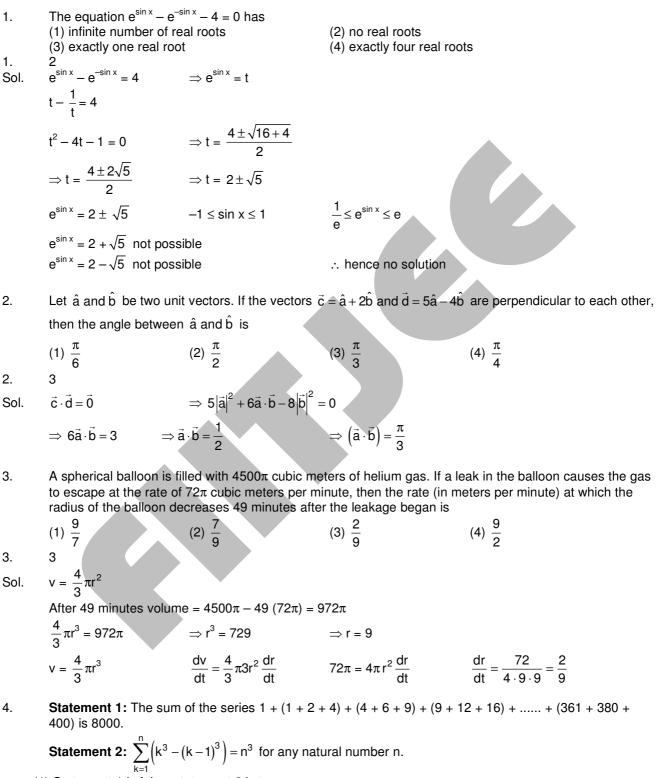
# AIEEE-2012 (Set - C)

### **IMPORTANT INSTRUCTIONS**

- 1. Immediately fill in the particulars on this page of the Test Booklet with *Blue/Black Ball Point Pen. Use of pencil is strictly prohibited.*
- 2. The Answer Sheet is kept inside this Test Booklet. When you are directed to open the Test Booklet, take out the Answer Sheet and fill in the particulars carefully.
- 3. The test is of **3** hours duration.
- 4. The Test Booklet consists of **90** questions. The maximum marks are **360**.
- 5. There are *three* parts in the question paper A, B, C consisting of **Mathematics**, **Physics** and **Chemistry** having 30 questions in each part of equal weightage. Each question is allotted 4 (four) marks for each correct response.
- 6. Candidates will be awarded marks as stated above in instruction No.5 for correct response of each question. 1/4 (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
- 7. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 6 above.
- 8. Use *Blue/Black Ball Point Pen only* for writing particulars/marking responses on *Side-1* and *Side-2* of the Answer Sheet. *Use of pencil is strictly prohibited.*
- 9. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc., except the Admit Card inside the examination hall/room.
- 10. Rough work is to be done on the space provided for this purpose in the Test Booklet only. This space is given at the bottom of each page and in **3** pages (Pages **21 23**) at the end of the booklet.
- 11. On completion of the test, the candidate must hand over the Answer Sheet to the Invigilator on duty in the Room/Hall. *However, the candidates are allowed to take away this Test Booklet with them.*
- 12. The CODE for this Booklet is **C**. Make sure that the CODE printed on **Side-2** of the Answer Sheet is the same as that on this booklet. In case of discrepancy, the candidate should immediately report the matter to the Invigilator for replacement of both the Test Booklet and the Answer Sheet.
- 13. Do not fold or make any stray marks on the Answer Sheet.

## **PART A: MATHEMATICS**



(1) Statement 1 is false, statement 2 is true

(2) Statement 1 is true, statement 2 is true; statement 2 is a correct explanation for statement 1

(3) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1

dx

(4) Statement 1 is true, statement 2 is false

4.

- Sol. Statement 1 has 20 terms whose sum is 8000 And statement 2 is true and supporting statement 1.  $\therefore k^{\text{th}}$  bracket is  $(k - 1)^2 + k(k - 1) + k^2 = 3k^2 - 3k + 1$ .
- 5. The negation of the statement "If I become a teacher, then I will open a school" is
  (1) I will become a teacher and I will not open a school
  (2) Either I will not become a teacher or I will not open a school
  (3) Neither I will become a teacher nor I will open a school
  (4) I will not become a teacher or I will open a school
  5. 1

Sol. 
$$\sim (\sim p \lor q) = p \land \sim q$$

6. If the integral 
$$\int \frac{5 \tan x}{\tan x - 2} dx = x + a \ln |\sin x - 2 \cos x| + k$$
, then a is equal to  
(1) -1 (2) -2 (3) 1 (4) 2

- Sol.  $\int \frac{5\tan x}{\tan x 2} dx = \int \frac{5\sin x}{\sin x 2\cos x} dx \qquad \Rightarrow \int \left[ \frac{2(\cos x + 2\sin x) + (\sin x 2\cos x)}{\sin x 2\cos x} \right]$  $= 2 \int \left( \frac{\cos x + 2\sin x}{\sin x 2\cos x} \right) dx + \int dx + k \qquad = 2 \log |\sin x 2\cos x| + x + k \quad \therefore a = 2$
- 7. **Statement 1:** An equation of a common tangent to the parabola  $y^2 = 16\sqrt{3}x$  and the ellipse  $2x^2 + y^2 = 4$  is  $y = 2x + 2\sqrt{3}$ .

**Statement 2:** If the line  $y = mx + \frac{4\sqrt{3}}{m}$ ,  $(m \neq 0)$  is a common tangent to the parabola

 $y^2 = 16\sqrt{3}x$  and the ellipse  $2x^2 + y^2 = 4$ , then m satisfies  $m^4 + 2m^2 = 24$ .

- (1) Statement 1 is false, statement 2 is true
- (2) Statement 1 is true, statement 2 is true; statement 2 is a correct explanation for statement 1
- (3) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1
- (4) Statement 1 is true, statement 2 is false

7. 2  
Sol. 
$$y^2 = 16\sqrt{3}x$$
  $\frac{x^2}{2} + \frac{y^2}{4} = 1$   
 $y = mx + \frac{4\sqrt{3}}{m}$  is tangent to parabola  
which is tangent to ellipse  $\Rightarrow c^2 = a^2m^2 + b^2$   
 $\Rightarrow \frac{48}{m^2} = 2m^2 + 4$   $\Rightarrow m^4 + 2m^2 = 24$   $\Rightarrow m^2 = 4$   
8. Let  $A = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 2 & 1 \end{pmatrix}$ . If  $u_1$  and  $u_2$  are column matrices such that  $Au_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$  and  $Au_2 = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$ , then  $u_1 + u_2$  is  
equal to  
 $(1) \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}$   $(2) \begin{pmatrix} -1 \\ 1 \\ -1 \end{pmatrix}$   $(3) \begin{pmatrix} -1 \\ -1 \\ 0 \end{pmatrix}$   $(4) \begin{pmatrix} 1 \\ -1 \\ -1 \end{pmatrix}$   
8. 4

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Sol. 
$$A = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 2 & 1 \end{pmatrix}$$

$$Let u_{1} = \begin{bmatrix} a \\ b \\ c \end{bmatrix} : u_{2} = \begin{bmatrix} d \\ e \\ 1 \end{bmatrix}$$

$$Au_{1} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \implies u_{1} = \begin{bmatrix} -2 \\ 1 \\ -2 \end{bmatrix} \implies u_{1} + u_{2} = \begin{bmatrix} 1 \\ -1 \\ -1 \end{bmatrix}$$

$$Au_{2} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \implies u_{2} = \begin{bmatrix} 0 \\ 1 \\ -2 \end{bmatrix} \implies u_{1} + u_{2} = \begin{bmatrix} 1 \\ -1 \\ -1 \end{bmatrix}$$
9. If n is a positive integer, then  $(\sqrt{3} + 1)^{2n} - (\sqrt{3} - 1)^{2n}$  is
(1) an irrational number
(2) an odd positive integer
(3) an even positive integer
(4) a rational number other than positive integers
(3) an even positive integer
(4) a rational number other than positive integers
(5) 1
$$(\sqrt{3} + 1)^{2n} - (\sqrt{3} - 1)^{2n} = \left[ (\sqrt{3} + 1)^{2} \right]^{n} - \left[ (\sqrt{3} - 1)^{2} \right]^{n} = (4 + 2\sqrt{3})^{n} - (4 - 2\sqrt{3})^{n}$$

$$= 2^{n} \left[ (2 + \sqrt{3})^{n} - (2 - \sqrt{3})^{n} \right]$$

$$= 2^{n+1} \left[ (-C_{2}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] - \left[ (-C_{0}2^{n} - (-C_{0}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 - \cdots + -) \right] \right]$$

$$= 2^{n+1} \left[ (-C_{2}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] - \left[ (-C_{0}2^{n} - (-C_{0}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 - \cdots + -) \right] \right]$$

$$= 2^{n+1} \left[ (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] - \left[ (-C_{0}2^{n} - (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 - \cdots + -) \right] \right]$$

$$= 2^{n+1} \left[ (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] - \left[ (\sqrt{3} - 1)^{2n} + (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 - \cdots + -) \right] \right]$$

$$= 2^{n+1} \left[ (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] - \left[ (\sqrt{3} - 1)^{2n} + (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 - \cdots + -) \right] \right]$$

$$= 2^{n+1} \left[ (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] - \left[ (\sqrt{3} - 1)^{2n} + (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 - \cdots + -) \right] \right]$$

$$= 2^{n+1} \left[ (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] - \left[ (\sqrt{3} - 1)^{2n} + (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] \right]$$

$$= 2^{n+1} \left[ (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] - \left[ (\sqrt{3} - (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] \right]$$

$$= 2^{n+1} \left[ (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] - \left[ (\sqrt{3} - \sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] \right]$$

$$= 2^{n+1} \left[ (-C_{1}2^{n-1}\sqrt{3} + (-C_{2}2^{n-2}3 + \cdots + -) \right] = \left[ (\sqrt{3} - \sqrt{3} + (-C_{2}2^{n-2}3$$

