General Certificate of Education June 2010

Applying Mathematics UOM4/1

Advanced Subsidiary Level

Final



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| Μ | mark is for method | | | | | | | | | |
|------------|--|-----|----------------------------|--|--|--|--|--|--|--|
| m or dM | mark is dependent on one or more M marks and is for method | | | | | | | | | |
| А | mark is dependent on M or m marks and is for accuracy | | | | | | | | | |
| В | mark is independent of M or m marks and is for method and accuracy | | | | | | | | | |
| E | mark is for explanation | | | | | | | | | |
| | | | | | | | | | | |
| or ft or F | follow through from previous | | | | | | | | | |
| | incorrect result | MC | mis-copy | | | | | | | |
| CAO | correct answer only | MR | mis-read | | | | | | | |
| CSO | correct solution only | RA | required accuracy | | | | | | | |
| AWFW | anything which falls within | FW | further work | | | | | | | |
| AWRT | anything which rounds to | ISW | ignore subsequent work | | | | | | | |
| ACF | any correct form | FIW | from incorrect work | | | | | | | |
| AG | answer given | BOD | given benefit of doubt | | | | | | | |
| SC | special case | WR | work replaced by candidate | | | | | | | |
| OE | or equivalent | FB | formulae book | | | | | | | |
| A2,1 | 2 or 1 (or 0) accuracy marks | NOS | not on scheme | | | | | | | |
| –x EE | deduct <i>x</i> marks for each error | G | graph | | | | | | | |
| NMS | no method shown | с | candidate | | | | | | | |
| PI | possibly implied | sf | significant figure(s) | | | | | | | |
| SCA | substantially correct approach | dp | decimal place(s) | | | | | | | |
| | | | | | | | | | | |

Key to mark scheme and abbreviations used in marking

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

General Certificate of Education

A/S Level - Applying Mathematics UOM 4/1

Answers and Marking Scheme – June 2010

Question 1

| (a) | $\frac{1}{2^3} = \frac{1}{8}$ | M1 | Some indication of 3 half- lives | | |
|-----|---|------|---|--|--|
| | $3 \times 3.8 = 11.4$ days | A1 | | | |
| (b) | 19/3.8 = 5 | M1 | Some indication of 5 half- lives or follow through from their (a) | | |
| | $\left(\frac{1}{2}\right)^5 = \frac{1}{32}$ | A1ft | (0.03128) or as a percentage or follow through from (a) | | |
| | TOTAL | 4 | | | |

Question 2

| $\frac{m_0}{2} = m_0 \ \mathrm{e}^{-\lambda \times 3.8}$ | | |
|--|----|--|
| $\frac{1}{2} = e^{-\lambda \times 3.8}$ | M1 | or $2 = e^{3.8\lambda}$ Correct statement without m_0 |
| $\ln \frac{1}{2} = -0.6931 = -\lambda \times 3.8 \text{ or } e^{-\lambda} = (0.5)^{\frac{1}{3.8}}$ | M1 | $\ln 2 = 3.8\lambda$ handling logs correctly |
| $\lambda = 0.182$ | A1 | must have both method marks |
| TOTAL | 3 | |

Question 3

| (a) | $\frac{1}{2} = e^{-\lambda \times 24}$ | | |
|-----|--|------|---|
| | $\ln\left(\frac{1}{2}\right) = -0.6931 = -\lambda \times 24$ | M1A1 | using ln |
| | $\lambda = 0.0289$ | A1 | |
| (b) | $p^{24} = 0.5$ | M1 | correct statement |
| | $\ln p^{24} = \ln(0.5)$ | M1 | alternatively $p = {}^{24} \sqrt{\frac{1}{2}}$ M2 Or 2 nd alternative $(p =)e - {}^{0.02891 \times 1}$ (M1) + M2 M2 dependent on M1 |
| | $24 \ln p = \ln 0.5$ | M1 | |
| | $\ln p = -0.2888$ | | |
| | p = 0.972 | A1 | condone 0.971 |
| | TOTAL | 7 | |

