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## GCE A level

# PHYSICS <br> ASSESSMENT UNIT PH5: <br> Electromagnetism, Nuclei \& Options 

A.M. THURSDAY, 20 June 2013
$13 / 4$ hours

## ADDITIONAL MATERIALS

In addition to this paper, you will require a calculator, a Case Study Booklet and a Data Booklet.

## INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use pencil or gel pen. Do not use correction fluid. Write your name, centre number and candidate number in the spaces at the top of this page.
Write your answers in the spaces provided in this booklet. If you run out of space, use the continuation pages at the back of the booklet, taking care to number the question(s) correctly.

## INFORMATION FOR CANDIDATES

This paper is in 3 sections, $\mathbf{A}, \mathbf{B}$, and $\mathbf{C}$.
Section A: 60 marks. Answer all questions. You are advised to spend about 1 hour on this section.
Section B: 20 marks. The Case Study. Answer all questions. You are advised to spend about 20 minutes on this section.
Section C: Options; 20 marks. Answer one option only. You are advised to spend about 20 minutes on this section.

## SECTION A

1. A student is uncertain whether or not a radioactive source emits $\alpha, \beta$ or $\gamma$ radiation or a combination of these radiations.
(a) Describe how the student would use a detector and counter along with suitable absorbers to find which radiation(s) are emitted by the radioactive source.

(b) A radioactive isotope has a starting activity of $76.0 \times 10^{15} \mathrm{~Bq}$ and a half life of 25.6 days.
(i) Calculate the activity after 51.2 days.
(ii) Calculate the activity after 1 year.

## (iii) Calculate the number of radioactive nuclei present at the start.

2. The following fusion reaction can occur inside stars with core temperatures of around 100 million kelvin.

(a) Calculate the energy released in the above reaction from the following data.

Mass of ${ }_{2}^{4} \mathrm{He}=4.0026 \mathrm{u}$
Mass of ${ }_{6}^{12} \mathrm{C}=12.0000 \mathrm{u}$
$1 \mathrm{u}=931 \mathrm{MeV}$
$\qquad$
$\qquad$
$\qquad$
(b) The isotope ${ }_{28}^{62} \mathrm{Ni}$ has a binding energy per nucleon of $8.795 \mathrm{MeV} /$ nucleon and this is the highest known binding energy per nucleon.
Calculate the mass of a ${ }_{28}^{62} \mathrm{Ni}$ nucleus in unified atomic mass units $(\mathrm{u})$ and give your answer to 5 significant figures.

$$
\text { mass of proton }=1.00728 \mathrm{u}, \quad \text { mass of neutron }=1.00866 \mathrm{u}, \quad 1 \mathrm{u}=931 \mathrm{MeV}
$$

3. (a) A 131 nF capacitor is charged using a potential difference of 1.62 V . Calculate the charge stored by the capacitor.
(b) This 131 nF capacitor is then disconnected from the power supply and a large resistor connected across its terminals. As the capacitor discharges, the pd across it decreases from 1.62 V to 0.47 V in 220 ms . Calculate the resistance of the resistor.
(c) The plates of this 131 nF capacitor are square and are separated by 0.15 mm . Calculate the length of a side of the capacitor plate.
(d) In practice, how could the capacitance of this capacitor be increased by a factor of 100 ?
4. The diagram below is an example of a particle accelerator called a synchrotron. In this synchrotron, protons are accelerated and their path is kept circular by a magnetic field which has to increase as the speed of the protons increases. The protons themselves are accelerated by the alternating potential difference applied to the quarter circle plates (see + and - in the diagram).

(a) Derive the equation $r=\frac{m v}{B e}$ for a particle of mass $m$ and charge $e$ moving with velocity $v$ at right angles to a uniform magnetic field, $B$.
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(b) Use the equation $r=\frac{m v}{B e}$ to explain why the magnetic field must be increased as the speed of the protons increases.
(c) Protons take $1.78 \mu \mathrm{~s}$ to complete a circuit of a synchrotron of radius 8.50 m . Calculate the strength of the magnetic field, $B$, required. $\left[m_{\text {proton }}=1.67 \times 10^{-27} \mathrm{~kg}\right.$.]
(d) (i) Modern synchrotrons use magnetic fields up to 10 T which cannot be produced using copper wires at room temperature. Explain why not, using $B=\mu_{0} n I$. [2]
(ii) Hence, explain why superconducting magnets are used to produce large magnetic fields in synchrotrons.
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5. (a) State the two laws of electromagnetic induction (Faraday's law and Lenz's law).
(b) A thick conducting bar is moved with constant speed over non-parallel conducting rails as shown below. The rails have negligible resistance and the $B$-field is uniform.