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(3) 
$$x - 2y + 2z - 1 = 0$$
  
12. 1  
Sol Equation of plane parallel to  $x - 2y + 2z - 5 = 0$  is  $x - 2y + 2z + k = 0$  (1)

SOI. Equation of plane parallel to x -∠y+2z+K= ..... (1) perpendicular distance from O(0, 0, 0) to (1) is 1 h.l

$$\frac{|\mathsf{K}|}{\sqrt{1+4+4}} = 1 \qquad \Rightarrow |\mathsf{k}| = 3 \qquad \Rightarrow \mathsf{k} = \pm 3 \qquad \therefore \ \mathsf{x} - 2\mathsf{y} + 2\mathsf{z} - 3 = 0$$

If the line 2x + y = k passes through the point which divides the line segment joining the points (1, 1) and 13. (2, 4) in the ratio 3 : 2, then k equals 29

(3) 6

Sol. Point 
$$p = \left(\frac{6+2}{5}\right)$$

5

(1)

Point p = 
$$\left(\frac{6+2}{5}, \frac{12+2}{5}\right)$$
  
p =  $\left(\frac{8}{5}, \frac{14}{5}\right)$   
p $\left(\frac{8}{5}, \frac{14}{5}\right)$  lies on 2x + y = k  $\Rightarrow \frac{16}{5} + \frac{14}{5} = k \Rightarrow k = \frac{30}{5} = 6$ 

- Let  $x_1, x_2, \dots, x_n$  be n observations, and let  $\overline{x}$  be their arithematic mean and  $\sigma^2$  be their variance. 14. **Statement 1:** Variance of  $2x_1$ ,  $2x_2$ , .....,  $2x_n$  is  $4 \sigma^2$ .
  - Statement 2: Arithmetic mean of  $2x_1, 2x_2, \dots, 2x_n$  is  $4\overline{x}$ .

(2)5

- (1) Statement 1 is false, statement 2 is true
- (2) Statement 1 is true, statement 2 is true; statement 2 is a correct explanation for statement 1
- (3) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1
- (4) Statement 1 is true, statement 2 is false
- 14.
- $\sigma^2 = \sum \frac{x_i^2}{n} \left(\sum \frac{x_i}{n}\right)^2$ Sol.

 $2\int \frac{d(p(t))}{p(t) - 900} = \int dt$ 

Variance of 
$$2x_1, 2x_2, \dots, 2x_n = \sum \frac{(2x_i)^2}{n} - \left(\sum \frac{2x_i}{n}\right)^2 = 4\left[\sum \frac{x_i^2}{n} - \left(\sum \frac{x_i}{n}\right)^2\right] = 4\sigma^2$$
  
Statement 1 is true.

A.M. of 
$$2x_1, 2x_2, \dots, 2x_n = \frac{2x_1 + 2x_2 + \dots + 2x_n}{n} = 2\left(\frac{x_1 + x_2 + \dots + x_n}{n}\right) = 2\overline{x}$$
  
Statement 2 is false

The population p(t) at time t of a certain mouse species satisfies the differential equation  $\frac{dp(t)}{dt} = 0.5 p(t)$ 15. -450. If p(0) = 850, then the time at which the population becomes zero is

(1) 2 ln 18 (2) ln 9 (3) 
$$\frac{1}{2}$$
ln 18 (4) ln 18  
15. 1  
Sol.  $\frac{d(p(t))}{dt} = \frac{1}{2}p(t) - 450$   
 $\frac{d(p(t))}{dt} = \frac{p(t) - 900}{2}$ 

 $2 \ln |p(t) - 900| = t + c$ t = 0  $\Rightarrow$  2 ln 50 = 0 + c ⇒ c = 2 ln 50  $\therefore 2 \ln |p(t) - 900| = t + 2 \ln 50$ P(t) = 0 $\Rightarrow$  2 ln 900 = t + 2 ln 50 t = 2 (ln 900 – ln 50) =  $2 \ln \left( \frac{900}{50} \right) = 2 \ln 18.$ 

Let a, b  $\in$  R be such that the function f given by f(x) = ln |x| + bx<sup>2</sup> + ax, x \neq 0 has extreme values at x = -1 16. and x = 2.

**Statement 1:** f has local maximum at x = -1 and at x = 2.

**Statement 2:** 
$$a = \frac{1}{2}$$
 and  $b = \frac{-1}{4}$ 

- (1) Statement 1 is false, statement 2 is true
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- (4) Statement 1 is true, statement 2 is false

16.

 $f'(x) = \frac{1}{x} + 2b x + a$ Sol.

2

f has extremevalues and differentiable

$$\Rightarrow t'(-1) = 0 \qquad \Rightarrow a - 2b = 1$$
  
$$f'(2) = 0 \qquad \Rightarrow a + 4b = -\frac{1}{2} \qquad \Rightarrow a = \frac{1}{2}, b = -\frac{1}{2}$$

f''(-1), f''(2) are negative. f has local maxima at -1, 2

The area bounded between the parabolas  $x^2 = \frac{y}{4}$  and  $x^2 = 9y$ , and the straight line y = 2 is 17.

(1) 
$$20\sqrt{2}$$
 (2)  $\frac{10\sqrt{2}}{3}$  (3)  $\frac{20\sqrt{2}}{3}$   
17. 3  
Sol. Required area  
 $17. -5 \int_{-1}^{2} \int_{-1}^{2}$ 

$$A = 2 \left[ \int_{0}^{1} \left( 3\sqrt{y} - \frac{\sqrt{y}}{2} \right) dy \right] = 2 \int_{0}^{1} \frac{\sqrt{y}}{2} dy$$
  
=  $5 \left[ \frac{y^{3/2}}{3/2} \right]_{0}^{2} = \frac{10}{3} \left[ 2^{3/2} - 0 \right] = \frac{20\sqrt{2}}{3}$ 

18. Assuming the balls to be identical except for difference in colours, the number of ways in which one or more balls can be selected from 10 white, 9 green and 7 black balls is (1) 880 (2) 629 (3) 630 (4) 879 4

(4) 10√2

 $x^{2} = 9y$   $x^{2} = \frac{9}{4}$ 

- 18.
- Number of ways of selecting one or more balls from 10 white, 9 green, and 7 black balls Sol.  $= (10 + 1)(9 + 1)(7 + 1) - 1 = 11 \times 10 \times 8 - 1 = 879.$

19. If f: 
$$R \to R$$
 is a function defined by  $f(x) = [x] \cos\left(\frac{2x-1}{2}\right)\pi$ , where [x] denotes the greatest integer function, then f is  
(1) continuous for every real x (2) discontinuous only at  $x = 0$   
(3) discontinuous only at non-zero integral values of x (4) continuous only at  $x = 0$   
19. 1

Sol. 
$$f(x) = \left[x\right] \cos\left(\frac{2x-1}{2}\right) \pi = \left[x\right] \cos\left(x-\frac{1}{2}\right) \pi$$
$$= \left[x\right] \sin \pi x \text{ is continuous for every real x.}$$
20. If the lines  $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-1}{4}$  and  $\frac{x-3}{1} = \frac{y-k}{2} = \frac{z}{1}$  intersect, then k is equal to  
(1) -1 (2)  $\frac{2}{9}$  (3)  $\frac{9}{2}$  (4) 0  
20. 3  
Sol. Any point on  $\frac{x-3}{1} = \frac{y+1}{2} = \frac{z-4}{4} = 1$  is  $(2t+1, 3t-1, 4t+1)$   
And any point on  $\frac{x-3}{1} = \frac{y-k}{2} = \frac{z}{1} = s$  is  $(s+3, 2s+k, s)$   
Given lines are intersecting  $\Rightarrow t = -\frac{3}{2}$  and  $s = -5$   $\therefore k = \frac{9}{2}$   
21. Three numbers are chosen at random without replacement from {1, 2, 3, ..., 8}. The probability that their  
minimum is 3, given that their maximum is 6, is  
(1)  $\frac{3}{8}$  (2)  $\frac{1}{5}$  (3)  $\frac{1}{4}$  (4)  $\frac{2}{5}$   
21. 2  
23. Let A be the event that maximum is 6.  
B be event that minimum is 3  
P(A)  $= \frac{^{5}C_{2}}{^{6}C_{3}}$  (the numbers > 3 are 5)  
P(B)  $= \frac{^{5}C_{2}}{^{6}C_{3}}$  (the numbers > 3 are 5)  
P(A  $\cap B) = \frac{^{2}C_{1}}{^{2}C_{3}}$   
Required probability is  $P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)} = \frac{^{2}C_{1}}{^{5}C_{2}} = \frac{2}{10} = \frac{1}{5}$ .  
22. If  $z \neq 1$  and  $\frac{z^{2}}{z-1}$  is real, then the point represented by the complex number z lies  
(1) either on the real axis or on a circle napssing through the origin  
(2) on a circle with earting in a z = 1)  
 $z^{2} = (x^{2} - y^{2}) + i(2xy)$   
 $\frac{z^{2}}{z-1}$  is real  $\Rightarrow$  its imaginary part = 0  
 $\Rightarrow 2xy(x - 1) - y(x^{2} - y^{2}) = 0$   
 $\Rightarrow y(x^{2} + y^{2} - z) = 0$ 

 $\therefore$  z lies either on real axis or on a circle through origin.

