## OXFORD CAMBRIDGE AND RSA EXAMINATIONS

## Advanced Subsidiary General Certificate of Education Advanced General Certificate of Education

MEI STRUCTURED MATHEMATICS

## 4761

Mechanics 1
Tuesday 7 JUNE 2005 Afternoon 1 hour 30 minutes
Additional materials:
Answer booklet
Graph paper
MEI Examination Formulae and Tables (MF2)

## TIME

 1 hour 30 minutes
## INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer all the questions.
- You are permitted to use a graphical calculator in this paper.


## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [ ] at the end of each question or part question.
- You are advised that an answer may receive no marks unless you show sufficient detail of the working to indicate that a correct method is being used.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by $\mathrm{g} \mathrm{m} \mathrm{s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use $\mathrm{g}=9.8$.
- The total number of marks for this paper is 72 .


## Section A (36 marks)

1 A particle travels along a straight line. Its acceleration during the time interval $0 \leqslant t \leqslant 8$ is given by the acceleration-time graph in Fig. 1.


Fig. 1
(i) Write down the acceleration of the particle when $t=4$. Given that the particle starts from rest, find its speed when $t=4$.
(ii) Write down an expression in terms of $t$ for the acceleration, $a \mathrm{~m} \mathrm{~s}^{-2}$, of the particle in the time interval $0 \leqslant t \leqslant 4$.
(iii) Without calculation, state the time at which the speed of the particle is greatest. Give a reason for your answer.
(iv) Calculate the change in speed of the particle from $t=5$ to $t=8$, indicating whether this is an increase or a decrease.

2 A particle moves along the $x$-axis with velocity, $v \mathrm{~m} \mathrm{~s}^{-1}$, at time $t$ given by

$$
v=24 t-6 t^{2} .
$$

The positive direction is in the sense of $x$ increasing.
(i) Find an expression for the acceleration of the particle at time $t$.
(ii) Find the times, $t_{1}$ and $t_{2}$, at which the particle has zero speed.
(iii) Find the distance travelled between the times $t_{1}$ and $t_{2}$.

3 A particle rests on a smooth, horizontal plane. Horizontal unit vectors $\mathbf{i}$ and $\mathbf{j}$ lie in this plane. The particle is in equilibrium under the action of the three forces $(-3 \mathbf{i}+4 \mathbf{j}) \mathrm{N}$ and $(21 \mathbf{i}-7 \mathbf{j}) \mathrm{N}$ and $\mathbf{R N}$.
(i) Write down an expression for $\mathbf{R}$ in terms of $\mathbf{i}$ and $\mathbf{j}$.
(ii) Find the magnitude of $\mathbf{R}$ and the angle between $\mathbf{R}$ and the $\mathbf{i}$ direction.

4 A block of mass 4 kg is in equilibrium on a rough plane inclined at $60^{\circ}$ to the horizontal, as shown in Fig. 4. A frictional force of 10 N acts up the plane and a vertical string AB attached to the block is in tension.


Fig. 4
(i) Draw a diagram showing the four forces acting on the block.
(ii) By considering the components of the forces parallel to the slope, calculate the tension in the string.
(iii) Calculate the normal reaction of the plane on the block.

5 The position vector of a particle at time $t$ is given by

$$
\mathbf{r}=\frac{1}{2} t \mathbf{i}+\left(t^{2}-1\right) \mathbf{j},
$$

referred to an origin O where $\mathbf{i}$ and $\mathbf{j}$ are the standard unit vectors in the directions of the cartesian axes $\mathrm{O} x$ and $\mathrm{O} y$ respectively.
(i) Write down the value of $t$ for which the $x$-coordinate of the position of the particle is 2 . Find the $y$-coordinate at this time.
(ii) Show that the cartesian equation of the path of the particle is $y=4 x^{2}-1$.
(iii) Find the coordinates of the point where the particle is moving at $45^{\circ}$ to both $\mathrm{O} x$ and $\mathrm{O} y$.

Section B (36 marks)
6 A car of mass 1000 kg is travelling along a straight, level road.


Fig. 6.1
(i) Calculate the acceleration of the car when a resultant force of 2000 N acts on it in the direction of its motion.

How long does it take the car to increase its speed from $5 \mathrm{~m} \mathrm{~s}^{-1}$ to $12.5 \mathrm{~m} \mathrm{~s}^{-1}$ ?

The car has an acceleration of $1.4 \mathrm{~m} \mathrm{~s}^{-2}$ when there is a driving force of 2000 N .
(ii) Show that the resistance to motion of the car is 600 N .

A trailer is now atached to the car, as shown in Fig. 6.2. The car still has a driving force of 2000 N and resistance to motion of 600 N . The trailer has a mass of 800 kg . The tow-bar connecting the car and the trailer is light and horizontal. The car and trailer are accelerating at $0.7 \mathrm{~m} \mathrm{~s}^{-2}$.


Fig. 6.2
(iii) Show that the resistance to the motion of the trailer is 140 N .
(iv) Calculate the force in the tow-bar.

The driving force is now removed and a braking force of 610 N is applied to the car. All the resistances to motion remain as before. The trailer has no brakes.
(v) Calculate the new acceleration. Calculate also the force in the tow-bar, stating whether it is a tension or a thrust (compression).

7 In this question take the value of $\boldsymbol{g}$ to be $\mathbf{1 0} \mathrm{m} \mathrm{s}^{\mathbf{- 2}}$.
A particle A is projected over horizontal ground from a point P which is 9 m above a point O on the ground. The initial velocity has horizontal and vertical components of $10 \mathrm{~m} \mathrm{~s}^{-1}$ and $12 \mathrm{~ms}^{-1}$ respectively, as shown in Fig. 7. The trajectory of the particle meets the ground at X. Air resistance may be neglected.


Fig. 7
(i) Calculate the speed of projection $u \mathrm{~ms}^{-1}$ and the angle of projection $\theta^{\circ}$.
(ii) Show that, $t$ seconds after projection, the height of particle A above the ground is $9+12 t-5 t^{2}$. Write down an expression in terms of $t$ for the horizontal distance of the particle from O at this time.
(iii) Calculate the maximum height of particle A above the point of projection.
(iv) Calculate the distance OX.

A second particle, $B$, is projected from $O$ with speed $20 \mathrm{~ms}^{-1}$ at $60^{\circ}$ to the horizontal. The trajectories of A and B are in the same vertical plane. Particles A and B are projected at the same time.
(v) Show that the horizontal displacements of A and B are always equal.
(vi) Show that, $t$ seconds after projection, the height of particle B above the ground is $10 \sqrt{3} t-5 t^{2}$.
(vii) Show that the particles collide 1.7 seconds after projection (correct to two significant figures).

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