## AQA

# LEVEL 3 CERTIFICATE Mathematical Studies 

1350/2B Critical Path Analysis
Mark scheme

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk.

## Glossary for Mark Schemes

Examinations are marked in such a way as to award positive achievement wherever possible. Thus, for mathematics papers, marks are awarded under various categories.
If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| M | mark is for method |
| :--- | :--- |
| dM | mark is dependent on one or more M marks and is for method |
| A | mark is dependent on M or m marks and is for accuracy |
| B | mark is independent of M or m marks and is for method and |
| E | mark is for explanation |
| ft | follow through from previous incorrect result |
| CAO | correct answer only |
| CSO | anything which falls within |
| AWFW | any correct form |
| AWRT | answer given |
| ACF | special case |
| AG | or equivalent <br> SC |
| OE 1 (or 0) accuracy marks |  |
| A2,1 | possibly implied |
| PI | substantially correct approach |
| SCA | significant figure(s) |
| c | decimal place(s) |
| sf | dp |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 1(a) | $1.23 \times 10^{9}$ | B1 |  |
| 1(a) Additional Guidance |  |  |  |
| 1(b) | Label (horizontal) $x$ axis (eg number of users) and/or (vertical) y axis (eg year) or label axis <br> Correctly place the year before the number of users (eg year 2004-2007) <br> Use key to indicate (eg for the ' $m$ ' or indicate what ' $m$ ' is or use ' '000 000s) or make it clear what ' $m$ ' stands for <br> Bar should be drawn in proportion or accept similar explanation or add a scale on the axis <br> Improve title/make it clear what the numbers represent eg what part of the year | E2 | E1 for each valid improvement Ignore any additional but incorrect suggestions <br> SC1 (two errors identified but no suggestions for improvement made) oe for all |


| 1(b) | Additional Guidance |
| :--- | :--- |
|  | E0 for suggesting other form of graphs eg line graph, vertical bar chart etc |
|  |  |


| 1(c) | It should be 608 not 680, making reference <br> to (680-360) <br> He should have stated the number in ' $m$ ' or <br> millions (should put ' $m$ ' next to his numbers) <br> The denominator should be 6 not 5 or seen <br> in calculation <br> He could use a quicker way to calculate <br> using final value - initial value <br> or $\frac{1230-58}{n}$ | B3 |
| :--- | :--- | :--- | :--- |
| He should have stated his answer/the |  |  |
| answer is not given |  |  |$\quad$| Calculating the mean doesn't score a mark |
| :--- |


| Q | Answer | Mark | Comments |
| :--- | :--- | :---: | :--- |
| Alt 1     $900+40$ or 940 M1  <br>  $(40 \div 940) \times 350$ M1 Award M1 for using stratified sampling     <br>  14 or 15 A1      <br>  Says that the data doesn't support the claim <br> or <br> They should have selected 14 or 15 users <br> not 25 <br> or <br> The number of Instagram users selected in <br> the survey is too large E1 Dep on second M1     <br>         |  |  |  |

Alt 2


|  | Alt 3 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 350-25 \text { or } 325 \\ & \text { or } \\ & 900+40 \text { or } 940 \end{aligned}$ | M1 |  |
|  | Using ratios <br> $\frac{325}{25}$ or $\frac{900}{40}$ or 13 or 22.5 <br> or <br> $\frac{325}{350}$ or $\frac{900}{940}$ or $0.92(85 \ldots)$ or $0.95(74 \ldots)$ | M1 |  |
|  | 'not equal' or 'not similar' or 'disproportionate' $\frac{325}{25} \neq \frac{900}{40} \text { or } 13 \neq 22.5$ <br> or $\frac{325}{350} \neq \frac{900}{940} \text { or } 0.92(85 \ldots) \neq 0.95(74 \ldots)$ | A1 | Award A1 for comparing both fractions/decimals/ratios and concluding that they are not equal/disproportionate <br> ft their ' 940 ' $\neq \text { can be implied }$ |
|  | Says that the data doesn't support the claim (must have compared two figures before concluding) | E1 | Dep on second M1 |
|  |  |  |  |