Let P and Q be  $3 \times 3$  matrices with P  $\neq$  Q. If P<sup>3</sup> = Q<sup>3</sup> and P<sup>2</sup>Q = Q<sup>2</sup>P, then determinant of 23.  $(P^2 + Q^2)$  is equal to (1) - 2(2) 1 (3) 0 (4) - 123. 3  $\begin{array}{l} 3 \\ P^{3} = Q^{3} \\ P^{3} - P^{2}Q = Q^{3} - Q^{2}P \\ P^{2}(P - Q) = Q^{2}(Q - P) \\ P^{2}(P - Q) + Q^{2}(P - Q) = O \\ (P^{2} + Q^{2})(P - Q) = O \qquad \Rightarrow |P^{2} + Q^{2}| = 0 \end{array}$ Sol. If  $g(x) = \int_{0}^{x} \cos 4t \, dt$ , then  $g(x + \pi)$  equals 24. (1)  $\frac{g(x)}{g(\pi)}$ (2)  $g(x) + g(\pi)$  (3)  $g(x) - g(\pi)$ (4)  $g(x) , g(\pi)$ 24. 2 or 4  $g(x) = \int \cos 4t \, dt$ Sol.  $\Rightarrow g(x) = \frac{\sin 4x}{4} + k \qquad \Rightarrow g(x) = \frac{\sin 4x}{4} [\because g(0) = 0]$  $\Rightarrow$  g'(x) = cos 4x  $g(x + \pi) = g(x) + g(\pi) = g(x) - g(\pi)$  (:  $g(\pi) = 0$ ) The length of the diameter of the circle which touches the x-axis at the point (1, 0) and passes through 25. the point (2, 3) is (1)  $\frac{10}{3}$ (2)  $\frac{3}{5}$ 6 5 (4)  $\frac{5}{3}$ (3) 25. Let (h, k) be centre.  $(h - 1)^{2} + (k - 0)^{2} = k^{2} \implies h = 1$ Sol.  $(h-2)^{2} + (k-3)^{2} = k^{2} \implies k = \frac{5}{3}$ (h, k) (2, 3)k k  $\therefore$  diameter is  $2k = \frac{10}{3}$ (1, 0)26. Let X = {1, 2, 3, 4, 5}. The number of different ordered pairs (Y, Z) that can be formed such that  $Y \subseteq X, Z$  $\subseteq$  X and Y  $\cap$  Z is empty, is (2) 3<sup>5</sup>  $(3) 2^5$  $(4) 5^3$ (1) 5<sup>2</sup> 26. 2  $Y \subseteq X, Z \subseteq X$ Sol. Let  $a \in X$ , then we have following chances that  $\begin{array}{ll} (1) \ a \in \ Y, & a \in \ Z \\ (2) \ a \notin \ Y, & a \in \ Z \end{array}$  $(3) a \in Y, \quad a \notin Z$ (4) a ∉ Y, a ∉ Z We require  $Y \cap Z = \phi$ Hence (2), (3), (4) are chances for 'a' to satisfy  $Y \cap Z = \phi$ .  $\therefore$  Y  $\cap$  Z =  $\phi$  has 3 chances for a. Hence for five elements of X, the number of required chances is  $3 \times 3 \times 3 \times 3 \times 3 = 3^{5}$ 27.

27. An ellipse is drawn by taking a diameter of the circle  $(x - 1)^2 + y^2 = 1$  as its semiminor axis and a diameter of the circle  $x^2 + (y - 2)^2 = 4$  as its semi-major axis. If the centre of the ellipse is the origin and its axes are the coordinate axes, then the equation of the ellipse is

(1) 
$$4x^2 + y^2 = 4$$
 (2)  $x^2 + 4y^2 = 8$  (3)  $4x^2 + y^2 = 8$  (4)  $x^2 + 4y^2 = 16$   
27. 4  
Sol. Semi minor axis b = 2  
Semi major axis a = 4  
Equation of ellipse  $= \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$   $\Rightarrow \frac{x^2}{16} + \frac{y^2}{4} = 1$   
 $\Rightarrow x^2 + 4y^2 = 16$ .  
28. Consider the function  $f(x) = |x - 2| + |x - 5|, x \in \mathbb{R}$ .  
Statement 1: f(4) = 0  
Statement 1: f(4) = 0  
Statement 1: is false, statement 2 is true  
(2) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1  
(3) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1  
(4) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1  
(4) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1  
(4) Statement 1 is true, statement 2 is false  
28.  
Sol.  $f(x) = 7 - 2x; x < 2$   
 $= 3; 2 \le x \le 5$   
 $= 2x - 7; x > 5$   
 $f(x)$  is constant function in [2, 5]  
f is continuous in [2, 5] and differentiable in (2, 5) and f(2) = f(5)  
by Rolle's theorem f(4) = 0  
 $\therefore$  Statement 1 both are true and statement 2 is correct explanation for statement 1.  
29. A line is drawn through the point (1, 2) to meet the coordinate axes at P and Q such that it forms a triangle OPQ, where O is the origin. If the area of the triangle OPG is least, then the slope of the line PQ is  
(1)  $-\frac{1}{4}$  (2)  $-4$  (3)  $-2$  (4)  $-\frac{1}{2}$   
39.  
Sol. Equation of line passing through (1, 2) with slope m is  $y - 2 = m(x - 1)$   
Area of  $\Delta OPQ = \frac{(m-2)^2}{2|m|}$   
 $\Delta = \frac{m^2 + 4 - 4m}{2m}$   $\Delta = \frac{m}{2} + \frac{2}{m} - 2$   
 $\Delta$  is least if  $\frac{m}{2} = \frac{2}{m}$   $\Rightarrow m^2 = 4$   $\Rightarrow m = \pm 2$   $\Rightarrow m = -2$   
30. Let ABCD be a parallelogram such that  $\overline{AB} = \overline{q}, \overline{AD} = \overline{p}$  and  $\angle BAD$  be an acute angle. If  $\overline{r}$  is the vector that coincides with the altitude directed from the vertex B to the side AD, then  $\overline{r}$  is given by  
(1)  $\overline{r} = 3\overline{q}, -\frac{3(\overline{p}, \overline{q})}{(\overline{p}, \overline{q})} \overline{p}$  (2)  $\overline{r} = -\overline{q} + \left(\frac{\overline{p}, \overline{q}}{\overline{q}, \overline{q}}\right) \overline{p}$ 

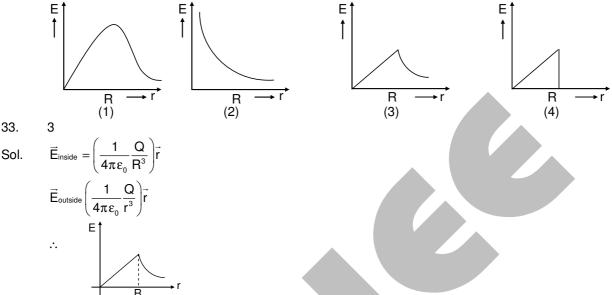
(1) 
$$\vec{r} = \vec{q} - \left(\vec{p} \cdot \vec{p}\right)\vec{p}$$
  
(2)  $\vec{r} = \vec{q} - \left(\vec{p} \cdot \vec{q}\right)\vec{p}$   
(3)  $\vec{r} = \vec{q} - \left(\frac{\vec{p} \cdot \vec{q}}{\vec{p} \cdot \vec{p}}\right)\vec{p}$   
(4)  $\vec{r} = -3\vec{q} + \frac{3(\vec{p} \cdot \vec{q})}{(\vec{p} \cdot \vec{p})}\vec{p}$ 

