

**OXFORD CAMBRIDGE AND RSA EXAMINATIONS**

**Advanced Subsidiary General Certificate of Education  
Advanced General Certificate of Education**

**MEI STRUCTURED MATHEMATICS**

**4755**

Further Concepts For Advanced Mathematics (FP1)

Friday            **21 JANUARY 2005**            Afternoon            1 hour 30 minutes

Additional materials:  
Answer booklet  
Graph paper  
MEI Examination Formulae and Tables (MF2)

**TIME**    1 hour 30 minutes

**INSTRUCTIONS TO CANDIDATES**

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer **all** the questions.
- You are permitted to use a graphical calculator in this paper.

**INFORMATION FOR CANDIDATES**

- The number of marks is given in brackets [ ] at the end of each question or part question.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The total number of marks for this paper is 72.

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**This question paper consists of 4 printed pages.**

## Section A (36 marks)

1 You are given the matrix  $\mathbf{M} = \begin{pmatrix} 2 & 3 \\ -2 & 1 \end{pmatrix}$ .

Find the inverse of  $\mathbf{M}$ .

The transformation associated with  $\mathbf{M}$  is applied to a figure of area 2 square units. What is the area of the transformed figure? [3]

2 (i) Show that  $\frac{1}{r+1} - \frac{1}{r+2} = \frac{1}{(r+1)(r+2)}$ . [2]

(ii) Hence use the method of differences to find the sum of the series

$$\sum_{r=1}^n \frac{1}{(r+1)(r+2)}. \quad [4]$$

3 (i) Solve the equation  $\frac{1}{x+2} = 3x+4$ . [3]

(ii) Solve the inequality  $\frac{1}{x+2} \leq 3x+4$ . [4]

4 Find  $\sum_{r=1}^n r^2(r+2)$ , giving your answer in a factorised form. [6]

5 The roots of the cubic equation  $x^3 + 2x^2 + x - 3 = 0$  are  $\alpha, \beta$  and  $\gamma$ .

Find the cubic equation whose roots are  $\alpha + 1, \beta + 1$  and  $\gamma + 1$ , simplifying your answer as far as you can. [6]

6 Prove by induction that  $\sum_{r=1}^n r2^{r-1} = 1 + (n-1)2^n$ . [8]

**Section B** (36 marks)

- 7 A curve has equation  $y = \frac{(2x - 3)(x + 1)}{(x + 4)(x - 2)}$ .
- (i) Write down the values of  $x$  for which  $y = 0$ . [1]
- (ii) Write down the equations of the three asymptotes. [3]
- (iii) Determine whether the curve approaches the horizontal asymptote from above or from below for
- (A) large positive values of  $x$ ,
- (B) large negative values of  $x$ . [3]
- (iv) Sketch the curve. [3]
- (v) Solve the inequality  $\frac{(2x - 3)(x + 1)}{(x + 4)(x - 2)} \leq 2$ . [4]
- 8 Two complex numbers are given by  $\alpha = 2 - j$  and  $\beta = -1 + 2j$ .
- (i) Find  $\alpha + \beta$ ,  $\alpha\beta$  and  $\frac{\alpha}{\beta}$  in the form  $a + bj$ , showing your working. [6]
- (ii) Find the modulus of  $\alpha$ , leaving your answer in surd form. Find also the argument of  $\alpha$ . [2]
- (iii) Sketch the locus  $|z - \alpha| = 2$  on an Argand diagram. [2]
- (iv) On a separate Argand diagram, sketch the locus  $\arg(z - \beta) = \frac{1}{4}\pi$ . [2]

9 You are given the matrix  $\mathbf{M} = \begin{pmatrix} 0.8 & 0.6 \\ 0.6 & -0.8 \end{pmatrix}$ .

(i) Calculate  $\mathbf{M}^2$ . [1]

You are now given that the matrix  $\mathbf{M}$  represents a reflection in a line through the origin.

(ii) Explain how your answer to part (i) relates to this information. [1]

(iii) By investigating the invariant points of the reflection, find the equation of the mirror line. [3]

(iv) Describe fully the transformation represented by the matrix  $\mathbf{P} = \begin{pmatrix} 0.8 & -0.6 \\ 0.6 & 0.8 \end{pmatrix}$ . [2]

(v) A composite transformation is formed by the transformation represented by  $\mathbf{P}$  followed by the transformation represented by  $\mathbf{M}$ . Find the single matrix that represents this composite transformation. [2]

(vi) The composite transformation described in part (v) is equivalent to a single reflection. What is the equation of the mirror line of this reflection? [1]

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