5 **(i)** Solve the inequality $|2x+1| \leqslant |x-3|$. **[5]**

(ii) Given that x satisfies the inequality $|2x+1| \leqslant |x-3|$, find the greatest possible value of $|x+2|$. **[2]**

6 **(i)** Show by calculation that the equation

$$\tan^2 x - x - 2 = 0,$$

where x is measured in radians, has a root between 1.0 and 1.1. **[3]**

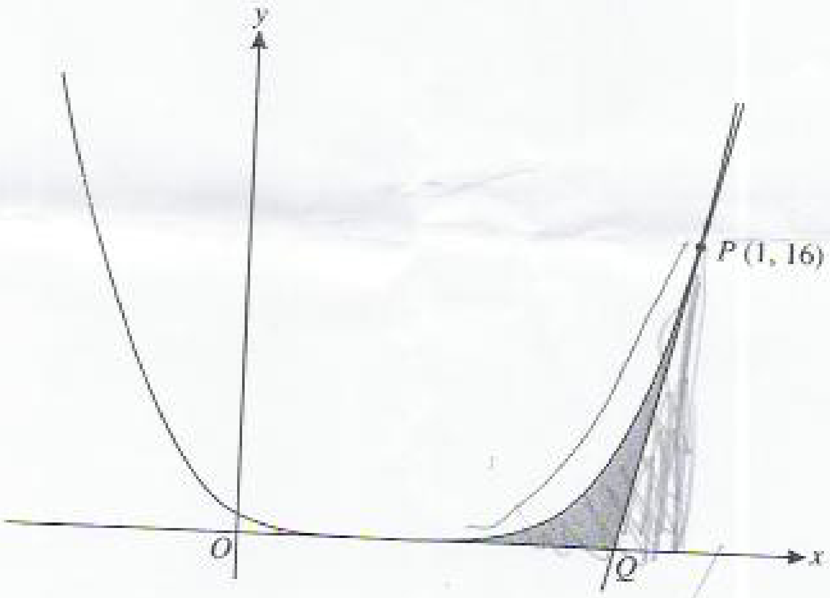
(ii) Use the iteration formula $x_{n+1} = \tan^{-1}\sqrt{2 + x_n}$ with a suitable starting value to find this root correct to 5 decimal places. You should show the outcome of each step of the process. **[4]**

(iii) Deduce a root of the equation

$$\sec^2 2x - 2x - 3 = 0.$$

[3]

7



The diagram shows the curve with equation $y = (3x-1)^4$. The point P on the curve has coordinates $(1, 16)$ and the tangent to the curve at P meets the x-axis at the point Q. The shaded region is bounded by PQ, the x-axis and that part of the curve for which $\frac{1}{3} \leqslant x \leqslant 1$. Find the exact area of this shaded region. **[10]**

8 **(i)** Express $3\cos x + 3\sin x$ in the form $R\cos(x-\alpha)$, where $R > 0$ and $0 < \alpha < \frac{1}{2}\pi$. **[3]**

(ii) The expression $\mathrm{T}(x)$ is defined by $\mathrm{T}(x) = \dfrac{8}{3\cos x + 3\sin x}$.

(a) Determine a value of x for which $\mathrm{T}(x)$ is not defined. **[2]**

(b) Find the smallest positive value of x satisfying $\mathrm{T}(3x) = \frac{8}{9}\sqrt{6}$, giving your answer in an exact form. **[4]**

[Question 9 is printed overleaf.]

Turn over