| 1(d) | Additional Guidance |
| :--- | :--- |
|  | For A1, must compare two fractions with same denominator or two decimals or percentages |
|  | Pairs of fractions can be inverted |
|  | Candidates may attempt to work out the actual numbers and compare. Eg <br> $\frac{25}{350} \times 940$ or $67 .(\ldots)$ or $\frac{25}{325} \times 900$ or $69 .(\ldots)$ scores M1M1A1 <br>  <br> Note: 350 must be paired with 940 or 325 must be paired with 900 to score A1 <br> Incorrect pairing can score M1M1A0E1 |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 1(e) | $\begin{aligned} & \hline 50 \times 61.48 \div 1.60 \\ & \text { or } \\ & 2000 \times 1.60 \div 50 \\ & \text { or } \\ & 2000 \times 1.60 \div 61.48 \\ & \text { or } \\ & 50 \times 61.48 \text { and } 2000 \times 1.6 \end{aligned}$ | M1 |  |
|  | (£) 1921.(...) <br> or <br> (\$) 64 <br> or <br> 52.(...) (shares) <br> or <br> (\$) 3074 and (\$) 3200 <br> and statement <br> No she is wrong/not correct | A1 | Allow 1900 or 1920 <br> oe |


| Q | Answer | Mark | Comments |
| :---: | :--- | :--- | :--- |
| 2(a)(i) (Figure 1) <br> The shapes are too close to each other or <br> overlap <br> Can't see where anything is in Central Asia <br> You can't work out the values accurately <br> The lines and the shapes don't correspond <br> with the numbers <br> Use of shapes makes readings inaccurate E1 reason |  | Ignore any additional but incorrect reason <br> oe for all |  |


| 2(a)(ii) | (Table 1) <br> Some data were not shown/missing (eg <br> total population/illiterate men) <br> (On the right column) it got mixed with \% <br> and numbers E1 | E1 for one valid reason |
| :--- | :--- | :---: | :--- |

## 2(a)(ii) Additional Guidance

Suggested improvements can imply the errors

| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| Alt 1 <br> Paul's Statement |  |  |  |
| 2(b) | 0.157 or 15.7\% | B1 |  |
|  | $781 \mathrm{~m} \div$ their ' 0.157 ' or 4975 m (or value rounds to 5billion) | M1 | ft their 0.157 for [0.15,0.18] |
|  | their ' $84.3 \%$ ' of their ' 4975 ' (or value rounds to 5billion) | M1 | their '84.3\%' must be 100 - their [15,18]\% |
|  | 4194 m (or value rounds to 4.2 billion) and Paul is right/statement is correct | A1 | SC2 5billion $\times 84.3 \%=4215 \mathrm{~m}$ and Paul is right SC1 without conclusion |
|  | Alt 2 <br> Paul's Statement |  |  |
|  | 0.157 or 15.7\% | B1 |  |
|  | 4.2 billion $\div$ their ' $84.3 \%$ ' or 4982 m (or value rounds to 5billion) | M1 | their ' $84.3 \%$ ' must be 100 - their '15.7\%' |
|  | their 4982 m (or value rounds to 5billion) x their ' 0.157 or $15.7 \%$ ' | M1 | ft their 0.157 for [0.15,0.18] |
|  | 782 m and Paul is right/statement is correct | A1 | SC2 5 billion $\times 15.7 \%=782 \mathrm{~m}$ and Paul is right SC1 without conclusion |
|  | Rena's statement |  |  |
|  | Cannot use the '20 years/2 decades' alongside the points in the graph/ Graph does not support/Graph cannot be used to check this or <br> Although 20 years cannot be worked out/calculated from the diagram, it is evident that several other regions have made much greater progress from their starting point <br> or <br> Central Asia has made the least progress in terms of raising percentage. <br> or <br> Other regions made greater progress | B1 |  |
|  | Not possible to check/tell/confirm Rena's statement. or Rena is wrong/ Her statement is incorrect. | E1 | ft their reasoning |
| 2(b) | Additional Guidance |  |  |
| \| There are 4 marks for Paul and 2 marks for Rena |  |  |  |