(i) Indicate the direction of the induced current on the diagram and explain how you arrived at your answer.
(ii) The conductor moves at a constant speed of $31 \mathrm{~m} \mathrm{~s}^{-1}$. Use Faraday's law to explain why the induced emf increases.
(iii) The conductor starts moving from the end near the $43 \Omega$ resistor. Calculate the (iii) The conductor starts moving from the end near the $43 \Omega$ resistor. Calculate the length of the track.
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6. Electrons flow through a silicon wafer which is used as a Hall probe.

(a) Show on the above diagram:
(i) the face of the silicon wafer that becomes positively charged;
(ii) how you would connect a voltmeter to measure the Hall voltage.
(b) Calculate the drift velocity of the electrons given that the Hall voltage is 0.314 mV .
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$\qquad$
(c) As electrons move through the wafer, explain why no work is done on them by the electric field, $E_{\mathrm{H}}$.
(d) The current flowing in the silicon wafer is 0.38 A . Calculate the number of free electrons per unit volume in the silicon wafer.

## SECTION B

The questions refer to the case study.
Direct quotes from the original passage will not be awarded marks.
7. (a) In your own words and referring to diagram 2 in the case study, explain lift in terms of Newton's laws. (See paragraph 3.)
(b) The streamline diagram shows streamlines getting further apart. Explain why there must be a net force to the left acting on the air in the streamline.
(See paragraphs 6 \& 7.)

(c) An aeroplane is initially flying forward at a constant speed horizontally. It then tilts as shown. The magnitude of the lift force remains constant. Explain why the aeroplane must now accelerate downwards and to the left.

(d) Houses can explode when tornados pass nearby. Explain this using Bernoulli's equation. (See paragraphs 7, $8 \& 9$.)
(e) Check that the figure for lift $(130 \mathrm{kN})$ for a super jumbo wing at $80 \mathrm{~m} \mathrm{~s}^{-1}$ is correct if you assume that the speed over the top of the wing is only $2 \%$ greater than $80 \mathrm{~m} \mathrm{~s}^{-1}$. (See paragraph 13.)

## (f) Show that the lift coefficient has no units. (See paragraph 17.)

(g) Calculate the lift coefficient for an Airbus super jumbo at take-off. (See paragraph 17.)
(h) Draw a labelled diagram of the set up that might be employed using a hair dryer, stand, clamp, protractor, digital balance and metal plate to measure lift coefficient against angle of attack. (See paragraphs 18 and 19.)

| SECTION C: OPTIONAL TOPICS |  |
| :--- | ---: |
| Option A: Further Electromagnetism and Alternating Currents | $\square$ |
| Option B: Revolutions in Physics - The Newtonian Revolution | $\square$ |
| Option C: Materials | $\square$ |
| Option D: Biological Measurement and Medical Imaging | $\square$ |
| Option E: Energy Matters | $\square$ |

Answer the question on one topic only.
Place a tick $(\checkmark)$ in one of the boxes above, to show which topic you are answering.
You are advised to spend about $\mathbf{2 0}$ minutes on this section.

## Option A: Further Electromagnetism and Alternating Currents

8. (a) Explain how an alternating current in the primary coil leads to an alternating emf in the secondary coil.

(c) (i) Calculate the reactances of the capacitor and inductor at the frequency shown.[3]

(ii) How can you tell that this is the resonance frequency of the circuit?
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$\qquad$
(iii) Calculate the current at the resonance frequency of 3817 Hz .
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(iv) Calculate the current when the frequency is 38.17 kHz (the rms pd remains 14.4 V ).
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(d) (i) Explain why the circuit shown is a high pass filter.

(ii) $C=470 \mathrm{nF}$ and $R=2.2 \mathrm{k} \Omega$. Using a phasor diagram or otherwise, calculate the frequency when $V_{\text {out }}=\frac{1}{\sqrt{2}} V_{\text {in }}$. [Hint: $\left.\cos 45^{\circ}=\frac{1}{\sqrt{2}}.\right]$

## Option B: Revolutions in Physics - The Newtonian Revolution

9. (a) (i) The diagram shows a simplified version of Ptolemy's scheme to account for the observed motion of Jupiter.

