## CIMA

## Management Accounting Pillar

Managerial Level Paper

## P2 - Management Accounting Decision Management

## 24 May 2006 - Wednesday Morning Session

## Instructions to candidates

| You are allowed three hours to answer this question paper |
| :--- |
| You are allowed 20 minutes reading time before the examination begins <br> during which you should read the question paper, and if you wish, make <br> annotations on the question paper. However, you will not be allowed, under <br> any circumstances, to open the answer book and start writing or use your <br> calculator during this reading time. |
| You are strongly advised to carefully read ALL the question requirements <br> before attempting the question concerned (that is, all parts and/or sub- <br> questions). The requirements for the questions in Sections B and C are <br> contained in a dotted box. |
| Answer the ONE compulsory question in Section A. This is comprised of <br> eight sub-questions and is on pages 2 to 5. |
| Answer ALL THREE compulsory questions in Section B on pages 6 to 8. |
| Answer TWO of the three questions in Section C on pages 10 to 15. |
| Maths Tables and Formulae are provided on pages 17 to 19. These pages <br> are detachable for ease of reference. |
| Write your full examination number, paper number and the examination <br> subject title in the spaces provided on the front of the examination answer <br> book. Also write your contact ID and name in the space provided in the right <br> hand margin and seal to close. |
| Tick the appropriate boxes on the front of the answer book to indicate which <br> questions you have answered. |

## Instructions for answering Section A:

The answers to the eight sub-questions in Section A should ALL be written in your answer book.

Your answers should be clearly numbered with the sub-question number and then ruled off, so that the markers know which sub-question you are answering. For multiple choice questions, you need only write the sub-question number and the letter of the answer option you have chosen. You do not need to start a new page for each sub-question.

For sub-questions $1.6,1.7$, and 1.8 you should show your workings as marks are available for the method you use to answer these sub-questions.

## Question One

1.1 X plc intends to use relevant costs as the basis of the selling price for a special order: the printing of a brochure. The brochure requires a particular type of paper that is not regularly used by $X$ plc although a limited amount is in $X$ plc's inventory which was left over from a previous job. The cost when $X$ plc bought this paper last year was $\$ 15$ per ream and there are 100 reams in inventory. The brochure requires 250 reams. The current market price of the paper is $\$ 26$ per ream, and the resale value of the paper in inventory is $\$ 10$ per ream.

The relevant cost of the paper to be used in printing the brochure is
A $\$ 2,500$
B $\$ 4,900$
C $\$ 5,400$
D $\$ 6,500$
1.2 A farmer grows potatoes for sale to wholesalers and to individual customers. The farmer currently digs up the potatoes and sells them in 20 kg sacks. He is considering a decision to make a change to this current approach. He thinks that washing the potatoes and packaging them in 2 kg cartons might be more attractive to some of his individual customers. Which of the following is relevant to his decision?
(i) the sales value of the dug potatoes
(ii) the cost per kg of growing the potatoes
(iii) the cost of washing and packaging the potatoes
(iv) the sales value of the washed and packaged potatoes

A (ii), (iii) and (iv) only
B (i), (ii) and (iii) only
C (i), (ii) and (iv) only
D (i), (iii) and (iv) only
1.3 A company makes and sells three products, R, S, and T. Extracts from the weekly profit statements are as follows:

|  | $R$ | $S$ | $T$ | Total |
| :--- | :---: | :---: | :---: | :---: |
|  | $\$$ | $\$$ | $\$$ | $\$$ |
| Sales | 10,000 | 15,000 | 20,000 | 45,000 |
|  |  |  |  |  |
| Variable cost of sales | 4,000 | 9,000 | 10,000 | 23,000 |
| Fixed costs* | 3,000 | 3,000 | 3,000 | 9,000 |
|  |  |  |  |  |
| Profit | 3,000 | 3,000 | 7,000 | 13,000 |

* general fixed costs absorbed using a unit absorption rate

If the sales revenue mix of products produced and sold were to be changed to: R $20 \%$, $\mathrm{S} 50 \%$, T 30\% then the new average contribution to sales ratio

A would be higher.
B would be lower.