## 3(a) Additional Guidance

|  | Time on $x$-axis may state hours and minutes or just minutes |
| :--- | :--- |
|  | For $1^{\text {st }}$ |

For $1^{\text {st }} \mathrm{M} 1$ not all activities starting at zero

|  |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathbf{Q}$ | Answer | Mark | Comments |

3(b) H B1

3(b) Additional Guidance

| 4(a) | 6 or 13 seen <br> $=\frac{6}{13}$ | B1 |  |
| :---: | :--- | :--- | :--- |


| 4(a) Additional Guidance |  |
| :--- | :--- |
|  |  |
|  |  |


| 4(b) $\text { Alt } 1$ | $66+4+2+5$ $\text { = } 77 \text { (\%) }$ | M1 A1 | Attempts to sum the percentages not in the hay fever circle <br> oe fraction, decimal or percentage |
| :---: | :---: | :---: | :---: |
| 4(b) $\text { Alt } 2$ | $100-(14+3+5+1)$ $77 \text { (\%) }$ | M1 <br> A1 | Attempts to subtract percentages in the hay fever circle from 100 <br> oe fraction, decimal or percentage |


| 4(b) Additional Guidance |  |
| :--- | :--- |
|  |  |
|  |  |
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| 4(c) | Person chosen at random may not be <br> taking medication for hay fever at that <br> precise moment in time | E1 | May not be on medication/ wrong time of year <br> for hay fever/ may use natural remedies/ fewer <br> people may have developed hay fever since the <br> study was conducted |
| :---: | :--- | :---: | :--- |

## 4(c) Additional Guidance

|  | Allow any reasonable statements |
| :--- | :--- |
|  |  |
|  |  |


| Q Answer | Mark | Comments |  |
| :---: | :--- | :---: | :--- |
| 5(a) |  |  | 0.31 seen |
|  | $0.29(45)$ | M1 |  |


| 5(a) Additional Guidance |  |
| :--- | :--- |
|  |  |
|  |  |
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| $\begin{aligned} & \text { 5(b) } \\ & \text { Alt } 1 \end{aligned}$ | Use of 'their' part (a) or 0.2945 seen $0.69 \times 0.85$ or 0.5865 seen <br> $0.2945+0.5865$ or 0.881 seen $0.881 \times 200 \times 40$ <br> or <br> 176.2 or 35.24 seen <br> (£) 7048 | M1 <br> M1 <br> M1 <br> M1 <br> A1ft | Probability of sales by telephone <br> Probability of sales from internet <br> Sums 'their' 0.2945 and 'their' 0.5865 <br> Multiplies 'their' probability by 200 or 40 <br> ft from part (a) Total expected sales |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { 5(b) } \\ & \text { Alt } 2 \end{aligned}$ | Use of 'their' part (a) or 0.2945 seen <br> $0.2945 \times 200 \times 40$ or 2356 <br> $0.69 \times 0.85$ or 0.5865 <br> $0.5865 \times 200 \times 40$ or 4692 <br> $(£ 2356+£ 4692)=(£) 7048$ | M1 <br> M1 <br> M1 <br> M1 <br> A1 | Probability of sales by telephone <br> Expected sales by telephone or 'their' part (a) $\times 200 \times 40$ <br> Probability of sales from internet. <br> Expected sales from internet or 'their' $0.5865 \times 200 \times 40$ <br> ft from part (a) Total expected sales |
| $\begin{aligned} & \text { 5(b) } \\ & \text { Alt } 3 \end{aligned}$ | Use of 'their' part (a) or 0.2945 seen $0.69 \times 0.85$ or 0.5865 seen $0.2945+0.5865 \text { or } 0.881 \text { seen }$ $(0.881 \times 200)=176.2$ <br> 176 people when rounded or $176 \times 40$ <br> (£) 7040 | M1 <br> M1 <br> M1 <br> M1 <br> A1 | Probability of sales by telephone Probability of sales from internet <br> Sums 'their' 0.2945 and 'their' 0.5865 <br> Multiplies 'their' probability by 200 and then rounds to nearest whole number of people <br> ft from part (a) Total expected sales |