(I) Label on the diagram the following: equant, deferent, epicycle.
(II) Explain whether Jupiter's observed motion is prograde or retrograde when it is in the position shown.
(III) Ptolemy's scheme predicts the motions of planets. What other changing feature of planets' appearances does the scheme predict?
(ii) The diagrams show two successive oppositions of Jupiter and the Sun, as seen on a simplified Copernican scheme. Opposition (2) occurs time $\Delta t$ after opposition (1).

Opposition (1)


Opposition (2)


It can be shown that $\frac{2 \pi}{T_{\mathrm{E}}} \Delta t-\frac{2 \pi}{T_{\mathrm{J}}} \Delta t=2 \pi$, or equivalently, $\frac{\Delta t}{T_{\mathrm{E}}}-\frac{\Delta t}{T_{\mathrm{J}}}=1$, in which $T_{\mathrm{E}}$ and $T_{\mathrm{J}}$ are the periodic times of the Earth and Jupiter.
(I) Explain how the equation (either version) arises.
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(II) The time $\Delta t$, observed between successive oppositions is found to be 1.092 years. Calculate Jupiter's period of revolution in years.
(b) The diagram shows a model illustrating an early idea of Kepler, involving the five regular solids.

(i) Explain Kepler's idea, and why, eventually, he rejected it.
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(ii) "By trying to make use of the regular solid, Kepler was following an ancient tradition." Discuss this statement briefly.
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(c) The diagram is taken from Newton's Principia (Proposition I, Theorem I).

(i) Explain what the path ABCDEF represents, and why there are sharp changes of direction at each of the points A, B, C, D, E and F.
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$\qquad$
(ii) What does Newton show, in Theorem I?
(d) The Moon's mean orbital radius is $3.84 \times 10^{8} \mathrm{~m}$, and its period of revolution is 27.3 days. The Earth's mean radius is $6.37 \times 10^{6} \mathrm{~m}$.
(i) Calculate the ratio: $\frac{\text { orbital acceleration of the Moon }}{\text { acceleration due to gravity on Earth's surface }}$
(ii) Show clearly that this supports an inverse square law of gravitation.
(iii) What assumption are you making about the Earth's mass distribution?

## Option C: Materials

10. (a) The diagram shows apparatus that may be used to obtain a value for the Young modulus of a metal in the form of a long wire. A known load, $F$, is applied to one end of the wire. The extension, $\Delta x$, of the wire is measured using the pointer and metre ruler.

(i) To obtain a value for the Young modulus, two other measurements must be made. State what these measurements are and what equipment you would use.
(ii) A graph of load, $F$, against extension, $\Delta x$, may be obtained from the experiment.


Explain how a value of the Young modulus may be obtained by using the measurements in part (a)(i) and information from the graph.
(ii) The strain energy, $W$, in the wire due to the stretching force $F$, is given by $\frac{1}{2} F \Delta x$, where $\Delta x$ represents the total extension in the wire combination. Show that

$$
\begin{equation*}
W=\frac{F^{2} l_{0}}{2 A}\left(\frac{1}{E_{\text {brass }}}+\frac{1}{E_{\text {iron }}}\right) \tag{2}
\end{equation*}
$$

(iii) Calculate $W$ when $F=47.0 \mathrm{~N}$. Assume the diameter of both wires is 1.0 mm and each has an unstretched length, $l_{0}$, of $2.0 \mathrm{~m} .\left[E_{\text {brass }}=100 \mathrm{GPa} ; E_{\text {iron }}=200 \mathrm{GPa}.\right]$
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Examiner
(iv) Hence, or otherwise, determine the overall extension of the combination of wires when $F=47.0 \mathrm{~N}$.
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(v) Explain, using the Young moduli given, which of the two wires has undergone the greater extension and hence determine the ratio $\frac{\Delta x_{\text {brass }}}{\Delta x_{\text {iron }}}$.
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(c) Use the information in the table below:
(i) to complete the table to determine whether the polymers given are examples of thermosetting or thermoplastic polymers;

| Name | Tensile <br> strength/MPa | Maximum <br> strain/\% | Young <br> modulus/GPa | Thermosetting or <br> thermoplastic? |
| :---: | :---: | :---: | :---: | :---: |
| Melamine <br> formaldehyde | 65 | 0.6 | 12 |  |
| Low density <br> polyethylene | 17 | 500 | 0.3 |  |

(ii) to explain which of the polymers given might be brittle and which of the two is the stiffer.
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## Option D: Biological Measurement and Medical Imaging

11. (a) An X-ray machine emits X-rays of minimum wavelength 0.030 nm .
(i) Sketch a graph of intensity against wavelength for the resulting X-ray spectrum. Label the main features of the spectrum.