C would remain unchanged.
D cannot be determined without more information.
1.4 Z Limited is a hotel that serves cakes and gateaux in its coffee shop. An analysis of its internal costs has revealed that the variable cost of preparing its own gateaux is $£ 5.50$ per gateau compared to the price of $£ 8 \cdot 00$ per gateau that would be charged by an external bakery. Z Limited employs a chef to prepare the gateaux at a salary of $£ 1,000$ per month. This chef is not able to carry out any other work in the hotel and is the only employee capable of preparing the gateaux.

Calculate the minimum monthly number of sales of gateaux at which it is worthwhile preparing the gateaux in the hotel.

The following data are to be used when answering questions 1.5 to 1.7
M plc is evaluating three possible investment projects and uses a $10 \%$ discount rate to determine their net present values.

| Investment | $A$ | $B$ | $C$ |
| :--- | ---: | ---: | ---: |
|  | $£ 000$ | $£ 000$ | $£ 000$ |
| Initial Investment | 400 | 450 | 350 |
|  |  |  |  |
| Incremental cashflows |  |  |  |
| Year 1 | 100 | 130 | 50 |
| Year 2 | 120 | 130 | 110 |
| Year 3 | 140 | 130 | 130 |
| Year 4 | 120 | 130 | 150 |
| Year 5* | 100 | 150 | 100 |
|  |  |  |  |
| Net present value | 39 | 55 | 48 |

*includes $£ 20,000$ residual value for each investment project.
1.5 Calculate the payback period of investment $A$.
1.6 Calculate the discounted payback period of investment $B$.
1.7 Calculate the Internal Rate of Return (IRR) of investment C.
1.8 A company is preparing a quotation for a new product. The time taken for the first unit of the product was 30 minutes and the company expects an $85 \%$ learning curve. The quotation is to be based on the time taken for the final unit within the learning period which is expected to end after the company has produced 200 units.

Calculate the time per unit to be used for the quotation.
Note: The learning index for an $85 \%$ learning curve is $-0 \cdot 2345$

## End of Section A

Section B starts on the next page

## SECTION B - 30 MARKS

## [the indicative time for answering this section is 54 minutes]

## ANSWER ALL THREE QUESTIONS

## Question Two

A manager is evaluating a three year project which has the following relevant pre-tax operating cashflows:

| Year | 1 | 2 | 3 |
| :--- | :---: | :---: | :---: |
|  | $\$ 000$ | $\$ 000$ | $\$ 000$ |
| Sales | 4,200 | 4,900 | 5,300 |
| Costs | 2,850 | 3,100 | 4,150 |

The project requires an investment of $\$ 2 m$ at the start of year 1 and has no residual value.
The company pays corporation tax on its net relevant operating cashflows at the rate of $20 \%$. Corporation tax is payable in the same year as the net relevant pre-tax operating cashflows arise. There is no tax depreciation available on the investment.

The manager has discounted the net relevant post-tax operating cashflows using the company's post-tax cost of capital of $7 \%$ and this results in a post-tax net present value of the project of $\$ 1 \cdot 018 \mathrm{~m}$.

Required:
(a) Briefly explain sensitivity analysis and how the manager may use it in the evaluation of this project.
(b) Calculate the sensitivity of the project to independent changes in
(i) the selling price;
(ii) the cost of capital.

## Question Three

A firm of financial advisors has established itself by providing high quality, personalised, financial strategy advice. The firm promotes itself by sponsoring local events, advertising, client newsletters, having a flexible attitude towards the times and locations of meetings with clients and seeking new and innovative ideas to discuss with its clients.

The senior manager of the firm has recently noticed that the firm's profitability has declined, with fewer clients being interested in the firm's new investment ideas. Indeed, many clients have admitted to not reading the firm's newsletters.

The senior manager seeks your help in restoring the firm's profitability to its former level and believes that the techniques of Value Analysis and Functional Analysis may be appropriate.

## Required:

(a) Explain the meanings of, and the differences between, Value Analysis and Functional Analysis.
(b) Briefly explain the series of steps that you would take to implement Value Analysis for this organisation.

