

# FREE-STANDING MATHEMATICS QUALIFICATION Advanced Level ADDITIONAL MATHEMATICS

6993/01

## **THURSDAY 14 JUNE 2007**

Additional materials: Answer booklet (16 pages) Graph paper Afternoon Time: 2 hours

#### INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer **all** the questions.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given correct to three significant figures where appropriate.

#### **INFORMATION FOR CANDIDATES**

- The number of marks is given in brackets [] at the end of each question or part question.
- The total number of marks for this paper is 100.

#### ADVICE TO CANDIDATES

- Read each question carefully and make sure you know what you have to do before starting your answer.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.

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#### Section A

[3]

- 1 Solve the inequality 3(x+2) > 2 x.
- 2 A particle moves in a straight line. Its velocity,  $v \text{ m s}^{-1}$ , *t* seconds after passing a point O is given by the equation

$$v = 6 + 3t^2$$
.

Find the distance travelled between the times t = 1 and t = 3. [4]

3 A circle has equation  $x^2 + y^2 - 4x - 6y + 3 = 0$ .

Find the coordinates of the centre and the radius of the circle. [3]

4 Find all the values of x in the range  $0^{\circ} < x < 360^{\circ}$  that satisfy  $\sin x = -4\cos x$ . [5]

5 A car is travelling along a motorway at  $30 \text{ m s}^{-1}$ . At the moment that it passes a point A the brakes are applied so that the car decelerates with constant deceleration. When it reaches a point B, where AB = 300 m, the speed of the car is  $10 \text{ m s}^{-1}$ .

Calculate

(i)	the constant deceleration,	[3]
(ii)	the time taken to travel from A to B.	[2]

- 6 Find the equation of the tangent to the curve  $y = x^3 3x + 4$  at the point (2, 6). [4]
- 7 Use calculus to find the *x*-coordinate of the minimum point on the curve

$$y = x^3 - 2x^2 - 15x + 30.$$

Show your working clearly, giving the reasons for your answer. [7]

8 The figure shows the graphs of  $y = 4x - x^2$  and  $y = x^2 - 4x + 6$ .



	(i) Use an algebraic method to find the <i>x</i> -coordinates of the points where the curves inte	rsect. [3]
	(ii) Calculate the area enclosed by the two curves.	[4]
9	The points A, B and C have coordinates $(-1, 1)$ , $(5, 8)$ and $(8, 3)$ respectively.	
	(i) Show that $AC = AB$ .	[2]
	(ii) Write down the coordinates of M, the midpoint of BC.	[1]
	(iii) Show that the lines BC and AM are perpendicular.	[2]

- (iv) Find the equation of the line AM. [2]
- 10 (i) By drawing suitable graphs on the same axes, indicate the region for which the following inequalities hold. You should shade the region which is **not** required.

$$2x + 3y \le 12$$
  

$$2x + y \le 8$$
  

$$y \ge 0$$
  

$$x \ge 0$$
[5]

(ii) Find the maximum value of x + 3y subject to these conditions. [2]

## 4 Section B

- (a) You are given that  $f(x) = x^3 3x^2 4x$ . 11
  - (i) Find the three points where the curve y = f(x) cuts the x-axis. [4]
  - (ii) Sketch the graph of y = f(x). [1]
  - (b) You are given that  $g(x) = x^3 3x^2 4x + 12$ .
    - (i) Find the remainder when g(x) is divided by (x + 1). [2]
    - (ii) Show that (x 2) is a factor of g(x). [1]
    - (iii) Hence solve the equation g(x) = 0. [4]
- 12 The work-force of a large company is made up of males and females in the ratio 9 : 11. One third of the male employees work part-time and one half of the female employees work part-time.

8 employees are chosen at random.

Find the probability that

(i)	all are males,	[2]
(ii)	exactly 5 are females,	[4]
(iii)	at least 2 work part-time.	[6]

(iii) at least 2 work part-time.

