, 1)	(c)	N (105, 6) (d) N	N (105, 36)	(e)	None of these
(xv)	If the bety	the coefficient of c ween $z = ax+b$ and	orrela d w=c	tion between two y+d will be equal	variab to	les x and y is giver	n by r,	then the coe	fficier	t of correlation
	(a)	(ac+bd)r	(b)	(acbd)r	(c)	r	(d)	(ac)r+bd	(e)	None of these
(xvi)	Ass R_{xy}	uming x, y and z z_z is given by	are th	ree variables, then	using	the usual notations	s, the	partial correl	ation (coefficient,
	(a)	$(r_{xy} - r_{xz}) \Big/ \sqrt{(1 - r_{xz})} \Big/ (1 - r_$	(r_{xy}^2)		(b)	$(r_{xy}-r_{xz}r_{yz})\Big/\sqrt{1-1}$	r_{xy}^2			
	(c)	$(r_{xy}-r_{xz})/[(\sqrt{1-r_{xy}})/((\sqrt{1-r_{xy}}))]$	$\overline{r_{xy}^2} \bigg($	$\overline{1-r_{yz}^2}$						
	(d)	$(r_{xy}-r_{xz}r_{yz})/[(\sqrt{1})]$	$1-r_{xz}^2$	$\left(\sqrt{1-r_{yz}^2}\right)$			(e)	None of the	nese	
(xvii)	A st 0.3	tock may result in and 0.3 then the a	ı profi verag	t of \$1, loss of \$1 ge profit will be	or bre	akeven (no gain no	loss)	with respect	ive pro	obabilities 0.4,
	(a)	\$1.0	(b)	\$0.4	(c)	\$0.25	(d)	\$0.1	(e)	None of these
(xviii)	Wh	ile expanding the	mom	ent generating fund	ction t	he coefficient of μ	ı', is gi	ven by		
	(a)	$t^{r}/r!$	(b)	t^{r}/r	(c)	t^{r}	(d)	r!t ^r	(e)	None of these
(xix)	Ass	ume that x and y	are tw	o independent ran	dom v	variables then the V	/(xy) i	is equal to		
	(a)	ху	(b)	zero	(c)	x/y	(d)	x+y	(e)	None of these
(xx)	If A	and B are two in	deper	ident variables the	n the c	conditional probabi	lity F	P(B A) =		
	(a)	$P(A \cap B)$	(b)	P(A)	(c)	P(B)	(d)	Zero	(e)	None of these

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PART-II

							PAR	[-II				10	
NOTE:(i) (ii) (iii)		PART-II is to be attempted on separate Answer Book. Attempt ANY FIVE questions from PART-II. All questions carry EQUAL marks Extra attempt of any question or any part of the attempted question will not be considered.									ouney.		
).2 .	(a)	Diffe for ea	erentiate ach typ	e betwe e of eve	en inder nt.	pendent,	depend	lent an	d mutu	ally exclu	sive events. C	Give one of	example (06)
	(b)	A shi sets 1	ipment andom	of 10 T ly. Find	V sets i :	ncludes	three th	hat are	defecti	ve. A stor	e dealer purch	nases four	r TV (06)
		(i)	Proba	ability o	f getting	g exactl	y two d	efective	e TV s	ets;			
		(ii)	Proba	ability o	f getting	g at leas	t one de	efective	e TV se	et.			
	(c)	In a l phon and c proba	arge ci e set is coloure ability	ty the p 0.86 an d mobil that the	robabili d 0.35, e phone family j	ties that respecti set is 0 possesse	a famil vely. Fu .29. A f es either	y, selecturther t amily f or bot	cted rat he prol from th h types	ndomly, h bability th his city is s s of mobil	as a black or a at the family selected rando e phones.	coloured has both omly, wha	mobile black at is the (04)
Q.3.	(a)	 A delicate surgical operation is quite successful and the probability of its failure is 0.005. What is the probability that among next 1000 patients, having this surgical operation, (04 + 04 (i) Exactly five will not survive? (ii) At least two will not survive? 											
	(b)	Let x, a random variable showing the number of calls arriving at a telephone exchange during										uring a	
		speci	fic tim	e period	, follow	vs a proł	oability	distrib	ution g	given by f($\mathbf{x}) = \frac{e^{-\lambda} \lambda^x}{x!} \text{for} $	or $\mathbf{x} = 0$, 1	1, 2,
		and .	λ>0. D	etermin	e mome	ent gene	erating f	function	n and f	ind mean	and variance	of x. (04 + (02 + 02
2.4.	(a)	Assu a nor	ming tl mal dis	nat a rar stributio	dom va n with p	riable x probabil	, repres ity dens	enting sity fun	the life ction,	e of a spec	ific type of tu	ibe light f	follows
		f(x)	$=\frac{1}{\sqrt{2\pi}}$	$=e^{-2\sigma^2}$	(x-μ) , W	vhere–•	o <i><x<∝< i=""></x<∝<></i>	D.					
		(i)	Show	that f(x	x) is a p	robabili	ty densi	ity func	ction.				(04)
		(ii)	Deter	mine m	aximun	n likelih	ood est	imators	s of μ	and σ^2 .			(06)
	(b)	A ma 1000 from 1000	nufact hours the pro hours	urer clai of opera oduction of opera	ims that ation be line an ation. Co	at most fore req d tested omment	5 perce uiring s . It was t on the	ent of the ervice. found manufa	he time Twent that the acturer	e a given p ty product ree of then 's claim.	broduct will su s were selecte m required ser	ustain fev d random rvice befo	ver than hly bre (06)
) .5.	A phan severe provid conduc Follow ExMee	rmaceu headad les, on cted an ving tal d	tical co che pat average d patie ble show 12 12	ompany ients. Tl e, early : nts with ws the r 23 9	ABC re ne comp recovery severe ecovery 22 11	ecently 1 bany AE y than theadach times c 12 10	auncheo BC has a ne existine were of 13 suo 13 9	d a new annound ing med admini ch patie 14 8	v medic ced tha dicine 1 istered ents.	cine to pro at their me ExMed. T these meo	ovide an early dicine named to test their cla dicines on ran	recovery , NewMe aim a stud dom basi	r to ed dy was s.
		(i)	12 Do t	ha data	nrovida	sufficie	nt avid	once a	10 t 5% la	aval of sig	nificance to c	accept the	alaim
		(I)	of A	BC?	provide	sumer		CHUE, à	ι <i>J</i> 70 Ιθ	ver of sig		accept the	(06)
		(ii)	Cons	truct a 9	0% cor	nfidence	interva	l for μ_{l}	New Med	$-\mu_{ExMed}$, a	and comment	on the rea	sult.
													(06
		(iii)	Cons	truct a 9	9% cor	nfidence	interva	l for σ	2 New Med	and comm	ent on the fin	ding.	× ·