30. 2

 $\overrightarrow{AE}$  = vector component of  $\vec{q}$  on  $\vec{p}$ Sol.  $\overrightarrow{\mathsf{AE}} = \frac{\left(\overrightarrow{p} \cdot \overrightarrow{q}\right)}{\left(\overrightarrow{p} \cdot \overrightarrow{q}\right)} \overrightarrow{p} \qquad \therefore \text{ From } \Delta \mathsf{ABE}; \ \overrightarrow{\mathsf{AB}} + \overrightarrow{\mathsf{BE}} = \overrightarrow{\mathsf{AE}}$ p  $\Rightarrow \vec{q} + \vec{r} = \frac{(\vec{p} \cdot \vec{q})\vec{p}}{(\vec{p} \cdot \vec{q})} \qquad \Rightarrow \vec{r} = -\vec{q} + \frac{(\vec{p} \cdot \vec{q})}{(\vec{p} \cdot \vec{q})}\vec{p}$ ā **PART B: PHYSICS** 31. A wooden wheel of radius R is made of two semicircular parts (see figure): The two parts are held together by a ring made of a metal strip of cross sectional area S and length L. L is slightly less than  $2\pi R$ . To fit the ring on the wheel, it is heated so that its temperature rises by  $\Delta T$  and it just steps over the wheel. As it cools down to surrounding temperature, it presses the semicircular parts together. If the coefficient of linear expansion of the metal is  $\alpha$ , and its Youngs' modulus is Y, the force that one part of the wheel applies on the other part is : (1)  $2\pi SY \alpha \Delta T$ (2) SY  $\alpha \Delta T$ (3)  $\pi SY \alpha \Delta T$ (4)  $2SY \alpha \Delta T$ 31. 4 Sol. If temperature increases by  $\Delta T$ , Increase in length L,  $\Delta L = L\alpha \Delta T$  $\frac{\Delta L}{L} = \alpha \Delta T$ 1F Let tension developed in the ring is T.  $\frac{T}{S} = Y \frac{\Delta L}{L} = Y \alpha \Delta T$ ÷.  $T = SY \alpha \Delta T$ • From FBD of one part of the wheel, F = 2TWhere, F is the force that one part of the wheel applies on the other part.  $\therefore$  F = 2SY  $\alpha \Delta T$ The figure shows an experimental plot for discharging of a 32. Potential difference capacitor in an R-C circuit. The time constant  $\tau$  of this circuit 25 V in volts lies between: 20 (1) 150 sec and 200 sec (2) 0 and 50 sec (3) 50 sec and 100 sec (4) 100 sec and 150 sec 0 50 100 150 200 Time t in seconds 32. 4 For discharging of an RC circuit, Sol.  $V = V_0 e^{-t/\tau}$  $V = \frac{V_0}{2}$ So, when  $\frac{V_0}{2} = V_0 e^{-t/\tau}$  $\ln \frac{1}{2} = -\frac{t}{\tau} \Rightarrow \tau = \frac{t}{\ln 2}$ 

From graph when 
$$V = \frac{V_0}{2}$$
, t = 100 s  $\therefore \tau = \frac{100}{\ln 2} = 144.3$  sec

33. In a uniformly charged sphere of total charge Q and radius R, the electric field E is plotted as a function of distance from the centre. The graph which would correspond to the above will be



34. An electromagnetic wave in vacuum has the electric and magnetic fields  $\vec{E}$  and  $\vec{B}$ , which are always perpendicular to each other. The direction of polarization is given by  $\vec{X}$  and that of wave propagation by  $\vec{k}$ . Then :

(1)  $\vec{X} \parallel \vec{B}$  and  $\vec{k} \parallel \vec{B} \times \vec{E}$  (2)  $\vec{X} \parallel \vec{E}$  and  $\vec{k} \parallel \vec{E} \times \vec{B}$  (3)  $\vec{X} \parallel \vec{B}$  and  $\vec{k} \parallel \vec{E} \times \vec{B}$  (4)  $\vec{X} \parallel \vec{E}$  and  $\vec{k} \parallel \vec{B} \times \vec{E}$ 

34.

3

- Sol. Direction of polarization is parallel to magnetic field,

and direction of wave propagation is parallel to  $\vec{E}{\times}\vec{B}$ 

∴ **K** || **E**×**B** 

35. If a simple pendulum has significant amplitude (up to a factor of 1/e of original) only in the period between t = Os to  $t = \tau s$ , then  $\tau$  may be called the average life of the pendulum. When the spherical bob of the pendulum suffers a retardation (due to viscous drag) proportional to its velocity, with 'b' as the constant of proportionality, the average life time of the pendulum is (assuming damping is small) in seconds:

(1) 
$$\frac{0.693}{b}$$
 (2) b (3)  $\frac{1}{b}$  (4)  $\frac{2}{b}$   
35. 4  
35. 4  
Sol. As retardation = bv  
 $\therefore$  retarding force = mbv  
 $\therefore$  net restoring torque when angular displacement is  $\theta$  is given by  
 $= - \operatorname{mg} \ell \sin \theta + \operatorname{mbv} \ell$   
 $\therefore$   $|\alpha = - \operatorname{mg} \ell \sin \theta + \operatorname{mbv} \ell$   
where,  $I = \operatorname{m} \ell^2$   
 $\therefore \qquad \frac{d^2\theta}{dt^2} = \alpha = -\frac{g}{\ell} \sin \theta + \frac{bv}{\ell}$   
for small damping, the solution of the above differential equation will be

÷.

$$\therefore \qquad \theta = \theta_0 e^{-\frac{bt}{2}} \sin(wt + \phi)$$

–b

angular amplitude will be =  $\theta \cdot e^{-2}$ 

According to question, in  $\tau$  time (average life-time),

angular amplitude drops to  $\frac{1}{2}$  value of its original value ( $\theta$ )

- $\therefore \qquad \frac{\theta_0}{e} = \theta_0 e^{\frac{-6\tau}{2}}$  $\frac{6\tau}{2} = 1$  $\therefore \qquad \tau = \frac{2}{b}$
- 36. Hydrogen atom is excited from ground state to another state with principal quantum number equal to 4. Then the number of spectral lines in the emission spectra will be (1) 2 (2) 3 (3) 5 (4) 6
- 36.

4

Sol. Number of spectral lines from a state n to ground state is

$$=\frac{n(n-1)}{2}=6$$

- 37. A coil is suspended in a uniform magnetic field, with the plane of the coil parallel to the magnetic lines of force. When a current is passed through the coil it starts oscillating; it is very difficult to stop. But if an aluminium plate is placed near to the coil, it stops. This is due to :
  (1) development of eigenverse when the place is placed.
  - (1) development of air current when the plate is placed.
  - (2) induction of electrical charge on the plate
  - (3) shielding of magnetic lines of force as aluminium is a paramagnetic material.
  - (4) electromagnetic induction in the aluminium plate giving rise to electromagnetic damping.
- 37.

4

- Sol. Oscillating coil produces time variable magnetic field. It cause eddy current in the aluminium plate which causes anti-torque on the coil, due to which is stops.
- 38. The mass of a spaceship is 1000 kg. It is to be launched from the earth's surface out into free space. The value of 'g' and 'R' (radius of earth) are 10 m/s<sup>2</sup> and 6400km respectively. The required energy for this work will be ;

(1) 
$$6.4 \times 10^{11}$$
 Joules (2)  $6.4 \times 10^{8}$  Joules (3)  $6.4 \times 10^{9}$  Joules (4)  $6.4 \times 10^{10}$  Joules

- 38.
- Sol. To launch the spaceship out into free space, from energy conservation,

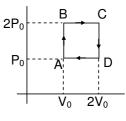
$$\frac{-GMm}{R} + E = 0$$

$$E = \frac{GMm}{R} = \left(\frac{GM}{R^2}\right)mR = mgR$$

$$= 6.4 \times 10^{10} \text{ J}$$

39. Helium gas goes through a cycle ABCDA (consisting of *two* isochoric and two isobaric lines) as shown in figure. Efficiency of this cycle is nearly: (Assume the gas to be close to ideal gas)

(1) 15.4%	(2) 9.1%
(3) 10.5%	(4) 12.5%



39.

1

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Sol. Work done in complete cycle = Area under P–V graph =  $P_0V_0$ from A to B, heat given to the gas

= 
$$nC_v\Delta T = n\frac{3}{2}R\Delta T = \frac{3}{2}V_0\Delta P = \frac{3}{2}P_0V_0$$
  
from B to C, heat given to the system

 $= nC_{p}\Delta T = n\left(\frac{5}{2}R\right)\Delta T$ 

$$=\frac{5}{2}(2P_0)\Delta V=5P_0V_0$$

from C to D and D to A, heat is rejected.

efficiency, 
$$\eta = \frac{\text{work done by gas}}{\text{heat given to the gas}} \times 100$$
  
 $\eta = \frac{P_0 V_0}{\frac{3}{2} P_0 V_0 + 5 P_0 V_0} = 15.4\%$ 

40. In Young's double slit experiment, one of the slit is wider than other, so that the amplitude of the light from one slit is double of that from other slit. If I<sub>m</sub> be the maximum intensity, the resultant intensity I when they interfere at phase difference φ is given by

(2)  $\frac{I_m}{3} \left( 1 + 2\cos^2 \frac{\phi}{2} \right)$ 

(3)  $\frac{I_{m}}{5} \left( 1 + 4\cos^{2}\frac{\phi}{2} \right)$  (4)  $\frac{I_{m}}{9} \left( 1 + 8\cos^{2}\frac{\phi}{2} \right)$ 

41.