13 In the pyramid OABC, OA = OB = 37 cm, OC = 40 cm, CA = CB = 20 cm and AB = 24 cm. M is the midpoint of AB.



#### Calculate

(i)	the lengths OM and CM,	[3]
( <b>ii</b> )	the angle between the line OC and the plane ABC,	[4]
(iii)	the volume of the pyramid.	[5]
	1	

[The volume of a pyramid  $= \frac{1}{3} \times \text{base area} \times \text{height.}$ ]

## [Question 14 is printed overleaf.]

14 An extending ladder has two positions. In position A the length of the ladder is x metres and, when the foot of the ladder is placed 2 metres from the base of a vertical wall, the ladder reaches y metres up the wall.



In position B the ladder is extended by 0.95 metres and it reaches an extra 1.05 metres up the wall. The foot of the ladder remains 2 m from the base of the wall.

(i) Use Pythagoras' theorem for position  $\mathbf{A}$  and position  $\mathbf{B}$  to write down two equations in x and y.

[2]

- (ii) Hence show that 2.1y = 1.9x 0.2. [3]
- (iii) Using these equations, form a quadratic equation in *x*.Hence find the values of *x* and *y*.

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# **Additional Mathematics**

ADVANCED FSMQ 6993

# Mark Scheme for the Unit

June 2007

6993/MS/R/07

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by Examiners. It does not indicate the details of the discussions which took place at an Examiners' meeting before marking commenced.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the Report on the Examination.

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# Additional Mathematics FSMQ (6993)

## MARK SCHEME FOR THE UNIT

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# Mark Scheme 6993 June 2007

Q.		Answer		Mark	Notes
Sec	tion /	A			
1		3(x+2) > 2-x		M1	Expand and collect
		$\Rightarrow 3x + 6 > 2 - x$		A1	Only 2 terms
		$\Rightarrow 4x > -4$		A1	
		$\Rightarrow x > -1$		5	
2		$v = 6 + 3t^2 \Longrightarrow s = 6t + t^3 + c$		M1 A1	Ignore c
				DM1	Either sub to find <i>c</i>
		Take $s = 0$ when $t = 1 \Longrightarrow c = -7$			or sub and subtract
		When $t = 3$ , $s = 18 + 27 - 7 = 38$		A1	from definite integral
		Alternatively:			M1 int A1
		$s = \int_{1}^{3} (6 + 3t^2) dt = [6t + t^3]^3 = (18 + 27)$ (6)	1) - 38		DM1 sub and sub
		$3 = \int_{1}^{1} (0+3i) di = [0i+i]_{1}^{1} = (10+2i) = (0+3i)$	-1) - 30	4	A1
2		2 2 4 6 2 0		N/1	Complete the square
5		$x^{2} + y^{2} - 4x - 6y + 3 = 0$			
		$\Rightarrow x^2 - 4x + y^2 - 6y = -3$			
		$\Rightarrow x^2 - 4x + 4 + y^2 - 6y + 9 = 4 + 9 - 3$			
		$\Rightarrow (x-2)^2 + (y-3)^2 = 10$		B1	Centre
		$\Rightarrow$ Centre (2, 3), radius $\sqrt{10}$ ( $\approx 3.162$ )		3	Accept correct
		SC: Penultimate line M1 A1			answers with no
		S.C. Centre B1			working
		Find a point on the circle			
		and then use Pythagoras M1 to find radius A1			
4		$\sin x = -4\cos x \Longrightarrow \tan x = -4$		B1	
		$\Rightarrow x = +75.96^{\circ}$		B1	For either value from
		$\Rightarrow x = 180 - 75.96 = 104^{\circ}$		M1	For method to find a
		and $x = 360 - 75.96 = 284^{\circ}$		A1	correct answer from
				5	calculator
		Alternatively			-1 extra values
		Use of $s^2 + c^2 = 1$	M1		outside 360 <sup>0</sup>
		$\Rightarrow \cos^2 x = \frac{1}{17}$			
		$\Rightarrow x = \pm 75.96^{\circ}$	A1		
		$\Rightarrow x = 180 - 75.96 = 104^{\circ}$	M1 A1		
		and $x = 360 - 75.96 = 284^{\circ}$	A1		
		S.C. Graphical method $\pm 2^{\circ}$ tolerance B1 B1			

