RECOGNISING ACHIEVEMENT

## ADVANCED SUBSIDIARY GCE

Additional materials: Answer Booklet (8 pages)
MEI Examination Formulae and Tables (MF2)

## INSTRUCTIONS TO CANDIDATES

- Write your name in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Read each question carefully and make sure you know what you have to do before starting your answer.
- Answer all the questions.
- You are not permitted to use a calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.


## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [ ] at the end of each question or part question.
- The total number of marks for this paper is 72 .
- You are advised that an answer may receive no marks unless you show sufficient detail of the working to indicate that a correct method is being used.


##  <br> WARNING <br> You are not allowed to use a calculator in this paper.

## Section A (36 marks)

1 Solve the inequality $3 x-1>5-x$.

2 (i) Find the points of intersection of the line $2 x+3 y=12$ with the axes.
(ii) Find also the gradient of this line.

3 (i) Solve the equation $2 x^{2}+3 x=0$.
(ii) Find the set of values of $k$ for which the equation $2 x^{2}+3 x-k=0$ has no real roots.

4 Given that $n$ is a positive integer, write down whether the following statements are always true (T), always false (F) or could be either true or false (E).
(i) $2 n+1$ is an odd integer
(ii) $3 n+1$ is an even integer
(iii) $n$ is odd $\Rightarrow n^{2}$ is odd
(iv) $n^{2}$ is odd $\Rightarrow n^{3}$ is even

5 Make $x$ the subject of the equation $y=\frac{x+3}{x-2}$.

6 (i) Find the value of $\left(\frac{1}{25}\right)^{-\frac{1}{2}}$.
(ii) Simplify $\frac{\left(2 x^{2} y^{3} z\right)^{5}}{4 y^{2} z}$.

7 (i) Express $\frac{1}{5+\sqrt{3}}$ in the form $\frac{a+b \sqrt{3}}{c}$, where $a, b$ and $c$ are integers.
(ii) Expand and simplify $(3-2 \sqrt{7})^{2}$.

8 Find the coefficient of $x^{3}$ in the binomial expansion of $(5-2 x)^{5}$.

9 Solve the equation $y^{2}-7 y+12=0$.
Hence solve the equation $x^{4}-7 x^{2}+12=0$.

## Section B (36 marks)

10 (i) Express $x^{2}-6 x+2$ in the form $(x-a)^{2}-b$.
(ii) State the coordinates of the turning point on the graph of $y=x^{2}-6 x+2$.
(iii) Sketch the graph of $y=x^{2}-6 x+2$. You need not state the coordinates of the points where the graph intersects the $x$-axis.
(iv) Solve the simultaneous equations $y=x^{2}-6 x+2$ and $y=2 x-14$. Hence show that the line $y=2 x-14$ is a tangent to the curve $y=x^{2}-6 x+2$.

11 You are given that $\mathrm{f}(x)=2 x^{3}+7 x^{2}-7 x-12$.
(i) Verify that $x=-4$ is a root of $\mathrm{f}(x)=0$.
(ii) Hence express $\mathrm{f}(x)$ in fully factorised form.
(iii) Sketch the graph of $y=\mathrm{f}(x)$.
(iv) Show that $\mathrm{f}(x-4)=2 x^{3}-17 x^{2}+33 x$.

12 (i) Find the equation of the line passing through $\mathrm{A}(-1,1)$ and $\mathrm{B}(3,9)$.
(ii) Show that the equation of the perpendicular bisector of AB is $2 y+x=11$.
(iii) A circle has centre $(5,3)$, so that its equation is $(x-5)^{2}+(y-3)^{2}=k$. Given that the circle passes through A, show that $k=40$. Show that the circle also passes through B.
(iv) Find the $x$-coordinates of the points where this circle crosses the $x$-axis. Give your answers in surd form.

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## 4751 (C1) Introduction to Advanced Mathematics