Sol.

40. 4 Sol. Let  $A_1 = A_0, A_2 = 2A_0$ If amplitude of resultant wave is A then  $A^2 = A_1^2 + A_2^2 + 2A_1A_2 \cos \phi$ 

For maximum intensity,

 $\frac{I_m}{q}(4+5\cos\phi)$ 

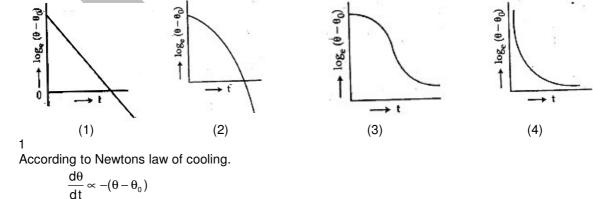
$$A_{max}^{2} = A_{1}^{2} + A_{2}^{2} + 2A_{1}A_{2}$$

$$\therefore \qquad \frac{A^{2}}{A_{max}^{2}} = \frac{A_{1}^{2} + A_{2}^{2} + 2A_{1}A_{2}\cos\phi}{A_{1}^{2} + A_{2}^{2} + 2A_{1}A_{2}}$$

$$= \frac{A_{0}^{2} + 4A_{0}^{2} + 2(A_{0})(2A_{0})\cos\phi}{A_{0}^{2} + 4A_{0}^{2} + 2(A_{0})(2A_{0})}$$

$$\frac{I}{I_{m}} = \frac{5 + 4\cos\phi}{9} = \frac{1 + 8\cos^{2}(\phi/2)}{9}$$

41. A liquid in a beaker has temperature  $\theta(t)$  at time t and  $\theta_0$  is temperature of surroundings, then according to Newton's law of cooling the correct graph between  $\log_e (\theta - \theta_0)$  and t is

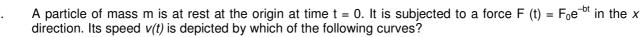


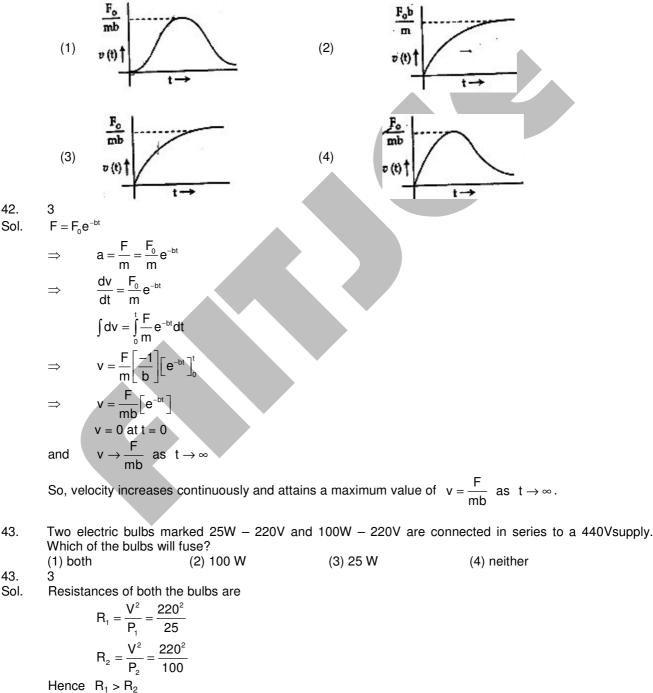
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$$\Rightarrow \qquad \frac{d\theta}{dt} = -k(\theta - \theta_0)$$
$$\int \frac{d\theta}{\theta - \theta_0} = \int -k \, dt$$
$$\Rightarrow \qquad \ln(\theta - \theta_0) = -kt + t$$

 $\Rightarrow \qquad ln(\theta - \theta_0) = -kt + c$ Hence the plot of  $ln(\theta - \theta_0)$  vs t should be a straight line with negative slope.

42.





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When connected in series, the voltages divide in them in the ratio of their resistances. The voltage of 440 V devides in such a way that voltage across 25 w bulb will be more than 220 V. Hence 25 w bulb will fuse.

44. Resistance of a given wire is obtained by measuring the current flowing in it and the voltage difference applied across it. If the percentage errors in the measurement of the current and the voltage difference are 3% each, then error in the value of resistance of the wire is (1) 6% (3) 1% (4) 3% (2) zero

44.

Sol.

=

ŀ

$$R = \frac{V}{i}$$

$$\Rightarrow \qquad \left|\frac{\Delta R}{R}\right| = \left|\frac{\Delta V}{V}\right| + \left|\frac{\Delta i}{i}\right|$$

$$= \frac{\Delta V}{V} \times 100 = 3$$

$$\Rightarrow \qquad \frac{\Delta V}{V} = 0.03$$
Similarly,  $\frac{\Delta i}{i} = 0.03$ 
Hence  $\frac{\Delta R}{R} = 0.06$ 

So percentage error is  $\frac{\Delta n}{R} \times 100 = 6\%$ 

A boy can throw a stone up to a maximum height of 10 m. The maximum horizontal distance that the boy 45. can throw the same stone up to will be (1)  $20\sqrt{2}$  m (3)  $10\sqrt{2}$  m (2) 10 m (4) 20 m

45.

maximum vertical height =  $\frac{u^2}{2g}$  = 10 m Sol.

> u<sup>2</sup> sin 20 Horizontal range of a projectile =

Range is maximum when  $\theta = 45^{\circ}$ 

Maximum horizontal range =

Hence maximum horizontal distance = 20 m.

- 46. This question has statement 1 and statement 2. Of the four choices given after the statements, choose the one that best describes the two statements
  - Statement 1 : Davisson germer experiment established the wave nature of electrons.

Statement 2 : If electrons have wave nature, they can interfere and show diffraction.

- (1) Statement 1 is false, Statement 2 is true
- (2) Statement 1 is true, Statement 2 is false
- (3) Statement 1 is true, Statement 2 is the correct explanation for statement 1
- (4) Statement 1 is true, Statement 2 is true, Statement 2 is not the correct explanation for statement 1. 3

46.

Sol. Davisson - Germer experiment showed that electron beams can undergo diffraction when passed through atomic crystals. This shows the wave nature of electrons as waves can exhibit interference and diffraction.

48.

Sol.

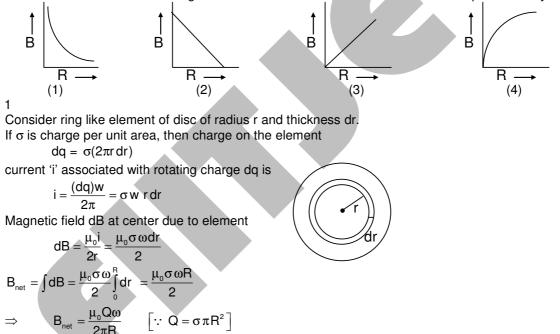
47. A thin liquid film formed between a U-shaped wire and a light slider supports a weight of 1.5 x10<sup>-2</sup>N (see figure). The length of the slider is 30 cm and its weight negligible. The surface tension of the liquid film is

(1) 0.0125 Nm<sup>-1</sup>
(2) 0.1 Nm<sup>-1</sup>
(3) 0.05 Nm<sup>-1</sup>
(4) 0.025 Nm<sup>-1</sup>



# 47. 4 Sol. The force of surface tension acting on the slider balances the force due to the weight. $\Rightarrow F = 2T \ell = w$ $\Rightarrow 2T(0.3) = 1.5 \times 10^{-2}$ $\Rightarrow T = 2.5 \times 10^{-2} \text{ N/m}$

48. A charge Q is uniformly distributed over the surface of non conducting disc of radius R. The disc rotates about an axis perpendicular to its plane and passing through its centre with an angular velocity ω. As a result of this rotation a magnetic field of induction B is obtained at the centre of the disc. If we keep both the amount of charge placed on the disc and its angular velocity to be constant and vary the radius of the disc then the variation of the magnetic induction at the centre of the disc will be represented by the figure

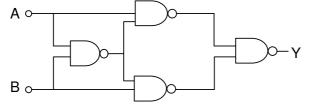


So if Q and w are unchanged then

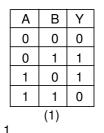
$$B_{net} \propto \frac{1}{B}$$

Hence variation of  $B_{net}$  with R should be a rectangular hyperbola as represented in (1).