5	(i)	Using $v^2 = u^2 + 2as$	M1		Got to be used!
		$\Rightarrow 10^2 = 30^2 + 2a.300$	A1		
		$\Rightarrow 600a = -800$	۸1		lanoro, vo oign
		$\Rightarrow a = -\frac{4}{2}$	AI		ignore –ve sign.
		3		3	
	(ii)	Using $v = u + at$	M1		
		$\Rightarrow 10 = 30 - \frac{4}{3}t$			
		$\Rightarrow t = 20 \times \frac{3}{4} = 15$	F1	2	From their <i>a</i>
		Or: $s = \frac{u+v}{2}t$ $\Rightarrow 300 = \frac{30+10}{2}t$ $\Rightarrow t = \frac{600}{40} = 15$			This could be used in (i) to find <i>t</i> then <i>a</i>
6		$\frac{\mathrm{d}y}{\mathrm{d}x} = 3x^2 - 3$	B1 M1		Diff correctly Substitute in their gradient function
		dy	DM1		Set up equation with
		At (2, 6) $\frac{1}{dx} = 9 \Rightarrow y - 6 = 9(x - 2)$	A 4		their gradient
		$\Rightarrow y = 9x - 12$	AI	4	
7		$\frac{dy}{dx} = 3x^2 - 4x - 15$ = 0 when $3x^2 - 4x - 15 = 0$ $\Rightarrow (3x + 5)(x - 3) = 0$	M1 A1 M1		=0 and attempt to solve
		$\Rightarrow (3x+3)(x-3)=0$ $\Rightarrow x=3,-\frac{5}{2}$	A1		
		$d^2 y$	M1		Differentiate again
		$\frac{1}{\mathrm{d}x^2} = 6x - 4$	F1		
		When $x = 3$ , $\frac{d^2 y}{dx^2} > 0$	A1		
		⇒ minimum		7	Providing all other marks earned
		$\Rightarrow x = 3$			
		N.B. Any valid method is acceptable, but not that $x = 3$ is the right hand value or that the y value is lower then for the other value of x.			

8	(i)	$4x - x^2 = x^2 - 4x + 6$	M1		Equate and attempt
		$\Rightarrow 2x^2 - 8x + 6 = 0$			to collect terms
		$\Rightarrow x^2 - 4x + 3 = 0$	M1		Solve a quadratic
		$\Rightarrow (x-3)(x-1) = 0$	A1		Ans only seen - B1
		$\Rightarrow x = 3,1$		3	
	(ii)	Area = $\int_{1}^{3} (4x - x^2) dx - \int_{1}^{3} (x^2 - 4x + 6) dx$	M1		Integrate
		$= \left[2x^{2} - \frac{x^{3}}{3}\right]_{1}^{3} - \left[\frac{x^{3}}{3} - 2x^{2} + 6x\right]_{1}^{3}$	A1		All terms; condone one slip
		$=(18-9)-(2-\frac{1}{3})-(9-18+18)+(\frac{1}{3}-2+6)$	DM1		Substitute and
		$(1)^2 + (1)^2$	A1		limits wrong)
		=9-1-9+4-=2-3		4	
		Alternatively:			
		Area = $\int_{1}^{3} (8x - 2x^2 - 6) dx$			M1 integrate
		$\begin{bmatrix} 2 & 2x^3 \end{bmatrix}^3$			A1
		$= \left\lfloor \frac{4x^2 - \frac{2x}{3} - 6x}{3} \right\rfloor_1$			DM1 sub and sub
		$= (36 - 18 - 18) - \left(4 - \frac{2}{3} - 6\right) = 0 - \left(-2\frac{2}{3}\right)$			A1
		$=2\frac{2}{3}$			
9	(i)	$AB = \sqrt{(5 - 1)^{2} + (8 - 1)^{2}} = \sqrt{85}$	M1		For sight of Pythagoras used at
		$AC = \sqrt{(81)^2 + (3-1)^2} = \sqrt{85}$	A1	2	least once
	(ii)	$M = \left(\frac{5+8}{2}, \frac{8+3}{2}\right) = \left(\frac{13}{2}, \frac{11}{2}\right)$	B1	1	
	(iii)	Grad BC = $\frac{8-3}{5-8} = -\frac{5}{2}$	E1		Both gradients; AM ft from their M
		Grad AM = $\frac{\frac{11}{2} - 1}{\frac{13}{2} + 1} = \frac{\frac{9}{2}}{\frac{15}{2}} = \frac{9}{15} = \frac{3}{5}$			
		$\Rightarrow m_1.m_2 = -\frac{5}{2} \cdot \frac{3}{7} = -1$	B1		Both and demonstration
		Allow a geometric argument with reference to M being midpoint and the triangle isosceles.		2	
	(iv)	$y = 1 - \frac{3}{2}(r+1)$	M1		Must use (-1, 1) or
		$ \begin{array}{c} y = 1 - \frac{1}{5} \left( x + 1 \right) \\ \rightarrow 5 y - 2 x + 9 \end{array} $	A1		their wi and their g
		$\rightarrow Jy = Jx + 0$		2	