## Question Four

The Managing Director of a manufacturing company based in Eastern Europe has recently returned from a conference on modern manufacturing. One of the speakers at the conference presented a paper entitled "Compliance versus Conformance - the quality control issue". The Managing Director would like you to explain to her some of the concepts that she heard about at the conference.

## Required:

Prepare a report, addressed to the Managing Director, that discusses quality costs and their significance for the company. Your report should include examples of the different quality costs and their classification within a manufacturing environment.
(10 marks)
Note: 2 marks are available for report format
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## SECTION C - 50 MARKS

## [the indicative time for answering this section is 90 minutes]

ANSWER TWO QUESTIONS OUT OF THREE

## Question Five

AVX Plc assembles circuit boards for use by high technology audio video companies. Due to the rapidly advancing technology in this field, AVX Plc is constantly being challenged to learn new techniques.

AVX Plc uses standard costing to control its costs against targets set by senior managers. The standard labour cost per batch of one particular type of circuit board (CB45) is set out below:

Direct labour-50 hours @ £10 /hour 500

The following labour efficiency variances arose during the first six months of the assembly of CB45:

| Month | Number of batches <br> assembled and sold | Labour Efficiency <br> Variance (£) |
| :--- | :---: | :---: |
| November | 1 | Nil |
| December | 1 | $170 \cdot 00$ Favourable |
| January | 2 | $452 \cdot 20$ Favourable |
| February | 4 | $1,089 \cdot 30$ Favourable |
| March | 8 | $1,711 \cdot 50$ Favourable |
| April | 16 | $3,423 \cdot 00$ Favourable |

An investigation has confirmed that all of the costs were as expected except that there was a learning effect in respect of the direct labour that had not been anticipated when the standard cost was set.

## Required:

(a)
(i) Calculate the monthly rates of learning that applied during the six months;
(ii) Identify when the learning period ended and briefly discuss the implications of your findings for AVX Plc.
(10 marks)

AVX PIc initially priced each batch of CB45 circuit boards on the basis of its standard cost of $£ 960$ plus a mark up of $25 \%$. Recently the company has noticed that, due to increasing competition, it is having difficulty maintaining its sales volume at this price.

The Finance Director has agreed that the long run unit variable cost of the CB45 circuit board is $£ 672 \cdot 72$ per batch. She has suggested that the price charged should be based on an analysis of market demand. She has discovered that at a price of $£ 1,200$ the demand is 16 batches per month, for every $£ 20$ reduction in selling price there is an increase in demand of 1 batch of CB45 circuit boards, and for every $£ 20$ increase in selling price there is a reduction in demand of 1 batch.

Required:
(b) Calculate the profit maximising selling price per batch using the data supplied by the Finance Director
(8 marks)
Note: If Price $(P)=a-b x$ then Marginal Revenue $(M R)=a-2 b x$

The Technical Director cannot understand why there is a need to change the selling price. He argues that this is a highly advanced technological product and that AVX Plc should not reduce its price as this reflects badly on the company. If anything is at fault, he argues, it is the use of Standard Costing and he has asked whether Target Costing should be used instead.

## Required:

(c)
(i) Explain the difference between standard costs and target costs;
(ii) Explain the possible reasons why AVX Plc needs to re-consider its pricing policy now that the CB45 circuit board has been available in the market for six months.
(7 marks)
(Total for Question Five = 25 marks)

## Section C continues on the next page

## Question Six

A health clinic is reviewing its plans for the next three years. It is a not for profit organisation but it has a financial responsibility to manage its costs and to ensure that it provides a value for money service to its clients. The health clinic uses the net present value technique to appraise the financial viability of delivering the service, but it also considers other non-financial factors before making any final decisions.

The present facilities, which incur an annual total cost of $£ 300,000$, are only sufficient to meet a low level of service provision so the manager is considering investing in facilities to meet potential higher levels of demand. For the purpose of evaluating this decision the possible levels of demand for the health clinic's services have been simplified to high, medium or low.