49. Truth table for system of four NAND gates as shown in figure is



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Α	В	Υ	
0	0	0	
0	1	0	
1	0	1	
1	1	1	
(2)			

		_
Α	В	
0	0	
0	1	
1	0	
1	1	
	(3)	

0

0

Α	В	Υ	
0	0	1	
0	1	0	
1	0	0	
1	1	1	
(4)			

49. Sol.

51.

Sol.

Α	В	у	<b>y</b> 1	<b>y</b> <sub>2</sub>	у
0	0	1	1	1	0
0	1	1	1	0	1
1	0	1	0	1	1
1	1	0	1	1	0

50. A radar has a power of 1 Kw and is operating at a frequency of 10 GHz. It is located on a mountain top of height 500 m. The maximum distance upto which it can detect object located on the surface of the earth (Radius of earth =  $6.4 \times 10^6$  m) is

	(1) 80	km	(2) 16 km	(3) 40 km	(4) 64 km
50.	1				
Sol.		um distance on ed is d, then $(h+R)^2 = d^2 +$		object can be	
	$\Rightarrow$	$d^2 = h^2 + 2Rh$		F	7
	since	$h \ll R, \Rightarrow$	$d^2 = 2hR$		
	$\Rightarrow$	$d = \sqrt{2(500)(6)}$	$4 \times 10^{6}) = 80 \text{ k}$	xm (\n	

51. Assume that a neutron breaks into a proton and an electron. The energy released during this process is (Mass of neutron =  $1.6725 \times 10^{-27}$  kg; mass of proton =  $1.6725 \times 10^{-27}$  kg; mass of electron =  $9 \times 10^{-31}$  kg)

(1) 0.73 MeV (2) 7.10 MeV (3) 6.30 MeV (4) 5.4 MeV 1  $\Delta m = (m_p + m_e) - m_n$   $= 9 \times 10^{-31} \text{ kg.}$ Energy released =  $(9 \times 10^{-31} \text{ kg})c^2$  joules

 $=\frac{9\times10^{-31}\times(3\times10^8)^2}{1.6\times10^{-13}}$  MeV = 0.73 MeV.

52. A Carnot engine, whose efficiency is 40%, takes in heat from a source maintained at a temperature of 500 K It is desired to have an engine of efficiency 60%. Then, the intake temperature for the same exhaust (sink) temperature must be
(1) efficiency of Carnot engine cannot be made larger than 50%

(1) endency of Carnot engine carnot be made larger than 50%  
(2) 1200 K (3) 750 K (4) 600 K  
52. 3  
Sol. 
$$\frac{40}{100} = \frac{500 - T_S}{500}$$
,  $T_S = 300$  K  
 $\frac{600}{100} = \frac{T - 300}{T} \Rightarrow T = 750$  K

53. This question has statement 1 and statement 2. Of the four choices given after the statements, choose the one that best describes the two statements.

53.

54.

54.

55.

55.

56.

56.

57.

57.

If two springs  $S_1$  and  $S_2$  of force constants  $k_1$  and  $k_2$ , respectively, are stretched by the same force, it is found that more work is done on spring  $S_1$  than on spring  $S_2$ . Statement 1 : If stretched by the same amount, work done on  $S_1$ , will be more than that on  $S_2$ Statement 2 :  $k_1 < k_2$ (1) Statement 1 is false, Statement 2 is true (2) Statement 1 is true, Statement 2 is false (3) Statement 1 is true, Statement 2 is the correct explanation for statement 1 (4) Statement 1 is true, Statement 2 is true, Statement 2 is not the correct explanation for statement 1. Sol.  $F = K_1S_1 = K_2S_2$  $W_1 = FS_1, W_2 = FS_2$  $K_1S_1^2 > K_2S_2^2$  $S_1 > S_2$  $K_1 < K_2$  $W \propto K$  $W_1 < W_2$ Two cars of masses  $m_1$  and  $m_2$  are moving in circles of radii  $r_1$  and  $r_2$ , respectively. Their speeds are such that they make complete circles in the same time t. The ratio of their centripetal acceleration is (1)  $m_1r_1 : m_2r_2$  $(2) m_1 : m_2$ (3)  $r_1$  :  $r_2$ (4) 1 : 1 3 Sol. a∝r A cylindrical tube, open at both ends, has a fundamental frequency, f, in air. The tube is dipped vertically in water so that half of it is in water. The fundamental frequency of the air-column is now (2) <sup>'</sup>/<sub>2</sub> (1) f (4) 2f 1  $f_0 = \frac{v}{2\ell}$ Sol.  $f_{\rm C} = \frac{v}{2\ell}$ An object 2.4 m in front of a lens forms a sharp image on a film 12 cm behind the lens. A glass plate 1cm thick, of refractive index 1.50 is interposed between lens and film with its plane faces parallel to film. At what distance (from lens) should object be shifted to be in sharp focus on film? (1) 7.2 m (2) 2.4 m (3) 3.2 m (4) 5.6 m 4 Sol. Case I: u = -240cm, v = 12, by Lens formula  $\frac{1}{f} = \frac{7}{80}$ Case II: v =  $12 - \frac{1}{3} = \frac{35}{3}$  (normal shift =  $1 - \frac{2}{3} = \frac{1}{3}$ )  $f = \frac{7}{80}$ u = 5.6 A diatomic molecule is made of two masses  $m_1$  and  $m_2$  which are separated by a distance r. If we calculate its rotational energy by applying Bohr's rule of angular momentum guantization, its energy will be given by (n is an integer) (2)  $\frac{n^2 h^2}{2(m_1 + m_2)r^2}$  (3)  $\frac{2n^2 h^2}{(m_1 + m_2)r^2}$  (4)  $\frac{(m_1 + m_2)n^2h^2}{2m_1 m_2 r^2}$ (1)  $\frac{(m_1 + m_2)^2 n^2 h^2}{2m_1^2 m_2^2 r^2}$ 4

Sol. 
$$r_1 = \frac{m_2 r}{m_1 + m_2}$$
;  $r_2 = \frac{m_1 r}{m_1 + m_2}$   
 $(l_1 + l_2)\omega = \frac{nh}{2\pi} = n\hbar$   
 $K.E = \frac{1}{2}(l_1 + l_2)\omega^2 = \frac{n^2\hbar^2(m_1 + m_2)}{2m_1m_2r^2}$ 

58. A spectrometer gives the following reading when used to measure the angle of a prism. Main scale reading: 58.5 degree Vernier scale reading : 09 divisions Given that 1 division on main scale corresponds to 0.5 degree. Total divisions on the vernier scale is 30 and match with 29 divisions of the main scale. The angle of the prism from the above data (1) 58.59° (2) 58.77° (3) 58.65°  $(4) 59^{\circ}$ 

Sol. L.C = 
$$\frac{1}{60}$$

3

Total Reading =  $585 + \frac{9}{60} = 58.65$ 

59. This question has statement 1 and statement 2. Of the four choices given after the statements, choose the one that best describes the two statements.

An insulating solid sphere of radius R has a uniformly positive charge density p. As a result of this uniform charge distribution there is a finite value of electric potential at the centre of the sphere, at the surface of the sphere and also at a point out side the sphere. The electric potential at infinity is zero.

Statement 1 : When a charge q is taken from the centre to the surface of the sphere, its potential energy changes by  $\frac{qp}{c}$ 

3ε,

**Statement 2**: The electric field at a distance r(r < R) from the centre of the sphere is  $\frac{\rho r}{3\epsilon_0}$ .

- (1) Statement 1 is true, Statement 2 is true, Statement 2 is not the correct explanation for statement 1.
- (2) Statement 1 is true, Statement 2 is false
- (3) Statement 1 is false, Statement 2 is true
- (4) Statement 1 is true, Statement 2 is the correct explanation for statement 1
- 59.

 $\oint \vec{\mathsf{E}} \cdot \vec{\mathsf{d}} \mathsf{A} = \frac{1}{\varepsilon_0}$ Sol.

3ε<sub>0</sub>

Statement 2 is correct

$$\Delta \mathsf{PE} = (\mathsf{V}_{\mathsf{sur}} - \mathsf{V}_{\mathsf{cent}})\mathsf{q} = -\frac{\mathsf{q}}{6\varepsilon_0}\rho\mathsf{R}^2$$

Statement 1 is incorrect

60. Proton, Deuteron and alpha particle of the same kinetic energy are moving in circular trajectories in a constant magnetic field. The radii of proton, deuteron and alpha particle are respectively  $r_p$ ,  $r_d$  and  $r_{\alpha}$ . Which one of the following relations is correct?