#### Section B

11	(a)(i)	$x^3 - 3x^2 - 4x = 0$	M1		
		$\Rightarrow x(x^2 - 3x - 4) = 0$	Δ1		Accept any valid method
		$\Rightarrow r(r-4)(r+1) = 0$	A1		valia metrica
		$\Rightarrow x(x-1)(x+1) = 0$ $\Rightarrow x = 0, -1, 4$	A1		
				4	
		S.C. just answers B2			
	(ii)	Must have points on axes	B1	1	
	(b)(i)	Remainder theorem or long division G(-1) = 12	M1 A1	2	For sub –1
	(ii)	g(2) = 0	B1	1	For sub $x = 2$
	(iii)	By continued trial	M1	-	
		or by division and quadratic factorisation	Δ1		3
		g(3) = 0, g(-2) = 0	A1		-2
		$\Rightarrow$ <i>x</i> = 2, 3, -2	A1	٨	Final answer
		S.C. just answers B2		4	
		Alternatively: By division by $(x - 2)$ and quadratic factorisation M1 $(x - 2)(x^2 - x - 6) = 0$ A1 $\Rightarrow (x - 2)(x + 2)(x - 3) = 0$ A1 $\Rightarrow x = 2, -2, 3.$ A1			

12	(i)	$(9)^{8}$			
		$P(All males) = \left(\frac{1}{20}\right) = 0.00168$		M1	
		(20)		2 AI	
	(ii)	$(9)^{3}(11)^{5}$		M1	powers
	. ,	$P(5 \text{ females}) = {}^{8}C_{5} \left[ \frac{3}{20} \right] \left[ \frac{11}{20} \right]$		M1	coefficient
		(20)(20)		A1	56 (could
		$= 0.2568 \approx 0.257$		A1	be implied)
				4	implied)
	(iii)	$23 \left(2 \text{ prot} 17\right)$		M1 A1	probability
		$P(\text{full-time}) = \frac{1}{40}  (\text{ Or } P(PT) = \frac{1}{40})$			
		P(at least two part-time) = 1 - P(all FT) - P(all FT)	(7FT 1PT)	N/1	1–2correct
		$\Gamma(at least two part-time) = \Gamma(an \Gamma \Gamma) = \Gamma$	(/11,111)		terms
				A1	Powers
		$-1 - \left(\frac{23}{23}\right)^8 - 8\left(\frac{23}{23}\right)^7 \left(\frac{17}{17}\right)$		A1	coefficient
		$-1 - \left(\frac{1}{40}\right) - 3 \left(\frac{1}{40}\right) \left(\frac{1}{40}\right)$		A1	Ans
		=1-0.0119-0.0706=0.917		6	
		Alternatively:			
		Add 7 terms	M1		
		$(23)^6 (17)^2 (17)^8$			
		$28\left(\frac{1}{40}\right)\left(\frac{1}{40}\right)$ + $\left(\frac{1}{40}\right)$	AI powers		
			A1 Coeffs		
		0.017			
		= 0.917	A1 Ans		
		S.C. Read "At least two" as "exactly two"			
		$(23)^6 (17)^2$			
		$28\left(\frac{-2}{40}\right)\left(\frac{1}{40}\right) = 28 \times 0.00653 = 0.1828$	B1		