The possible demand for the services in the first year and the level of demand that could follow that specific level in the next years, and their expected probabilities, are as follows:

| Year 1 | Probability | Years 2 and 3 | Probability |
| :--- | :---: | :--- | :---: |
| Low | $30 \%$ | Low | $40 \%$ |
|  |  | Medium | $60 \%$ |
|  |  | High | $0 \%$ |
| Medium | $50 \%$ | Low | $30 \%$ |
|  |  | Medium | $40 \%$ |
|  |  | High | $30 \%$ |
| High | $20 \%$ |  |  |
|  |  | Low | $0 \%$ |
|  |  | Medium | $30 \%$ |
|  |  | High | $70 \%$ |

The level of demand will be the same in years 2 and 3.
The manager is considering two alternative investments in facilities:
Facility A has the capacity to meet the low and medium levels of demand and requires an investment at the start of year 1 of $£ 500,000$. Thereafter it incurs annual fixed costs of $£ 100,000$ and annual variable costs depending on the level of operation. These annual variable costs are expected to be $£ 150,000$ at the low level of operation and $£ 250,000$ at the medium level of operation.

Facility $B$ has the capacity to meet all levels of demand and requires an investment at the start of year 1 of $£ 800,000$. Thereafter it incurs annual fixed costs of $£ 200,000$ and annual variable costs depending on the level of operation. These annual variable costs are expected to be $£ 100,000$ at the low level of operation, $£ 150,000$ at the medium level of operation and $£ 200,000$ at the high level of operation.

Neither of these alternative investments has any residual value at the end of year 3.
If the facilities of the health clinic are insufficient to meet the level of service demand that occurs, the clinic must obtain additional facilities on a yearly contract basis at the following annual costs:

| Level of service provision | Level of service provision | Annual cost of additional |
| :---: | :---: | :---: |
| available internally | demanded | facilities |
| Low | Medium | $£ 100,000$ |
| Low | High | $£ 250,000$ |
| Medium | High | $£ 150,000$ |

These additional facilities are not under the direct control of the health clinic manager.
Note: All monetary values used throughout the question have been stated in terms of their present value. No further discounting is required.

## Required:

(a) Prepare a decision tree to illustrate the investment decision that needs to be made by the manager of the health clinic. (Numerical values are NOT required).
(6 marks)
(b) Advise the manager of the health clinic which investment decision should be undertaken on financial grounds.
(c) Briefly discuss any non-financial factors that the manager should consider before making her final investment decision.

## Question Seven

GHK manufactures four products from different combinations of the same direct materials and direct labour. An extract from the flexible budgets for next quarter for each of these products is as follows:

| Product | $G$ |  | $H$ |  | $J$ |  | $K$ |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | 3,000 | 5,000 | 3,000 | 5,000 | 3,000 | 5,000 | 3,000 | 5,000 |
| Units |  |  |  |  |  |  |  |  |
|  | $\$ 000$ | $\$ 000$ | $\$ 000$ | $\$ 000$ | $\$ 000$ | $\$ 000$ | $\$ 000$ | $\$ 000$ |
| Revenue | 30 | 50 | 60 | 100 | 45 | 75 | 90 | 150 |
|  |  |  |  |  |  |  |  |  |
| Direct Material A (note 1) | 9 | 15 | 12 | 20 | $4 \cdot 5$ | $7 \cdot 5$ | 18 | 30 |
| Direct Material B (note 2) | 6 | 10 | 6 | 10 | $13 \cdot 5$ | $22 \cdot 5$ | 36 | 60 |
| Direct labour (note 3) | 6 | 10 | 24 | 40 | $22 \cdot 5$ | $37 \cdot 5$ | 9 | 15 |
| Overhead (note 4) | 6 | 8 | 13 | 19 | 11 | 17 | 11 | 17 |

## Notes

1 Material A was purchased some time ago at a cost of $\$ 5$ per kg . There are $5,000 \mathrm{kgs}$ in inventory. The costs shown in the flexible budget are based on this historical cost. The material is in regular use and currently has a replacement cost of $\$ 7 \mathrm{per} \mathrm{kg}$.
2 Material B is purchased as required; its expected cost is $\$ 10$ per kg. The costs shown in the flexible budget are based on this expected cost.
3 Direct labour costs are based on an hourly rate of $\$ 10$ per hour. Employees work the number of hours necessary to meet production requirements.
4 Overhead costs of each product include a specific fixed cost of \$1,000 per quarter which would be avoided if the product was to be discontinued. Other fixed overhead costs are apportioned between the products but are not affected by the mix of products manufactured.