(1) 
$$r_{\alpha} = r_{p} = r_{d}$$
 (2)  $r_{\alpha} = r_{p} < r_{d}$  (3)  $r_{\alpha} > r_{d} > r_{p}$  (4)  $r_{\alpha} = r_{d} > r_{p}$   
60. 2  
Sol.  $r = \frac{\sqrt{2mK}}{Bq}$ 

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$$r \propto \frac{\sqrt{m}}{q}$$
  
 $r_{\alpha} = r_{p} < r_{d}$ 

## **PART C: CHEMISTRY**

61.	Which among the following will be named as dibromidobis(ethylene diamine)chromium(III) bromide ?					
	(1) $\left[ Cr(en)_3 \right] Br_3$ (2) $\left[ Cr(en)_2 Br_2 \right] Br$	(3) [Cr(en)Br <sub>4</sub> ]	(4) \[Cr(en)Br_2]Br			
61.	2					
Sol.	$\left[ Cr(en)_{2}Br_{2} \right] Br$ – dibromido bis (ethylene diam	nine)chromium(III) bromi	de			
62.	Which method of purification is represented by t	he following equation :				
	$Ti(s) + 2l_2(g) \xrightarrow{523K} Til_4(g) \xrightarrow{1700K} Ti(s) + 2$					
	(1) zone refining (2) cupellation	(3) Poling	(4) Van Arkel			
62.	4					
Sol.	Van Arkel method $T(x) = 21 (x) = \frac{523K}{2} T(x) (x)$					
	$Ti(s) + 2I_{2}(g) \xrightarrow{523K} TiI_{4}(g)$					
	$\operatorname{Til}_{4}(g) \xrightarrow{1700 \text{ K}} \operatorname{Ti}(s) + 2\operatorname{I}_{2}(g)$					
60	Lithium forma hady control cubic structure. The	length of the side of its	unit coll in QE1 pm. Atomic radius			
63.	Lithium forms body centred cubic structure. The of the lithium will be :	length of the side of its t	unit cell is 351 pm. Atomic radius			
	(1) 75 pm (2) 300 pm	(3) 240 pm	(4) 152 pm			
63.	4					
Sol.	For BCC, $\sqrt{3}a = 4r$					
	$r = \frac{\sqrt{3} \times 351}{4} = 152pm$					
	4					
64.	The molecule having smallest bond angle is :					
64.	(1) NCl <sub>3</sub> (2) AsCl <sub>3</sub> 3	(3) SbCl <sub>3</sub>	(4) PCI <sub>3</sub>			
Sol.	As the size of central atom increases lone pair bond pair repulsions increases so, bond angle					
	decreases					
65.	Which of the following compounds can be detect	ted by Molisch's test ?				
00.	(1) Nitro compounds (2) Sugars	(3) Amines	(4) Primary alcohols			
65.	2					
Sol.	Molisch's Test : when a drop or two of alcoholic solution of $\alpha$ -naphthol is added to sugar solution and then conc. H <sub>2</sub> SO <sub>4</sub> is added along the sides of test tube, formation of violet ring takes place at the junction					
	of two liquids.		et mig takes place at the janetion			
00	The income to come size a second the fall of its is					
66.	The incorrect expression among the following is		V			
	(1) $\frac{\Delta G_{\text{system}}}{\Delta S_{\text{total}}} = -T$	(2) In isothermal process $w_{\text{reversible}} = -nRT ln \frac{V_f}{V_f}$				
			v			
	(3) $InK = \frac{\Delta H^0 - T\Delta S^0}{BT}$	(4) $K = e^{-\Delta G^0 / RT}$				
66.	3					
Sol.	$\Delta G^{\circ} = -RTIn K and \Delta G^{0} = \Delta H^{0} - T\Delta S^{0}$					

67. The density of a solution prepared by dissolving 120 g of urea (mol. Mass = 60 u ) in 1000g of water is 1.15 g/mL. The molarity of this solution is : (1) 0.50 M (2) 1.78 M (3) 1.02 M (4) 2.05 M 67. Δ Total weight of solution = 1000 + 120 = 1120 g Sol.  $Molarity = \frac{120}{60} \times \frac{1000}{1120/1.15} = 2.05M$ The species which can best serve as an initiator for the cationic polymerization is : 68. (1)  $LiAlH_4$ (2) HNO<sub>3</sub> (3) AICl<sub>3</sub> (4) BuLi 68. 3 Sol. lewis acids can initiate the cationic polymerization. Which of the following on thermal decomposition yields a basic as well as an acidic oxide ? 69. (1) NaNO<sub>3</sub> (2) KCIO<sub>3</sub> (3) CaCO<sub>3</sub>  $(4) NH_4NO_3$ 69. 3  $CaCO_3 \rightarrow CaO_4 + CO_2$ Basic Acidic Sol. The standard reduction potentials for  $Zn^{2+}/Zn$ ,  $Ni^{2+}/Ni$ , and  $Fe^{2+}/Fe$  are -0.76, -0.23 and -0.44 V respectively. The reaction  $X + Y^{2+} \rightarrow X^{2+} + Y$  will be spontaneous when : (1) X = Ni, Y = Fe (2) X = Ni, Y = Zn (3) X = Fe, Y = Zn (4) X = Zn, Y = Ni70. 70.  $\begin{array}{l} Zn + Fe^{+2} \rightarrow Zn^{+2} + Fe \\ Fe + Ni^{+2} \rightarrow Fe^{2+} + Ni \end{array}$ Sol.  $Zn + Ni^{2+} \rightarrow Zn^{+2} + Ni$ All these are spontaneous 71. According to Freundlich adsorption isotherm, which of the following is correct ? (2)  $\frac{x}{m} \propto p^1$ (1)  $\frac{x}{m} \propto P^0$ (3)  $\frac{x}{m} \propto p^{1/n}$ (4) All the above are correct for different ranges of pressure 71.  $\frac{x}{m} \propto P^0$  is true at extremely high pressures Sol.  $\frac{x}{m} \propto p^1$ ;  $\frac{x}{m} \propto p^{1/n}$  are true at low and moderate pressures The equilibrium constant (K<sub>c</sub>) for the reaction  $N_2(g) + O_2(g) \rightarrow 2NO(g)$  at temperature T is 4 x 10<sup>-4</sup>. The 72. value of K<sub>C</sub> for the reaction, NO(g)  $\rightarrow \frac{1}{2} N_2(g) + \frac{1}{2} O_2(g)$  at the same temperature is : (1) 0.02 (2) 2.5 x 10<sup>2</sup> (3) 4 x 10<sup>-4</sup> (4) 50.0 (1) 0.02 72.  $N_2 + O_2 \longrightarrow 2NO$   $K_c = 4 \times 10^{-4}$ Sol. NO  $\xrightarrow{1}{2}$  N<sub>2</sub> +  $\frac{1}{2}$ O<sub>2</sub> K<sup>1</sup><sub>C</sub> =  $\sqrt{\frac{1}{K_{c}}}$  $K_{C}^{1} = \frac{1}{\sqrt{4 \times 10^{-4}}} = 50$ 73. The compressibility factor for a real gas at high pressure is : (1) 1 + RT/pb (3) 1 + pb/RT(4) 1-pb/RT (2) 1 73. 3

At high pressure  $Z = 1 + \frac{Pb}{BT}$ Sol.

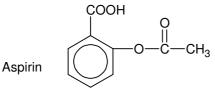
74. Which one of the following statements is correct ? (1) All amino acids except lysine are optically active (2) All amino acids are optically active (3) All amino acids except glycine are optically active (4) All amino acids except glutamic acid are optically active 74 3

Sol.

Glycine  $\longrightarrow$  CH<sub>2</sub>  $H_2$ COOH

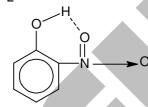
75. Aspirin is known as : (1) Acetyl salicylic acid (3) Acetyl salicylate 1

75.



(2) Phenyl salicylate (4) Methyl salicylic acid

- Acetyl salicylic acid Sol.
- 76. Ortho-Nitrophenol is less soluble in water than p- and m- Nitrophenols because : (1) o-Nitrophenol is more volatile in steam than those of m - and p-isomers
  - (2) o-Nitrophenol shows Intramolecular H-bonding
  - (3) o-Nitrophenol shows Intermolecular H-bonding
  - (4) Melting point of o-Nitrophenol is lower than those of m-and p-isomers. 2
- 76.



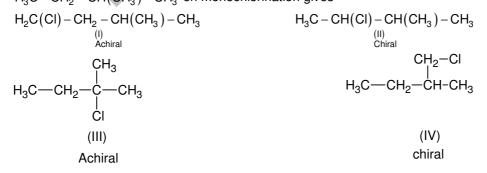
Sol.

Intramolecular H-bonding decreases water solubility.

- 77. How many chiral compounds are possible on monochlorination of 2-methyl butane ? (2) 2 (3) 4 (4) 6 (1) 8
- 77.

2

Sol.  $H_3C - CH_2 - CH(CH_3) - CH_3$  on monochlorination gives



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78.
 Very pure hydrogen (99.9%) can be made by which of the following processes ?

