www. trenepapers.com

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS Pre-U Certificate

MARK SCHEME for the May/June 2012 question paper for the guidance of teachers

9794 MATHEMATICS

9794/02

Paper 2 (Pure Mathematics 2), maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• Cambridge will not enter into discussions or correspondence in connection with these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2012 question papers for most IGCSE, Pre-U, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.



Page 2	Mark Scheme: Teachers' version	Syllabus	Paper	
	Pre-U – May/June 2012	9794	02	

1	(i) Using the quadratic formula or equivalent, $8 \pm \sqrt{64-16}$	M1	[2]		up to 1 error
	$x = \frac{8 \pm \sqrt{64 - 16}}{2} = 4 \pm 2\sqrt{3}$	A1	[2]		
	(ii) $(6+2\sqrt{3})(2-\sqrt{3}) = 12-6\sqrt{3}+4\sqrt{3}-2\sqrt{3}\sqrt{3}$	M1			Multiply out
	$= 12 - 6\sqrt{3} + 4\sqrt{3} - 6$	B1			$\sqrt{3}\sqrt{3} = 3$
	$=6-2\sqrt{3}$	A1	[3]	[5]	
2	(i) (a) $AB = \sqrt{6^2 + 8^2} = 10$	M1 A1	[2]		Use Pythagoras
	(b) Midpoint of AB is $(6, -3)$	B1	[1]		
	(c) $(x-6)^2 + (y+3)^2 = 25 \text{ AEF}$	$ \begin{array}{c} \sqrt{B1} \\ \sqrt{B1} \\ \sqrt{B1} \end{array} $	[3]		ft their values from (a) + (b)
	(ii) Gradient of AC is -0.5 Use of $y = mx + c$ or equivalent Required equation: $y = -\frac{1}{2}x + \frac{11}{2}$	M1 M1 A1	[3]	[9]	$\Delta y / \Delta x$
3	$\int_0^1 (e^x - x) dx = \left[e^x - \frac{1}{2} x^2 \right]_0^1$	M1 A1			$ke^x + mx^2$
	$=e-\frac{3}{2}$	M1 A1	[4]	[4]	Use of limits Without $+ c$
4	Take logarithms and apply log rule $(2x-1)\log 2 = \log 5$ Rearrange to make x the subject	M1 A1 M1			Up to 1 error
	Obtain $x = \frac{1}{\log 4} = 1.66096$ AEF	A1	[4]	[4]	
5	(i) Sine wave through the origin, showing intersections with the <i>x</i> -axis at (0), π and 2π .	B1	[1]		
	(ii) Sine wave translated in the negative <i>x</i> -direction <i>x</i> -intercepts $\frac{5}{6}\pi$, $\frac{11}{6}\pi$, <i>y</i> -intercept 0.5 and symmetrical about the <i>x</i> -axis.	M1 A1	[2]	[3]	
6	(i) (a) $u_1 = 5$, $u_5 = 37$ implies $4d = 32$ d = 8 $u_n = 8n - 3$ AEF ft their d	M1 A1 M1 √A1	[4]		seen in either part
	(b) $S_n = \frac{n}{2}(2+8n)$ AEF ft their d	M1 √A1	[2]		
	(ii) $S_{25} - S_4 = 2525 - 68$ = 2457	M1 A1	[2]	[8]	Or equivalent

Page 3	Mark Scheme: Teachers' version	Syllabus	Paper
	Pre-U – May/June 2012	9794	02

7	(i) Attempt product rule	M1			
	$\frac{dy}{dx} = 2e^{-2x} - 2(2x - 3)e^{-2x}$	A1			
		A1	[3]		
	$= (8-4x)e^{-2x}$	711	[2]		
	,				
	dv				
	(ii) $\frac{dy}{dx} \ge 0$ seen	B1			
	y is increasing when $x \le 2$.	B1	[2]	[5]	
	, 6 –	Di	[4]	[-]	
8	Separate variables, prior to integration:	M1			
	$\int \frac{-1}{v^2} \mathrm{d}y = \int x^3 \mathrm{d}x$	A1			
	$\mathbf{J}_{\mathbf{y}^2}$	AI			
	$\frac{1}{y} = \frac{1}{4}x^4$ (+c)	A1			
	y	A1			
	Subs into expression including <i>c</i> and solve	M1			
	$c = \frac{1}{4} \text{ so } y = \frac{4}{x^4 + 1}$ AEF		5.63	[6]	
	$c - \frac{1}{4} \operatorname{so} y = \frac{1}{x^4 + 1} \operatorname{AEF}$	A1	[6]	[6]	
9	P = 2n + 2m	D1			
9	(i) $P = 2r + 2rx$ $A = r^2x$	B1 B1	[2]		
		Di	[4]		
	(ii) $P = 20 \text{ implies } r = \frac{10}{1+x}$	M1			r = f(x)
	_				
	so $A = \left(\frac{10}{1+x}\right)^2 x = \frac{100x}{(1+x)^2}$ AG	A1	[2]		
			[-]		
	(iii) Use quotient rule				
	$\frac{dA}{dx} = \frac{100(1+x)^2 - 200x(1+x)}{(1+x)^4} \left[= \frac{100(1-x)}{(1+x)^3} \right]$	M1			
	$dx \qquad (1+x)^4 \qquad \left[\begin{array}{c} - & (1+x)^3 \end{array} \right]$	A1			
	Set equal to zero and find $x = 1$	A1			Allow ±1
	Attached to the second of Control (Control (Cont				
	Attempt to show with first differential test that it is max.	M1			Or equivalent
	Completely correct solution		r <i>e</i> n	101	
	Completely contest solution	A1	[5]	[9]	