## Section A

| 1 | $x>6 / 4$ o.e. isw | 2 | M1 for $4 x>6$ or for $6 / 4$ o.e. found or for their final ans ft their $4 x>k$ or $k x>6$ | 2 |
| :---: | :---: | :---: | :---: | :---: |
| 2 | (i) $(0,4)$ and $(6,0)$ <br> (ii) $-4 / 6$ o.e. or ft their (i) isw | $\begin{aligned} & 2 \\ & 2 \end{aligned}$ | 1 each; allow $x=0, y=4$ etc; condone $x=6, y=4$ isw but 0 for $(6,4)$ with no working <br> 1 for $-\frac{4}{6} x$ or $4 /-6$ or $4 / 6$ o.e. or ft (accept 0.67 or better) 0 for just rearranging to $y=-\frac{2}{3} x+4$ | 4 |
| 3 | (i) 0 or $-3 / 2$ o.e. <br> (ii) $k<-9 / 8$ o.e. www | $2$ $3$ | 1 each <br> M2 for $3^{2}(-)(-8 k)<0$ o.e. or $-9 / 8$ found or M1 for attempted use of $b^{2}-4 a c$ (may be in quadratic formula); SC: allow M1 for $9-8 k<0$ and M1 ft for $k>9 / 8$ | 5 |
| 4 | (i) T <br> (ii) E <br> (iii) T <br> (iv) F | 3 | 3 for all correct, 2 for 3 correct. 1 for 2 correct | 3 |
| 5 | $y(x-2)=(x+3)$ <br> $x y-2 y=x+3$ or ft [ft from earlier errors if of comparable difficulty - no ft if there are no $x y$ terms] $x y-x=2 y+3 \text { or } \mathrm{ft}$ $[x=] \frac{2 y+3}{y-1} \text { o.e. or ft }$ <br> alt method: $\begin{aligned} y & =1+\frac{5}{x-2} \\ y-1 & =\frac{5}{x-2} \\ x-2 & =\frac{5}{y-1} \\ x & =2+\frac{5}{y-1} \end{aligned}$ | M1 <br> M1 <br> M1 <br> M1 <br> M1 <br> M1 <br> M1 <br> M1 | for multiplying by $x-2$; condone missing brackets <br> for expanding bracket and being at stage ready to collect $x$ terms <br> for collecting $x$ and 'other' terms on opposite sides of eqn <br> for factorising and division <br> for either method: award 4 marks only if fully correct | 4 |


| 6 | (i) 5 www <br> (ii) $8 x^{10} y^{13} z^{4}$ or $2^{3} x^{10} y^{13} z^{4}$ | $2$ <br> 3 | allow 2 for $\pm 5$; M1 for $25^{1 / 2}$ seen or for $1 / 5$ seen or for using $25^{1 / 2}=5$ with another error (ie M1 for coping correctly with fraction and negative index or with square root) <br> mark final answer; B2 for 3 elements correct, B1 for 2 elements correct; condone multn signs included, but -1 from total earned if addn signs | 5 |
| :---: | :---: | :---: | :---: | :---: |
| 7 | (i) $\frac{5-\sqrt{3}}{22}$ or $\frac{5+(-1) \sqrt{3}}{22}$ or $\frac{5-1 \sqrt{3}}{22}$ <br> (ii) $37-12 \sqrt{ } 7$ isw www | 2 3 | or $a=5, b=-1, c=22$; M1 for attempt to multiply numerator and denominator by $5-\sqrt{3}$ <br> 2 for 37 and 1 for $-12 \sqrt{ } 7$ or M1 for 3 correct terms from $9-6 \sqrt{ } 7-6 \sqrt{ } 7+28$ or $9-3 \sqrt{ } 28-3 \sqrt{ } 28+28$ or $9-\sqrt{ } 252-$ $\sqrt{ } 252+28$ o.e. eg using $2 \sqrt{ } 63$ or M2 for $9-12 \sqrt{ } 7+28$ or $9-6 \sqrt{ } 28+$ 28 or $9-2 \sqrt{ } 252+28$ or $9-\sqrt{ } 1008+$ 28 o.e.; 3 for $37-\sqrt{ } 1008$ but not other equivs | 5 |
| 8 | -2000 www | 4 | M3 for $10 \times 5^{2} \times(-2[x])^{3}$ o.e. or M2 for two of these elements or M1 for 10 or $(5 \times 4 \times 3) /(3 \times 2 \times 1)$ o.e. used $\left[{ }^{5} \mathrm{C}_{3}\right.$ is not sufficient] or for 15101051 seen; <br> or B3 for 2000; <br> condone $x^{3}$ in ans; <br> equivs: M3 for e.g $5^{5} \times 10 \times\left(-\frac{2}{5}[x]\right)^{3}$ <br> o.e. [ $\left[5^{5}\right.$ may be outside a bracket for whole expansion of all terms], M2 for two of these elements etc similarly for factor of 2 taken out at start | 4 |
| 9 | $\begin{aligned} & (y-3)(y-4)[=0] \\ & y=3 \text { or } 4 \text { cao } \\ & x= \pm \sqrt{3} \text { or } \pm 2 \text { cao } \end{aligned}$ | M1 <br> A1 <br> B2 | for factors giving two terms correct or attempt at quadratic formula or completing square or B2 (both roots needed) <br> B1 for 2 roots correct or ft their $y$ (condone $\sqrt{ } 3$ and $\sqrt{ } 4$ for B1) | 4 |

## Section B





