## ADVANCED GCE UNIT <br> MATHEMATICS (MEI)

## 4754(B)/01

Applications of Advanced Mathematics (C4)
Paper B: Comprehension

## TUESDAY 23 JANUARY 2007

Afternoon
Time: Up to 1 hour

Additional materials:
Rough paper
MEI Examination Formulae and Tables (MF2)

Candidate
Name
Centre
Number $\square$
Candidate Number
$\square$

## INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided.
- Answer all the questions.
- Write your answers in the spaces provided on the question paper.
- You are permitted to use a graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.


## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [ ] at the end of each question or part question.
- The total number of marks for this paper is 18 .
- The insert contains the text for use with the questions.
- You may find it helpful to make notes and do some calculations as you read the passage.
- You are not required to hand in these notes with the question paper.


## ADVICE TO CANDIDATES

- Read each question carefully and make sure you know what you have to do before starting your answer.
- You are advised that an answer may receive no marks unless you show

| For Examiner's Use |  |
| :---: | :---: |
| Qu. | Mark |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| Total |  | sufficient detail of the working to indicate that a correct method is being used.

This document consists of 4 printed pages and an insert.

1 In a certain country, twenty cars are on display in a car showroom. The costs of the cars in the local currency, the zen, are shown below.

| 10255 | 23250 | 48500 | 25950 | 12340 |
| ---: | ---: | ---: | ---: | ---: |
| 34750 | 5690 | 13580 | 7450 | 9475 |
| 18890 | 14675 | 6295 | 21225 | 37850 |
| 51200 | 43340 | 16575 | 8380 | 28880 |

(i) Complete the table giving the frequencies of the leading digits.

| Leading digit | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 6 | 4 | 2 |  |  |  |  |  |  |

The country joins the European Union and so the costs of the cars are converted to euros. The exchange rate is 1 zen $=3$ euros.
(ii) Give the costs of the cars in euros in the space below and then complete the table giving the frequencies of the leading digits in euros.
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$\qquad$
$\qquad$
$\qquad$

| Leading digit | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 7 |  |  |  |  |  |  |  | 0 |

(iii) In the table below, give the frequencies predicted by Benford's Law, in each case correct to one decimal place.

| Leading digit | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 6.0 |  |  |  |  |  |  |  |  |

(iv) Compare the results in the three tables.
$\qquad$
$\qquad$

2 On lines 28 and 29 it says 'Similarly, the numbers in Table 3 with leading digit 5, 6, 7, 8 or 9 give numbers in Table 5 with leading digit 1'. Explain how this is reflected in the frequencies in Table 4 and Table 6.
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$\qquad$
$\qquad$

3 Line 104 refers to the relationship $p_{1}=p_{3}+p_{4}+p_{5}$. Explain how this relationship is obtained.
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$\qquad$
$\qquad$
$\qquad$

4 Benford's Law is quoted on lines 126 to 127. Show that this is equivalent to

$$
p_{n}=\log _{10}\left(1+\frac{1}{n}\right)
$$

$\qquad$
$\qquad$
$\qquad$
$\qquad$

5 Using the results $\mathrm{L}(4)=2 \times \mathrm{L}(2)$ and $\mathrm{L}(6)=\mathrm{L}(3)+\mathrm{L}(2)$, and the relationship $p_{6}+p_{7}=p_{3}$, derive the result $\mathrm{L}(8)=3 \times \mathrm{L}(2)$ stated on line 123 .
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$\qquad$
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$\qquad$
$\qquad$

6 The distribution of leading digits in the daily wages, in pounds sterling, of the employees of

The employees all work a 5-day week. Using the values for the daily wages above, find the entries marked $a$ and $b$ for the weekly wages in the table below. Explain your reasoning.[4]

| Leading digit | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency <br> (weekly wages) | $a$ |  |  | $b$ |  |  |  |  |  |

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$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