 (1) Reaction of methane with steam
 (2) Mixing nature Hydrogen to another the hydrogen of high molecular weight

 (3) Electrolysis of water
 (4) Reaction of sall like hydrides with water

 78.
 3

 21.
 Highly pure hydrogen is obtained by the electrolysis of water.

 79.
 The electrons identified by quantum numbers n and 1:

 (a) n = 4, 1 = 1
 (b) n = 4, 1 = 0

 (2) (c) < (d) < (b) < (a) (2) (2) (c) (c) < (a) (a) (b) < (d) < (a) < (c) (d) (a) (c) < (b) < (d)

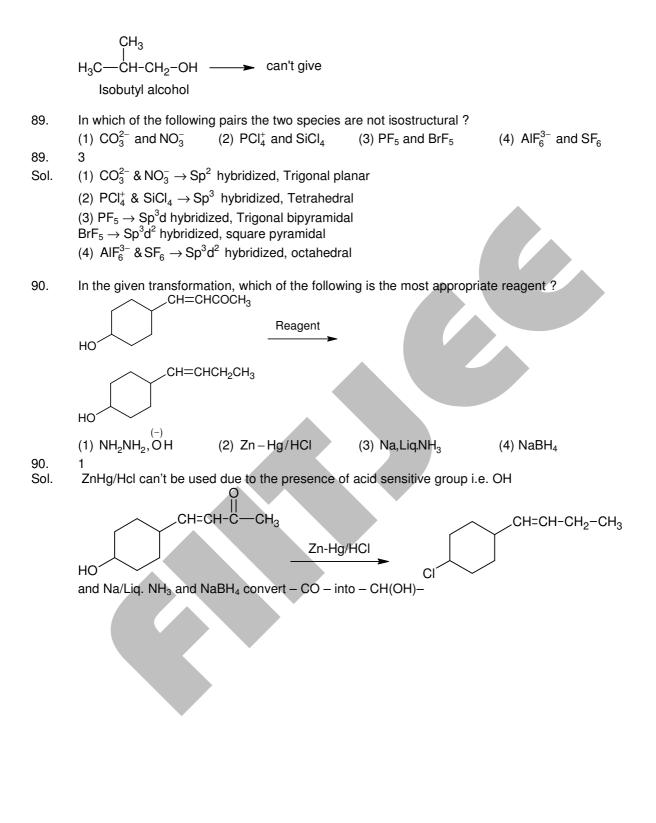
 79.
 The electrons identified by quantum numbers n and 1:

 (a) n = 4, 1 = 1
 (b) n = 4, 1 = 0
 (c) n = 3, 1 = 2

 (a) (n + 1) = 4 + 1 = 5
 (b) (n + 1) = 4 + 0 = 4
 (c) (n + 1) = 3 + 2 = 5
 (d) (n + 1) = 3 + 1 = 4

 80.
 For a first order reaction, (A) 
$$\rightarrow$$
 products, the concentration of A changes from 0.1 M to 0.025 M in 40 minin (3) 3.47 × 10° Mmin (2) 3.47 × 10° Mmin (3) 3.47 × 10° Mmin (2) 3.47 × 10° Mmin (3) 3.47 × 10° Mmin (2) 3.47 × 10° Mmin (3) 3.47 × 10° Mmin (2) 3.47 × 10° Mmin (3) 3.47 × 10° Mmin (2) 3

 $K_f$  for water is 1.86K kg mol<sup>-1</sup>. If your automobile radiator holds 1.0 kg of water, how many grams of 84. ethylene glycol ( $C_2H_6O_2$ ) must you add to get the freezing point of the solution lowered to  $-2.8^{\circ}C$ ? (1) 72g (2) 93g (3) 39g (4) 27g 84. 2 Sol.  $\Delta T_f = K_f.m$  $2.8 = 1.86 \times \frac{\text{wt}}{62} \times \frac{1000}{1000}$ Wt = 93g85. What is DDT among the following : (1) Greenhouse gas (2) A fertilizer (3) Biodegradable pollutant (4) Non-biodegradable pollutant 85. 4 Sol. DDT - non-biodegradable pollutant. 86. The increasing order of the ionic radii of the given isoelectronic species is : (4) K<sup>+</sup>, S<sup>2-</sup>, Ca<sup>2+</sup>, Cl<sup>-</sup> (2) S<sup>2-</sup>, Cl<sup>-</sup>, Ca<sup>2+</sup>, K<sup>+</sup> (3) Ca<sup>2+</sup>, K<sup>+</sup>, Cl<sup>−</sup>, S<sup>2+</sup> (1) Cl<sup>−</sup>, Ca<sup>2+</sup>, K<sup>+</sup>, S<sup>2−</sup> 86. 3 For isoelectronic species, as the z/e decreases, ionic radius increases Sol. 87. 2-Hexyne gives trans-2-Hexene on treatment with : (4)  $LiAIH_4$ (1) Pt/H<sub>2</sub> (3) Pd/BaSO<sub>4</sub> (2) Li/NH<sub>3</sub> 87. 2 H₂C Li/NH<sub>3</sub>  $H_3C - CH_2 - CH_2 - C \equiv C - CH_3$ **Birch reduction** 2-Hexyne Trans-2-Hexene Sol. lodoform can be prepared from all except : 88. (1) Ethyl methyl ketone (2) Isopropyl alcohol (3) 3-Methyl - 2- butanone (4) Isobutyl alcohol 88. 4 1) methyl ketones R-CO-CH<sub>3</sub> lodoform is given by Sol. 2) alcohols of the type R-CH(OH)CH<sub>3</sub> where R can be hydrogen also H<sub>2</sub>C-٠Ĉ C<sub>2</sub>H<sub>5</sub> ethyl methyl ketone CH3 H<sub>3</sub>C---ĊH-OH can give lodoform Test Isopropyl alchol H<sub>2</sub>C-·ĊH-CH₂ 3-methyl 2-butanone



### READ THE FOLLOWING INSTRUCTIONS CAREFULLY

- 1. The candidates should fill in the required particulars on the Test Booklet and Answer Sheet (*Side-1*) with *Blue/Black Ball Point Pen.*
- 2. For writing/marking particulars on *Side-2* of the Answer Sheet, use *Blue/Black Ball Point Pen only.*
- 3. The candidates should not write their Roll Numbers anywhere else (except in the specified space) on the Test Booklet/Answer Sheet.
- 4. Out of the four options given for each question, only one option is the correct answer.
- 5. For each *incorrect response, one-fourth (1/4)* of the total marks allotted to the question would be deducted from the total score. *No deduction* from the total score, however, will be made *if no response* is indicated for an item in the Answer Sheet
- 6. Handle the Test Booklet and Answer Sheet with care, as under no circumstance (except for discrepancy in Test Booklet Code and Answer Sheet Code), will another set be provided.
- 7. The candidates are not allowed to do any rough work or writing work on the Answer Sheet. All calculations/writing work are to be done in the space provided for this purpose, in the Test Booklet itself, marked 'Space for Rough Work'. This space is given at the bottom of each page and in 3 pages (Pages 21 23) at the end of the booklet.
- 8. On completion of the test, the candidates must hand over the Answer Sheet to the Invigilator on duty in the Room/Hall. However, the candidates are allowed to take away this Test Booklet with them.
- 9. Each candidate must show on demand his/her Admit Card to the Invigilator.
- 10. No candidate, without special permission of the Superintendent or Invigilator, should leave his/her seat.
- 11. The candidates should not leave the Examination Hall without handing over their Answer Sheet to the Invigilator on duty and sign the Attendance Sheet again. Cases where a candidate has not signed the Attendance Sheet a second time will be deemed not to have handed over the Answer Sheet and dealt with as an unfair means case. The candidates are also required to put their left hand THUMB impression in the space provided in the Attendance Sheet.
- 12. Use of Electronic/Manual Calculator and any Electronic Item like mobile phone, pager etc. is prohibited.
- 13. The candidates are governed by all Rules and Regulations of the Board with regard to their conduct in the Examination Hall. All cases of unfair means will be dealt with as per Rules and Regulations of the Board.
- 14. No part of the Test Booklet and Answer Sheet shall be detached under any circumstances.
- 15. Candidates are not-allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, electronic device or any other material except the Admit Card inside the examination hall/room.

## KEY (SET – C) PART A: MATHEMATICS

1.	2	2.	3	3.	3	4.	2	
5.	1	6.	4	7.	2	8.	4	
9.	1	10.	4	11.	1	12.	1	
13.	3	14.	4	15.	1	16.	3	
17.	3	18.	4	19.	1	20.	3	
21.	2	22.	1	23.	3	24.	2 or 4	
25.	1	26.	2	27.	4	28.	2	
29.	3	30.	2					
			<b>P</b> /	ART B: PH	YSIC	2S		
31.	4	32.	4	33.	3	34.	3	
35.	4	36.	4	37.	4	38.	4	
39.	1	40.	4	41.	1	42.	3	
43.	3	44.	1	45.	4	46.	3	
47.	4	48.	1	49.	1	50.	1	
51.	1	52.	3	53.	1	54.	3	
55.	1	56.	4	57.	4	58.	3	
59.	3	60.	2					
PART C: CHEMISTRY								
					riis.			
61.	2	62.	4	63.	4	64.	3	
65.	2	66.	3	67.	4	68.	3	
69.	3	70.	4	71.	4	72.	4	
73.	3	74.	3	75.	1	76.	2	
77.	2	78.	3	79.	2	80.	2	
81.	4	82.	3	83.	2	84.	2	
85.	4	86.	3	87.	2	88.	4	
89.	3	90.	1					
		-						