Intensity

(ii) Calculate the accelerating potential difference used to produce a spectrum with a minimum wavelength of 0.030 nm .
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(iii) When diagnosing and treating a child's broken arm, images of the arm are needed. What two properties of X-rays make them suitable for this imaging?
(iv) X-ray imaging is not suitable for revealing brain tumours. Which imaging technique should be used? Give reasons for your choice.
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(b) The fraction, $f$, of ultrasound reflected back at a boundary between two materials of acoustic impedances $Z_{1}$ and $Z_{2}$ is given by the equation:

$$
f=\frac{\left(Z_{2}-Z_{1}\right)^{2}}{\left(Z_{2}+Z_{1}\right)^{2}}
$$

(i) Define acoustic impedance, $Z$.
(ii) Using the information given in the table below determine the fraction of ultrasound reflected at an air / skin boundary.

| Medium | Density <br> $/ \mathrm{kg} \mathrm{m}^{-3}$ | Velocity of ultrasound <br> $/ \mathrm{m} \mathrm{s}^{-1}$ |
| :---: | :---: | :---: |
| Air | 1.300 | 340 |
| Skin | 1075 | 1590 |

(iii) | Explain the importance of your answer to (b) (ii) and state what ultrasound |
| :--- |
| radiographers must do to obtain clear images of the body. |
| [2] |

(c) (i) Explain the difference between radiation exposure and absorbed dose.
(ii)
(xxplain why, for the same absorbed dose, the dose equivalent would be different
[3] radiographers must do to obtain clear images of the body.
(c) (i) Explain the difference between radiation exposure and absorbed dose.

## Option E: Energy Matters

12. A new nuclear reactor has been proposed based on the reaction of lithium-7 and a proton to produce two $\alpha$-particles.

$$
{ }_{1}^{1} \mathrm{p}+{ }_{3}^{7} \mathrm{Li} \rightarrow{ }_{4}^{8} \mathrm{Be} \rightarrow{ }_{2}^{4} \mathrm{He}+{ }_{2}^{4} \mathrm{He}+17.1 \mathrm{MeV}
$$

Although this is not a new nuclear reaction (it was the original splitting the atom experiment in 1932), there have been some theoretical developments that suggest this might be a useful reaction.

The above reaction is produced by ionising hydrogen and accelerating the resulting protons in a vacuum to an energy of around 300 keV . Unfortunately, in the past, only one in 30 million protons accelerated to the correct voltage have produced this nuclear reaction.
(a) (i) The above reaction is produced by accelerating ionised hydrogen with 300 kV . Explain two possible benefits of the system compared with fission reactors.
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(ii) Calculate the energy required to accelerate 30 million protons to an energy of 300 keV and explain why the above reaction does not seem profitable.
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$\qquad$
(iii) There is around $10^{16} \mathrm{~kg}$ of ${ }_{3}^{7} \mathrm{Li}$ in the world's oceans and the mass of ${ }_{3}^{7} \mathrm{Li}$ can be taken as 7 u . Calculate the number of ${ }_{3}^{7} \mathrm{Li}$ atoms in the world's oceans.
(iv) The total annual world energy consumption is around $5 \times 10^{20} \mathrm{~J}$. Assuming that each ${ }_{3}^{7} \mathrm{Li}$ atom can, ideally, provide an energy of 17.1 MeV , calculate the number of years ${ }_{3}^{7} \mathrm{Li}$ could supply the world's energy consumption.
(b) (i) It has been suggested that lithium wafers of dimension $20 \mathrm{~mm} \times 20 \mathrm{~mm} \times 2.5 \mathrm{~mm}$ be used as a target for the proton bombardment, leading to the temperature difference shown. Calculate the heat transferred through the lithium wafer from the data shown.