Question 4

| Shorter | B 1 | |
|--|------------|-----------------------|
| Must refer to quantifiable factor eg may show half-life 1.39 days or refer to how much substance after a certain length of time or " λ is greater" or sketch graph. | B1 | dependant on first B1 |
| TOTAL | 2 | |

Question 5

| $m_0 = 1$ | M1 | evidence of use of recurrence relation |
|---------------|----|--|
| $m_1 = 0.833$ | | |
| $m_2 = 0.694$ | A1 | accurately (at least once) |
| $m_3 = 0.578$ | | |
| $m_4 = 0.482$ | | |
| $m_5 = 0.401$ | A1 | SC2 0.482 |
| TOTAL | 3 | |

Question 6

| $p^n = 0.6^n = \frac{1}{2}$ | | |
|--|------|---|
| $\ln(0.6)^n = \ln\left(\frac{1}{2}\right)$ | M1 | using logs correctly with P1 = $\frac{1}{2}$ |
| $n \ln (0.6) = \ln \left(\frac{1}{2}\right)$ | M1 | correct law of logs |
| $n = \frac{\ln\left(\frac{1}{2}\right)}{\ln 0.6} = 1.357 = 1.36$ | A1 | |
| $1.357 \text{ days} = 24 \times 1.357 = 32.56 \text{ hours}$ | M1 | $(n \times 24)$ |
| 33 hours | A1ft | From their <i>n</i> |
| (1 day 8.56 hours = 1 day 9 hours) | | |
| TOTAL | 5 | |

Question 7

| (a) | See table on next page | | |
|-----|--|----|---|
| (b) | The probability would suggest $N = 12$ | B1 | Quantifying Alternatively 7 atoms out of 20 suggests $P = 0.35$ |
| | The value in the simulation is lower because more of the random numbers are 0,1,2,3, than might be expected (but that's randomness!) | B1 | must mention randomness/predictability or sample size |
| | TOTAL | 6 | |
| | TOTAL MARK FOR PAPER | 30 | |

1, 2, 3 =atom decaying

4, 5, 6, 7, 8, 9 = atom not decaying

| atom | t=0 | t= | =1 | t= | =2 | t= | =3 | t= | =4 | t= | =5 | t= | =6 |
|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| | status | random | status | randon | status | random | status | random | status | random | status | random | status |
| | | no | |
| Α | 1 | 2 | 0 | | | | | | | | | | |
| В | 1 | 5 | 1 | 1 | 0 | | | | | | | | |
| С | 1 | 2 | 0 | | | | | | | | | | |
| D | 1 | 0 | 0 | | | | | | | | | | |
| Е | 1 | 3 | 0 | | | | | | | | | | |
| F | 1 | 9 | 1 | 9 | 1 | 3 | 0 | | | | | | |
| G | 1 | 3 | 0 | | | | | | | | | | |
| Н | 1 | 4 | 1 | 1 | 0 | | | | | | | | |
| Ι | 1 | 1 | 0 | | | | | | | | | | |
| J | 1 | 5 | 1 | 7 | 1 | 8 | 1 | 9 | 1 | 1 | 0 | | |
| Κ | 1 | 0 | 0 | | | | | | | | | | |
| L | 1 | 3 | 0 | | | | | | | | | | |
| Μ | 1 | 3 | 0 | | | | | | | | | | |
| Ν | 1 | 2 | 0 | | | | | | | | | | |
| 0 | 1 | 3 | 0 | | | | | | | | | | |
| Р | 1 | 9 | 1 | 2 | 0 | | | | | | | | |
| Q | 1 | 3 | 0 | | | | | | | | | | |
| R | 1 | 0 | 0 | | | | | | | | | | |
| S | 1 | 9 | 1 | 8 | 1 | 2 | 0 | | | | | | |
| Т | 1 | 4 | 1 | 4 | 1 | 4 | 1 | 3 | 0 | | | | |
| | | | | | | | | | | | | | |
| total | 20 | | 7 | | 4 | | 2 | | 1 | | 0 | | |

for t = 3, B1 for correct random nos.

for t = 4, B1ft for status of their random nos and renewing atoms.

for t = 5, B1ft for status of their random nos. and renewing atoms

B1ft for correct total row (their columns added correctly).

4 marks in total only