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- StudentBounty.com Q.6. Considering the simple linear regression model, $y_i = \beta_1 + \beta_2 x_i + e_i$, for i = 1, (a) assumptions and derive least square estimators of the β_1 and β_2 .
 - **(b)** Following table shows the income and saving of seven families residing at a specific local

Income	e (I)	9	11	13	15	17	19	21
Saving	; (S)	5	6	9	11	12	14	15
(i)	Fit a r	regressio	on mode	el, $\hat{S}_i =$	$\hat{\beta}_1 + \hat{\beta}_2$	I_i for i =	= 1, 2, .	, 7.

- Test the hypothesis H_0 : $\beta_2 = 1$ against H_0 : $\beta_2 < 1$ at 5% level of significance. (ii) (03)
- Q.7. (a) Assume that a random sample of size n is drawn from a population of size N. the population is further assumed to have a mean μ and variance σ^2 . Prove that, $V(\bar{y}) = \frac{\sigma^2}{n} \left(\frac{N-n}{N}\right)$.
 - **(b)** Draw all possible samples of size 3, without replacement, from the population: 12, 9, 15, 9 and 21 and prove that $E(\overline{y}) = \mu$ (08)
- A study was conducted to establish relationship between the nature of crime and educational **O.8**. (a) facilities available. The study was based on 291 respondents and the number of respondents found involved in various types of crimes were recorded as given below. Data collected during the study is also given below: (08)

	Nature of Crime				
Education Level	Low	Medium	High		
Low	17	22	47		
Medium	12	15	22		
High	32	21	14		
Very High	45	33	11		

Could it be concluded, at 1% level of significance, that there exists a significant association between the availability of education facility and nature of crime?

A study was conducted to compare the lifespan of three types of batteries. Fifteen batteries, five **(b)** of each type, were selected randomly from the production line and observed till they expired. Their lifespans, as recorded, are given below: (08)

Battery Type								
А	В	С						
23	23	54						
34	22	56						
44	21	55						
45	23	67						
44	34	65						

Test the hypothesis, $H_0: \mu_A = \mu_B = \mu_C$ at 5% level of significance.

- Write short notes on the following topics: **Q.9**.
 - Role of statistics in highlighting socio-economic problems of a society. (a)
 - **(b)** Comparison and advantages of Stratified and Systematic sampling schemes.
 - Partial and Multiple regression and correlations. (c)
 - **(d)** Importance of hypothesis testing in real life situations.

(05)

(08)

(04 + 04 + 04 + 04 = 16)