GHK has been advised by the only supplier of material $B$ that the quantity of material $B$ that will be available during the next quarter will be limited to $5,000 \mathrm{kgs}$. Accordingly the company is being forced to reconsider its production plan for the next quarter. GHK has already entered into contracts to supply one of its major customers with the following:

500 units of product G
1,600 units of product H 800 units of product $J$ 400 units of product $K$

Apart from this, the demand expected from other customers is expected to be
3,600 units of product $G$
3,000 units of product H
3,000 units of product J
4,000 units of product K
The major customer will not accept partial delivery of the contract and if the contract with this major customer is not completed in full, then GHK will have to pay a financial penalty of $\$ 5,000$.

## Required:

(a) For each of the four products, calculate the relevant contribution per \$ of material $B$ for the next quarter.
(6 marks)
(b) It has been determined that the optimum production plan based on the data above is to produce 4,100 units of product $\mathrm{G}, 4600$ units of product $\mathrm{H}, 800$ units of product J , and 2,417 units of product K . Determine the amount of financial penalty at which GHK would be indifferent between meeting the contract or paying the penalty.
(5 marks)
(c) Calculate the relevant contribution to sales ratios for each of the four products.
(d) Assuming that the limiting factor restrictions no longer apply, prepare a sketch of a multi product profit volume chart by ranking the products according to your contribution to sales ratio calculations based on total market demand. Your sketch should plot the products using the highest contribution to sales ratio first.
(6 marks)
(e) Explain briefly, stating any relevant assumptions and limitations, how the multi product profit volume chart that you prepared in (d) above may be used by the manager of GHK to understand the relationships between costs, volume and profit within the business.
(6 marks)
(Total for Question Seven = 25 marks)
(Total for Section C = 50 marks)

## End of question paper

## Maths Tables and Formulae are on pages 17 to 19

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## PRESENT VALUE TABLE

Present value of $\$ 1$, that is $(1+r)^{-n}$ where $r=$ interest rate; $n=$ number of periods until payment or receipt.

| Periods | Interest rates $(r)$ |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $(n)$ | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 |  |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 |  |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 |  |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 |  |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0705 | 0.666 | 0.630 | 0.596 | 0.564 |  |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 |  |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 |  |
| 9 | 0.914 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 |  |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.350 |  |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 |  |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 |  |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 |  |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 |  |
| 16 | 0.853 | 0.728 | 0.623 | 0.534 | 0.458 | 0.394 | 0.339 | 0.292 | 0.252 | 0.218 |  |
| 17 | 0.844 | 0.714 | 0.605 | 0.513 | 0.436 | 0.371 | 0.317 | 0.270 | 0.231 | 0.198 |  |
| 18 | 0.836 | 0.700 | 0.587 | 0.494 | 0.416 | 0.350 | 0.296 | 0.250 | 0.212 | 0.180 |  |
| 19 | 0.828 | 0.686 | 0.570 | 0.475 | 0.396 | 0.331 | 0.277 | 0.232 | 0.194 | 0.164 |  |
| 20 | 0.820 | 0.673 | 0.554 | 0.456 | 0.377 | 0.312 | 0.258 | 0.215 | 0.178 | 0.149 |  |


| Periods |  |  |  |  |  |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $(n)$ | Interest rates $(r)$ |  |  |  |  |  |  |  |  |  |
|  | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.079 | 0.065 |
| 16 | 0.188 | 0.163 | 0.141 | 0.123 | 0.107 | 0.093 | 0.081 | 0.071 | 0.062 | 0.054 |
| 17 | 0.170 | 0.146 | 0.125 | 0.108 | 0.093 | 0.080 | 0.069 | 0.060 | 0.052 | 0.045 |
| 18 | 0.153 | 0.130 | 0.111 | 0.095 | 0.081 | 0.069 | 0.059 | 0.051 | 0.044 | 0.038 |
| 19 | 0.138 | 0.116 | 0.098 | 0.083 | 0.070 | 0.060 | 0.051 | 0.043 | 0.037 | 0.031 |
| 20 | 0.124 | 0.104 | 0.087 | 0.073 | 0.061 | 0.051 | 0.043 | 0.037 | 0.031 | 0.026 |