13	(i)	Pythagoras:	M1	Correct use of Pythagoras for at
		$OM^2 = 37^2 - 12^2 \Longrightarrow OM = 35$	A1	least one
		$CM^2 = 20^2 - 12^2 \Rightarrow CM = 16$	A1	
			3	
	(ii)	Use cosine rule on triangle OCM	M1	Correct angle
		$16^2 \pm 40^2 = 35^2$	M1	Correct use of
		$\Rightarrow \cos C = \frac{10^{\circ} + 40^{\circ} - 55^{\circ}}{2 \cdot 16^{\circ} + 40^{\circ}} \Rightarrow C = 60.5^{\circ}$	A1	cosine formula
		$2 \times 16 \times 40$	A1	Ans
			4	
	(iii)	Sight of attempt to find base area	M1	
		1	A1	Can be implied
		Area = $\frac{1}{2} \times 16 \times 24 = 192$		
		2	M1	
		Sight of attempt to find height		
		$h = 40 \sin 60.5 = 34.8$	A1	Can be implied
		n = +0.511100.5 = 5+.0		
		$\Rightarrow \text{Volume} = \frac{1}{3} \times 192 \times 34.8 = 2228 \approx 2230 \text{cm}^3$	A1 5	

14	(i)	Apply Pythagoras to both triangles:			
	(-)	$x^2 = y^2 + 4$	B1		
		$(x + 0.95)^2 = (y + 1.05)^2 + 4$	B1		
				2	
	(ii)	Subtract:	M1	-	
	()	$2 \times 0.95 \times \pm 0.95^2 = 2 \times 1.05 \times \pm 1.05^2$	A1		
		$\Rightarrow 2.1 = 1.0 \times (1.05^2 - 0.05^2)$	/		
		$\Rightarrow 2.1y = 1.0x = (1.00 = 0.00)$	Δ1		
		$\Rightarrow 2.1y = 1.9x - 0.2$	///	З	
		Alternatively.		5	
		Multiply out one of the brackets B1			
		Substitute for y M1			
		Correct result A1			
	/:::)	Substitute for us	N/1		Cot y as subject
	(111)	Substitute for y.			Get y as subject
		$x^{2} = (1.9x - 0.2)^{2} + 4$	N/1		Sub expression
		$x = \left(\frac{2}{2}\right)^{+4}$			Sub expression
					ior y
		$\Rightarrow 2.1^{2} x^{2} = 1.9^{2} x^{2} - 2 \times 0.2 \times 1.9 x + 0.2^{2} + 4 \times 2.1^{2}$	A 4		
		$\rightarrow 0.8r^2 + 0.76r - 17.68 = 0$	AI		Corrot
					Conect
		$\Rightarrow x = \frac{-0.76 \pm \sqrt{0.76^2 + 4 \times 0.8 \times 17.68}}{-0.76 \pm \sqrt{0.76^2 + 4 \times 0.8 \times 17.68}} = \frac{-0.76 \pm 7.56}{-0.76 \pm 7.56} = 4.25$			quadratic
		1.6 1.6	AI		Solve
		Substitute :			ignore other root
		(1.9x - 0.2)			
		$y = \left[ \frac{1}{21} \right] = 3.75$		7	
				1	
		With head least ments if means them are an annual sites			
		withhold last mark if more than one answer given			
		The quadratic in v is $20v^2 + 21v - 360 = 0$			
		Integer coefficients for x equation gives			
		$20x^2 + 19x - 442 = 0$			

#### FSMQ Advanced Additional Mathematics 6993 June 2007 Assessment Session

## **Unit Threshold Marks**

Unit	Maximum Mark	Α	В	С	D	E	U
6993	100	70	60	50	40	30	0

The cumulative percentage of candidates awarded each grade was as follows:

	Α	В	С	D	E	U	Total Number of Candidates
6993	28.8	38.6	48.1	57.5	66.8	100	5500

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# **Additional Mathematics**

ADVANCED FSMQ 6993

# **Report on the Unit**

# June 2007

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This report on the Examination provides information on the performance of candidates which it is hoped will be useful to teachers in their preparation of candidates for future examinations. It is intended to be constructive and informative and to promote better understanding of the syllabus content, of the operation of the scheme of assessment and of the application of assessment criteria.

Reports should be read in conjunction with the published question papers and mark schemes for the Examination.

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# Additional Mathematics FSMQ (6993)

### **REPORT ON THE UNIT**

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### Free Standing Mathematics Qualification, Advanced Level Additional Mathematics 6993

We can report another rise in the number of candidates sitting this examination with an entry of 5500.