Page 4	Mark Scheme: Teachers' version	Syllabus	Paper	
	Pre-U – May/June 2012	9794	02	

10	(i)	(a)	$\ln(1+e^x) + c$	B1 B1	[2]		
		(b)	$ln(1 + e^{ln3}) - ln(1 + e^{0})$ = ln 4 - ln 2	M1			Use of limits
			Use log rule correctly = ln 2 CAO	M1 A1	[3]		
	(ii)	(a)	Make substitution, including attempt at changing dx to du .	M1			
			Attempt to simplify to obtain $\int \frac{u-1}{u^2} du$	A1			
			$= \int \frac{1}{u} - \frac{1}{u^2} du$ Deal with integrand,	M1			
			$= \ln(u) + \frac{1}{u} + c$	√ A 1			
			$= \ln(1 + e^x) + \frac{1}{1 + e^x} + c$ CAO	A1	[5]		
	(b)		$\pi \int_{-\ln 3}^{\ln 3} \left(\frac{e^x}{1 + e^x} \right)^2 dx \text{and attempt to integrate}$	M1			
		$=\pi$	$\left[\ln(1+e^x) + \frac{1}{1+e^x}\right]_{-\ln 3}^{\ln 3} = \pi(\ln 3 - \frac{1}{2})$	A1	[2]	[12]	

Page 5	Mark Scheme: Teachers' version	Syllabus	Paper
	Pre-U – May/June 2012	9794	02

11	(i)	$\frac{\mathrm{df}}{\mathrm{d}t} = 2\cos t - 2\sin 2t$	M1			kcos $t + m$ sin $2t$
		$dt = 2 \cos t - 4 \sin t \cos t$				
		$= 2\cos t (1 - 2\sin t)$	A1	[2]		AG
	(**)	F: 11 1 · · · · ·	3.61			
	(11)	Find local maxima/minima $f(x) = 0$ implies $x = \frac{1}{2}\pi, \frac{3}{2}\pi, \frac{1}{6}\pi, \frac{5}{6}\pi$	M1 A1			Any four
		Values of f 1, -3, 1.5, 1.5	A1			All eight
		values 011 1, 3, 1.3, 1.3	AI			All Cight
		Values of f at endpoints 1, 1	B1			
		Hence range is [-3, 1.5]	A1	[5]		
	(iii)	Substitute for <i>x</i> and <i>y</i> , and multiply out:				
		$(2\cos t + \sin 2t)^2 + (2\sin t + \cos 2t)^2$				
		$=4\cos^2 t + 4\cos t\sin 2t + \sin^2 2t$				
		$+4\sin^2 t + 4\sin t\cos 2t + \cos^2 2t$	M1			Including cross-terms
		$= 4(\cos^2 t + \sin^2 t) + (\cos^2 2t + \sin^2 2t)$				-
		$+4(\cos t \sin 2t + \sin t \cos 2t)$	DM1			Pythagorean identity OR addition formula
		$= 5 + 4\sin(t + 2t) = 5 + 4\sin 3t$	A1	[3]		AG
	(iv)	$x^2 + y^2 = r^2$ is a circle centre the origin 5 + 4sin3 $t \in [1,9]$	В 0,	1, 2		Either statement B1 Both and conclusion B2
						Both and conclusion B2
		so C lies between and on circles of radius 1 and 3.				
	(v)	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\mathrm{d}y}{\mathrm{d}t} \div \frac{\mathrm{d}x}{\mathrm{d}t}$	N/ 1			acost+bsin2t
	(1)		M1			$\frac{a\cos t + b\sin 2t}{c\sin t + d\cos 2t}$
		$=\frac{2\cos t - 2\sin 2t}{-2\sin t + 2\cos 2t}$	A1			
		at $t = 0$, $\frac{dy}{dx} = \frac{2 - 0}{-0 + 2} = 1$	A1	[3]	[15]	