\begin{tabular}{|c|c|c|c|c|}
\hline \[
\begin{gathered}
\text { 5(b) } \\
\text { Alt } 4
\end{gathered}
\] \& \begin{tabular}{l}
\(200 \times 0.69\) or 138 and \\
\(200-138\) or \(200 \times 0.31\) or 62 \\
\(138 \times 0.85\) or 117.3 or 117 \\
\(62 \times 0.95\) or 58.9 or 59 \\
Their 117 + their 59 or 176 \\
(176×40 =) \\
(£) 7040
\end{tabular} \& M1
M1
M1
M1
M \& \begin{tabular}{l}
For both \\
ft from part (a)
\end{tabular} \& Total expected sales \\
\hline \[
\begin{aligned}
\& \text { 5(b) } \\
\& \text { Alt } 4
\end{aligned}
\] \& \begin{tabular}{l}
\(200 \times 0.69\) or 138 and \\
\(200-138\) or \(200 \times 0.31\) or 62 \\
\(138 \times 0.85\) or 117.3 or 117 \\
\(62 \times 0.95\) or 58.9 or 59 \\
\(59 \times 40\) or 2360 and \(117 \times 40\) or 4680
\[
(2360+4680=)
\] \\
(£) 7040
\end{tabular} \& M1
M1
M1
M1

A1 \& | For both |
| :--- |
| For both | \& Total expected sales <br>

\hline \multicolumn{5}{|l|}{5(b) Additional Guidance} <br>
\hline - ${ }^{\text {Probabilities may be expressed explicitly or may be expressed as a tree diagram }}$ \& \multicolumn{4}{|l|}{Probabilities may be expressed explicitly or may be expressed as a tree diagram} <br>
\hline \& \multicolumn{4}{|l|}{Check method used} <br>
\hline
\end{tabular}

| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| $\begin{gathered} \hline 6(a) \\ \text { Alt } 1 \end{gathered}$ | 250 <br> (600-800) or -200 <br> or <br> (1500-800) or 700 <br> $\frac{93}{310}=0.3$ or $\frac{217}{310}=0.7$ used as a <br> probability <br> Their 0.3 x their -200 or their 0.7 x their 700 <br> their $0.3 \times$ their $-200+$ their $0.7 \times$ their 700 or 430 <br> (250 < 430) so Agricultural Show | M1 <br> M1 <br> M1 <br> A1 <br> E1 | Expected profit at CF <br> Attempts to subtract fee from expected takings at AS <br> Used only in AS calculations <br> ft their values <br> Expected profit at AS <br> Dep A1 |
| 6(a) $\text { Alt } 2$ | $\begin{aligned} & (450-200) \text { or } 250 \\ & \frac{93}{310}=0.3 \text { or } \frac{217}{310}=0.7 \text { used as a } \\ & \text { probability } \\ & \text { Their } 0.3 \times 600 \text { or their } 0.7 \times 1500 \\ & \text { their } 0.3 \times 600+\text { their } 0.7 \times 1500 \text { or } 1230 \\ & 1230-800 \text { or } 430 \\ & (250<430) \text { Agricultural Show } \\ & \hline \end{aligned}$ | B1 <br> M1 <br> M1 <br> M1 <br> A1 <br> E1 | Expected profit at CF <br> Used only in AS calculations <br> their total expected takings at AS <br> Expected profit at AS <br> Dep A1 |