Cumulative present value of $\$ 1$ per annum, Receivable or Payable at the end of each year for $n$ years $\frac{1-(1+r)^{-n}}{r}$

| Periods <br> (n) | Interest rates (r) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 |
| 3 | 2.941 | 2.884 | 2.829 | 2.775 | 2.723 | 2.673 | 2.624 | 2.577 | 2.531 | 2.487 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | 3.465 | 3.387 | 3.312 | 3.240 | 3.170 |
| 5 | 4.853 | 4.713 | 4.580 | 4.452 | 4.329 | 4.212 | 4.100 | 3.993 | 3.890 | 3.791 |
| 6 | 5.795 | 5.601 | 5.417 | 5.242 | 5.076 | 4.917 | 4.767 | 4.623 | 4.486 | 4.355 |
| 7 | 6.728 | 6.472 | 6.230 | 6.002 | 5.786 | 5.582 | 5.389 | 5.206 | 5.033 | 4.868 |
| 8 | 7.652 | 7.325 | 7.020 | 6.733 | 6.463 | 6.210 | 5.971 | 5.747 | 5.535 | 5.335 |
| 9 | 8.566 | 8.162 | 7.786 | 7.435 | 7.108 | 6.802 | 6.515 | 6.247 | 5.995 | 5.759 |
| 10 | 9.471 | 8.983 | 8.530 | 8.111 | 7.722 | 7.360 | 7.024 | 6.710 | 6.418 | 6.145 |
| 11 | 10.368 | 9.787 | 9.253 | 8.760 | 8.306 | 7.887 | 7.499 | 7.139 | 6.805 | 6.495 |
| 12 | 11.255 | 10.575 | 9.954 | 9.385 | 8.863 | 8.384 | 7.943 | 7.536 | 7.161 | 6.814 |
| 13 | 12.134 | 11.348 | 10.635 | 9.986 | 9.394 | 8.853 | 8.358 | 7.904 | 7.487 | 7.103 |
| 14 | 13.004 | 12.106 | 11.296 | 10.563 | 9.899 | 9.295 | 8.745 | 8.244 | 7.786 | 7.367 |
| 15 | 13.865 | 12.849 | 11.938 | 11.118 | 10.380 | 9.712 | 9.108 | 8.559 | 8.061 | 7.606 |
| 16 | 14.718 | 13.578 | 12.561 | 11.652 | 10.838 | 10.106 | 9.447 | 8.851 | 8.313 | 7.824 |
| 17 | 15.562 | 14.292 | 13.166 | 12.166 | 11.274 | 10.477 | 9.763 | 9.122 | 8.544 | 8.022 |
| 18 | 16.398 | 14.992 | 13.754 | 12.659 | 11.690 | 10.828 | 10.059 | 9.372 | 8.756 | 8.201 |
| 19 | 17.226 | 15.679 | 14.324 | 13.134 | 12.085 | 11.158 | 10.336 | 9.604 | 8.950 | 8.365 |
| 20 | 18.046 | 16.351 | 14.878 | 13.590 | 12.462 | 11.470 | 10.594 | 9.818 | 9.129 | 8.514 |