(ii) The heat transferred through the lithium wafer is used to raise the temperature of a flowing gas. By sending this gas quickly through a compressor, its temperature can be raised dramatically. Explain why the temperature of the gas increases using the first law of thermodynamics.
(iii) Eventually, water will be boiled to produce superheated steam to drive turbines and generators. Explain why superheated steam at $500^{\circ} \mathrm{C}$ leads to greater efficiencies than steam at $100^{\circ} \mathrm{C}$.

| Question number | Additional page, if required. <br> Write the question numbers in the left-hand margin. |
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Examiner only


## GCE A level

## 1325/01-B

## PHYSICS

ASSESSMENT UNIT PH5
A.M. THURSDAY, 20 June 2013

## CASE STUDY FOR USE WITH SECTION B

## Examination copy

To be given out at the start of the examination. The pre-release copy must not be used.

From Newton, through Bernoulli to Super Jumbos - an explanation of lift
Let's define some forces first. Air flowing past a body exerts forces on it. Lift is the force that is perpendicular to the flow direction and drag is the force parallel to the flow direction. Other forces that act are weight and thrust. The thrust on an aeroplane is provided by the propellers or jets but this force is absent for gliders.

Lift is commonly associated with wings but lift is also generated by propellers, kites, helicopter rotors, rudders, sails on sailboats, hydrofoils, wings on racing cars, wind turbines and other objects. While the common meaning of the word "lift" assumes that lift opposes gravity, lift in its technical sense can be in any direction since it is defined with respect to the direction of flow rather than the direction of gravity. When an aircraft is


Diagram 1: Forces on an aerofoil flying straight and level, the lift opposes the weight. However, when an aircraft is climbing, descending, or banking in a turn, for example, the lift is tilted with respect to the vertical. Lift may also be entirely downwards in some aerobatic manoeuvres, or on the spoiler of a racing car. Lift may also be horizontal, for instance on the sail on a sailing boat.

## Newton's laws: lift and the deflection of the flow

Flow of air around an aerofoil in a wind tunnel. Note the curved streamlines above and below the foil, and the overall downward deflection of the air. One way to understand the generation of lift is to observe that the air is deflected as it passes the aerofoil. Since the foil must exert a force on the air to change its direction, the air must exert a force of equal magnitude but opposite direction on the foil. In the case of an aeroplane wing, the wing exerts a downward force on the air and the air exerts an upward force on the wing. This explanation relies on the second and third of Newton's laws of motion: The net force on an object is equal to its rate of momentum


Diagram 2: Vector diagram of flow past an aerofoil

## Pressure differences

Lift may also be described in terms of air pressure. Wherever there is a net force there is also a pressure difference, thus deflection of the flow indicates the presence of a net force and a pressure difference. This pressure difference implies the average pressure on the upper surface of the wing is lower than the average pressure on the underside.

## Bernoulli's Equation

In much the same way as the laws of electricity can be derived from conservation of charge and 5 energy, the theories of aerodynamics can be derived from conservation of mass and energy. Let's consider conservation of mass first but we also have to make a couple of assumptions:

1. The density of the air is a constant (it turns out that this is a very good approximation as long as speeds remain below about 250 mph ).
2. We consider a steady flow so that the air is moving along in steady streamlines.

Now let's consider streamlines that are getting closer together in this narrowing tube of starting 6 cross-sectional area $A_{1}$ and finishing cross-sectional area $A_{2}$.


Diagram 3: Air flow in a streamline

The streamlines follow the path of the air so that (by definition) no air crosses the streamlines. The volume of air entering the tube in time $\Delta t$ is

$$
A_{1} \Delta x_{1}=A_{1} v_{1} \Delta t
$$

and the volume of air leaving the tube in time $\Delta t$ is

$$
A_{2} \Delta x_{2}=A_{2} v_{2} \Delta t
$$

Because the density is a constant, mass is proportional to volume and conservation of mass now means conservation of volume. So:

$$
A_{1} v_{1} \Delta t=A_{2} v_{2} \Delta t \quad \text { or } \quad A_{1} v_{1}=A_{2} v_{2}
$$

As the area decreases from left to right then the velocity must increase due to conservation of mass.

You can go even further than this, if the velocity is increasing from left to right then we have an acceleration and there must be a net force. The only thing that can supply this net force is a greater pressure on the left side of the tube than on the right. This would suggest that the pressure must be higher on the left side where the speed of the air is lower. Bernoulli's equation can be derived using this concept and the result is this:

$$
p=p_{0}-\frac{1}{2} \rho v^{2}
$$

where $p$ is the pressure, $p_{0}$ is the pressure of air that isn't moving, $\rho$ is the density of air and $v$ is the speed of the air. Basically, Bernoulli's equation says that the pressure of air that is moving is decreased by an amount $\frac{1}{2} \rho v^{2}$.