I regret to say, however, that we also have to report a rise in the number of candidates who seem, from their scripts, to be entered inappropriately. The specification states that Additional Mathematics is suitable for candidates with (or are expecting to receive) a high grade at Higher level GCSE; for such candidates this specification can be used as enrichment work. When candidates do not even demonstrate an understanding of some material in the Intermediate tier and who gain a total mark in single figures we are left doubting the wisdom of their entry. One candidate even wrote on question 7 "what is calculus?"

For many candidates, the level seemed appropriate but perhaps the paper was a little long; it was evident that some strong candidates did not finish Question 14 for lack of time.

Most candidates gave their answers to an appropriate degree of accuracy, though there were still a significant minority either writing down all the digits seen on their calculator or approximating to only 2 significant figures. As in previous years, examiners deducted a mark where it was seen for the first time (and only once throughout the paper).

### Section A

### Q1 (Inequality)

A few could not cope with the inequality sign and replaced it with an equal sign and then tried to deduce what the answer might be at the end, rarely getting it correct. Others had difficulty with the manipulation of algebra. For the better candidates it was an easy start to the paper.

#### Q2 (Variable acceleration)

This defeated all but the strongest candidates. The vast majority of candidates assumed constant acceleration and tried to apply the formulae that they knew to get an answer. Many who would otherwise have got it correct added the value for *s* at the two end points of integration rather than subtract.

### Q3 (Circle)

Many knew what they were trying to obtain (and wrote down the coordinates of the centre correctly) but were once again defeated by the algebraic manipulation.

It is worth noting that  $\sqrt{10}$  is the exact value of the radius and is therefore an acceptable answer. Those who wrote down an approximation were not penalised for having too many significant figures if the exact value had already been seen.

### Q4 (Trigonometrical equation)

This question tested not only the identity  $\frac{\sin x}{\cos x} = \tan x$  but how to identify the angles in the

required range from the value given on the calculator. Strong candidates managed both; others were less than successful. We saw only rarely an effort to square and use the identity  $\sin^2 x + \cos^2 x = 1$  with none totally successful.

In this case, correct to three significant figures is also correct to the nearest degree and this was the expected approximation.

#### Q5 Constant acceleration

Many candidates had difficulty in choosing the right formula to use and then difficulty in identifying the original and final velocities. It was of course possible, and permissible, to find the time first and then the deceleration.

Using the standard notation,  $a = -\frac{4}{3}$ , giving the deceleration as  $\frac{4}{3}$  m s<sup>-2</sup>. On this occasion the

negative sign and the units were ignored.

#### **Q6 Gradient function**

Here the major error was to put the gradient function equal to zero; for these candidates the connection between the gradient function and the gradient of the tangent at a point was missed.

#### Q7 Maxima and minima

Most candidates were able to find the points where stationary values occurred, though few seemed prepared to factorise. Demonstrating that there is a minimum at x = 3 was acceptable in one of three ways; via the second gradient function, the magnitude of the gradient either side of x = 3 and the value of the function either side of x = 3. Simply saying that the larger value of x is the minimum because the curve is a cubic was not acceptable.

#### Q8 Area between two curves

Not all candidates were able to find the points of intersection of the curves. It was not necessary to identify which curve was which and so a negative value for the area was accepted. Some candidates subtracted the functions before integrating and others integrated to find the area between each curve separately and subtracting to find the answer. A very small number of able candidates found the area between one curve and the line y = 3 and doubled the answer – we would have liked to have given bonus marks for these candidates!

#### **Q9** Coordinate geometry

Part (i) was usually done well, but in part (ii) candidates often halved the difference in coordinates rather than halving the sum. In part (iii) candidates were expected to demonstrate knowledge of the

relationship of perpendicular gradients  $m_1m_2 = -1$ . To say " $m_1 = -\frac{5}{3}$ ,  $m_2 = \frac{3}{5}$  and therefore the lines

are perpendicular" is not enough. This is a case where "show that..." requires candidates to demonstrate fully their understanding and knowledge of what is being tested.

A geometric argument was accepted, though this had to be convincing. Simply to say that the triangle ABC is isosceles was not enough, though we did not expect a full proof of congruency.

### Q10 Linear programming

The graph of the lines was an easy source of marks and usually candidates shaded the correct part for the two lines. Additionally in this question, candidates were required to show  $x \ge 0$  and  $y \ge 0$  and many missed this shading.