| Periods <br> $(n)$ | Interest rates $(r)$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 |
| 3 | 2.444 | 2.402 | 2.361 | 2.322 | 2.283 | 2.246 | 2.210 | 2.174 | 2.140 | 2.106 |
| 4 | 3.102 | 3.037 | 2.974 | 2.914 | 2.855 | 2.798 | 2.743 | 2.690 | 2.639 | 2.589 |
| 5 | 3.696 | 3.605 | 3.517 | 3.433 | 3.352 | 3.274 | 3.199 | 3.127 | 3.058 | 2.991 |
| 6 | 4.231 | 4.111 | 3.998 | 3.889 | 3.784 | 3.685 | 3.589 | 3.498 | 3.410 | 3.326 |
| 7 | 4.712 | 4.564 | 4.423 | 4.288 | 4.160 | 4.039 | 3.922 | 3.812 | 3.706 | 3.605 |
| 8 | 5.146 | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | 4.207 | 4.078 | 3.954 | 3.837 |
| 9 | 5.537 | 5.328 | 5.132 | 4.946 | 4.772 | 4.607 | 4.451 | 4.303 | 4.163 | 4.031 |
| 10 | 5.889 | 5.650 | 5.426 | 5.216 | 5.019 | 4.833 | 4.659 | 4.494 | 4.339 | 4.192 |
| 11 | 6.207 | 5.938 | 5.687 | 5.453 | 5.234 | 5.029 | 4.836 | 4.656 | 4.486 | 4.327 |
| 12 | 6.492 | 6.194 | 5.918 | 5.660 | 5.421 | 5.197 | 4.988 | 7.793 | 4.611 | 4.439 |
| 13 | 6.750 | 6.424 | 6.122 | 5.842 | 5.583 | 5.342 | 5.118 | 4.910 | 4.715 | 4.533 |
| 14 | 6.982 | 6.628 | 6.302 | 6.002 | 5.724 | 5.468 | 5.229 | 5.008 | 4.802 | 4.611 |
| 15 | 7.191 | 6.811 | 6.462 | 6.142 | 5.847 | 5.575 | 5.324 | 5.092 | 4.876 | 4.675 |
| 16 | 7.379 | 6.974 | 6.604 | 6.265 | 5.954 | 5.668 | 5.405 | 5.162 | 4.938 | 4.730 |
| 17 | 7.549 | 7.120 | 6.729 | 6.373 | 6.047 | 5.749 | 5.475 | 5.222 | 4.990 | 4.775 |
| 18 | 7.702 | 7.250 | 6.840 | 6.467 | 6.128 | 5.818 | 5.534 | 5.273 | 5.033 | 4.812 |
| 19 | 7.839 | 7.366 | 6.938 | 6.550 | 6.198 | 5.877 | 5.584 | 5.316 | 5.070 | 4.843 |
| 20 | 7.963 | 7.469 | 7.025 | 6.623 | 6.259 | 5.929 | 5.628 | 5.353 | 5.101 | 4.870 |

## FORMULAE

## Time series

Additive model:
Series = Trend + Seasonal + Random

Multiplicative model:
Series = Trend*Seasonal*Random

## Regression analysis

The linear regression equation of $Y$ on $X$ is given by:

$$
Y=a+b X \quad \text { or } \quad Y-\bar{Y}=b(X-\bar{X}),
$$

where:

$$
b=\frac{\operatorname{Covariance}(X Y)}{\operatorname{Variance}(X)}=\frac{n \sum X Y-\left(\sum X\right)\left(\sum Y\right)}{n \sum X^{2}-\left(\sum X\right)^{2}}
$$

and

$$
a=\bar{Y}-b \bar{X}
$$

or solve

$$
\begin{aligned}
& \sum Y=n a+b \sum X \\
& \sum X Y=a \sum X+b \sum X^{2}
\end{aligned}
$$

Exponential $\quad Y=a b^{x}$
Geometric
$Y=a X^{b}$

## Learning curve

$$
Y_{x}=a X^{b}
$$

where:
$Y_{x}=$ the cumulative average time per unit to produce $X$ units;
$a=$ the time required to produce the first unit of output;
$X=$ the cumulative number of units;
$b=$ the index of learning.
The exponent $b$ is defined as the log of the learning curve improvement rate divided by log 2 .
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## Management Accounting Pillar

## Managerial Level

## P2 - Management Accounting Decision Management

May 2006

Wednesday Morning Session