There are many things that can be explained using Bernoulli's equation but here's a little explanation of one of the most annoying aerodynamic effects of all. Consider a person taking a shower with a light shower curtain. Which way does the shower curtain move?

To use Bernoulli's equation you need some idea of the speed of the air. Outside the shower, the air should be stationary (unless you live in a draughty house) but inside the shower, the water droplets are causing the air to move slightly. According to Bernoulli's equation, the pressure inside the shower will be lower so that the net force on the shower curtain is inward. There you are - an explanation of why that irritating cold and wet shower curtain always creeps spookily inwards towards you.

## Explaining lift using Bernoulli



Diagram 4: Flow past an aerofoil showing time intervals
The diagram to the left represents the same flow past a wing as the previous vector diagram (diagram 2). The horizontal gaps between the dots in the diagram represent equal intervals of time. Note that the spaces between the dark dots are much bigger at the upper surface than at the lower surface. This means that the speed of the flow is far greater over the top of the wing than over the bottom. Hence, applying Bernoulli's equation explains why the above wing experiences lift.

Diagram 4 is great for explaining lift using Bernoulli's equation but it also debunks the old explanation of lift which went like this:

- when the air splits to go above and below the wing, the air passing above the wing takes exactly the same time to reach the back of the wing as the air passing underneath,
- the top side of the wing is designed to be longer than the bottom,
- so air travels quicker over the top of the wing,
- Bernoulli explains why the pressure below is bigger than above and hence lift.

One look at diagram 4 should dismiss the first point of the old argument. Also, if the old explanation was complete:

1. how can an aeroplane fly when the top of the wing is only $2 \%$ longer than the bottom?
2. how can an aeroplane fly upside down?

To get an idea of the first point, an Airbus super jumbo takes off at a speed of $80 \mathrm{~m} \mathrm{~s}^{-1}$ in air of density $1.2 \mathrm{~kg} \mathrm{~m}^{-3}$. Its wings are made in Broughton, North Wales and have an enormous area of around $850 \mathrm{~m}^{2}$. If you assume that the speed over the top of the wing is $2 \%$ larger, this gives a total lift force of 130 kN . This may sound impressive until you realise that the mass of an empty super jumbo is around 300 tonnes. The truth is that although the top side of the wing is only $2 \%$ longer than the bottom, the increase in speed can be more than $50 \%$ over the top side of the wing.

The second point is answered by considering the angle of attack $(\theta)$ of the wing because this is also 14 important in deflecting the airflow.

## Lift due to an angle of attack



The aerofoil shown to the left is symmetrical - the top and bottom of the aerofoil are the same (the wings of aerobatic planes are designed to be like this so that they 15 fly equally well upside down). In order to produce lift, the wings have to be tilted to produce the same flow as in diagrams $2 \& 4$.
$\theta$ (angle of attack)

## Diagram 5

An aeroplane flying upside down can still have an angle of attack and produce lift.


## Lift coefficient

The lift force provided by a wing can be calculated as a function of speed with the following 17 equation:

$$
L=\frac{1}{2} \rho v^{2} A C_{L}
$$

where

- $L$ is lift force,
- $\quad \rho$ is air density,
- $\quad v$ is air speed,
- $A$ is the area of the wing, and
- $C_{L}$ is the lift coefficient of the wing (dependent on the angle of attack).

This theory works very well and a standard experiment is to measure the lift coefficient as a function of angle of attack. In practice, real wings would be tested in extremely expensive wind tunnels but you could set up a cheap version of the experiment in a school lab using a thin metal 18 plate as a makeshift aerofoil. You'd also need a hair dryer, stand, clamp, protractor and a digital balance.

You won't be able to get such good data with a makeshift set-up because of the accuracy of your protractor and it's unlikely that a cheap hairdryer will produce a particularly uniform airflow. However, you should be able to measure the lift very accurately using the digital scales and the general trend of the graph shown should be measurable.

## Conclusions

There are many aspects of the physics of lift and flight that are accessible to you as A-level physics students. It's surprising how far you can get just with Newton's laws of motion but applying these laws to obtain Bernoulli's equation leads to a far greater understanding of lift and fluid dynamics in general. You should now be able to explain how an aeroplane can fly upside down and even perform a rough experiment to show that your explanation is valid. You can even tell your friends what the likely pressure difference is between the top and bottom surface of an Airbus super jumbo wing.

Lift coefficient