In part (ii) many candidates assumed that the answer was one of the vertices of their required area and worked out the value of x + 3y at each, concluding correctly the value of 12. Others treated P = x + 3y as an objective function and, by drawing a typical line, deduced the right answer. A small minority shaded the quadrilateral instead of shading everywhere else.

In questions like this, it is not necessary to plot the lines on graph paper, but it is helpful to use appropriate scales -a scale on the *x* axis, for instance, that goes from 0 to 50 does leave the required area looking a little small!

## Section B

### Q11 Polynomials

Part (a) (i) required candidates to solve a cubic equation. Given that there is no constant term in the function, it was expected that at this level candidates would spot that *x* was a factor and that x = 0 was one of the roots. This reduces the function immediately to a quadratic. Those who did spot this completed this part of the question very easily. Others who did not spot it spent a very long time (and much more than the 4 marks would indicate was necessary) trying to find roots by the factor formula.

Part (ii) was a simple sketch; the main failure here for candidates who got the shape of the curve correct was the failure to put any scale on the axes to indicate where the curve cut the axes. Many candidates drew the curve "upside down".

Part (b) was done very much better and many candidates scored all 7 marks here with no marks for part (a).

It is worth noting that long division, carried out correctly, will always demonstrate a root or find the remainder. However, it is also worth noting that this is always very time consuming and may have contributed significantly to the fact that many failed to finish the paper. In part (b)(i), for instance, the value of g(-1) can be found in a single line, while dividing g(x) by (x + 1) takes very much longer; in this case it also introduced a further worry for candidates in that the remainder had no constant term and so it seemed as though something was missing.

### **Q12 Binomial Distribution**

A number of candidates misread the question and set n = 20.

For those comfortable with this topic, the first two parts rarely produced any problems. Finding the probability to use in (iii) caused a problem for some, as did the question to find "at least... "

A few found the remaining terms, thus expending more time than necessary; others took 1 or 3 terms from 1.

Fewer candidates expressed their answers to an inappropriate number of significant figures, but rather more only wrote their answers to 2 decimal places.

It also seemed clear to the examiners that a number of candidates had no understanding of the Binomial Distribution and some little idea of probability, given that we saw some answers greater that 1.

### Q13 3-D Geometry

Part (i) was usually completed satisfactorily, though some got the terms muddled in their Pythagoras calculation. A significant number, however, worked out the wrong angle in part (ii), typically one of the other two angles in triangle OCM and rather more frequently the angle OCB. Candidates who thought that this was the angle might have been alerted to the fact that the results of part (i) were not used in this calculation and therefore might have asked themselves what was the purpose of part (i).

We have commented before that we believe that candidates would benefit from drawing the triangles in which they are carrying out a calculation. Had they done so then there would be less likelihood of getting Pythagoras wrong in part (i). Additionally some attempted to use the cosine formula in part (ii) with lengths drawn from different triangles.

To find the volume in part (iii) it was required to find the base area and the height. This defeated many, perhaps because of the multiple steps. Others took the height to be OB or OC and took the

base area as  $\frac{1}{2} \times 20 \times 40$  - again, we wonder whether this error would have occurred had a triangle

been drawn.

### Q14 Algebraic manipulation

Strong candidates were not phased by the fact that there were non-integer values here. They wrote down the two equations, subtracted to obtain the linear relationship, made y the subject, substituted back to give a quadratic which they then solved (sometimes by factorisation!) to give exact answers for x and y. This was all completed in less than a page.

Others had less success and were let down by algebra.

The question included a "show that..." and candidates should be aware that every step must be written and convincing to obtain the marks.

Some rather startling errors were:

$$x^2 = y^2 + 4 \Longrightarrow x = y + 2$$

 $(y+1.05)^2 = y^2 + 1.05^2$ 

It was also clear that the rather poor response to this question was often due to lack of time.

### FSMQ Advanced Additional Mathematics 6993 June 2007 Assessment Session

## **Unit Threshold Marks**

Unit	Maximum Mark	Α	В	С	D	E	U
6993	100	70	60	50	40	30	0

The cumulative percentage of candidates awarded each grade was as follows:

	A	В	С	D	E	U	Total Number of Candidates
6993	28.8	38.6	48.1	57.5	66.8	100	5500

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