| 6 (a) Additional guidance |  |
| :--- | :--- |
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|  |  |
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| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\begin{aligned} & \text { 6(b) } \\ & \text { Alt } 1 \end{aligned}$ | $(0.3 \times(600+300))+0.7 \times 1500$ Or <br> (£) 1320 <br> their 1320-800-100 <br> (£) 420 <br> This is less than the expected profit without insurance so Lila should not take out insurance | M1 <br> M1 <br> A1 | Calculates the expected takings including insurance payout and returned cost of insurance. <br> Subtracts fee and insurance costs from their expected takings. |
| :---: | :---: | :---: | :---: |
| 6(b) $\text { Alt } 2$ | If rains takings $(=600+300)=900$ <br> Costs $(=800+100)=900$ <br> Part of expected profit from rain(= $0 x$ $0.3)=(£) 0$ <br> If does not rain takings $=1500$ <br> Costs $(=800+100)=900$ <br> Part of expected profit from no rain (= $600 \times 0.7)=(£) 420$ <br> Expected profit $=(£) 420$ <br> This is less than the expected profit without insurance so Lila should not take out insurance | M1 <br> M1 <br> A1 | Subtract costs from takings to get expected profit if it rains <br> Subtracts costs from takings to get expected profit if it does not rain |
| 6(b) $\text { Alt } 3$ | $0.3 \times 300 \text { or } 90$ $90<100 \text { or } 90-100=-10$ <br> Negative profit / she makes a loss | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | Expected profit calculated |
| 6(b) <br> Alt 4 | $\begin{aligned} & ((300-100) \times 0.3)=60 \\ & (100 \times 0.7)=70 \\ & \\ & 60-70 \text { or }-10 \\ & \text { Expected loss so Lila should not take } \\ & \text { our insurance } \\ & \text { or } \\ & (430+60-70)=(£) 420 \\ & \text { This is less than the expected profit } \\ & \text { without insurance so Lila should not } \\ & \text { take out insurance } \end{aligned}$ | M1 M1 A1 | Finds extra profit from insurance payout if rains <br> Finds extra cost of taking insurance if no rain <br> Uses the expected profit from part (a) to correctly find the expected profit with insurance |

## 6(b) Additional guidance

| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 7(a) | Network, at least 5 activities and 4 arcs <br> Task B immediately preceding tasks F, C and J only <br> Only tasks F, E and G immediately preceding task H <br> Activity network correct <br> Start times at C, F and J correct <br> Start time at H correct <br> All start times correct <br> Finish times correct at $\mathrm{H}, \mathrm{I}, \mathrm{K}, \mathrm{L}$ <br> Finish time correct at $D$ <br> B1 <br> M1 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 <br> M1 Allow follow through from their part (a) <br> M1 FT <br> All finish times correct |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
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## 7(a) Additional guidance

|  | Arrows are not required on arcs as long as the direction is obvious |
| :--- | :--- |
|  | Any mark for finish time can only be awarded if (finish time) < (start time) |


| Q | Answer | Mark | Comments |
| :---: | :--- | :---: | :---: |
| 7(b) ABCDEHL B1  <br> 7(b) Additional guidance    <br>     <br>     |  |  |  |


| 7(c) <br> Alt 1 | $(20-15)=5$ days extra needed for <br> task I <br>  <br>  <br> $(5-2)=3$ days extra overall <br> 65 | B1 |  |
| :---: | :--- | :---: | :--- |
| 7(c) | $44+20$ or 64 | A1 | FT their latest finish time for L in part 6(a) |
| Alt 2 'their float time' |  |  |  |
|  | $64+1$ | M1 |  |
|  | 65 | M1 |  |

## 7(c) Additional guidance

