

OXFORD CAMBRIDGE AND RSA EXAMINATIONS

Advanced Subsidiary General Certificate of Education Advanced General Certificate of Education

MEI STRUCTURED MATHEMATICS

2601

Pure Mathematics 1

Wednesday

12 JANUARY 2005

Afternoon

1 hour 20 minutes

Additional materials: Answer booklet Graph paper MEI Examination Formulae and Tables (MF12)

TIME 1 hour 20 minutes

INSTRUCTIONS TO CANDIDATES

- Write your Name, Centre Number and Candidate Number in the spaces provided on the answer booklet.
- Answer **all** questions.
- You are permitted to use only a scientific calculator in this paper.

INFORMATION FOR CANDIDATES

- The allocation of marks is given in brackets [] at the end of each question or part question.
- You are advised that an answer may receive no marks unless you show sufficient detail of the working to indicate that a correct method is being used.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The total number of marks for this paper is 60.

2

Section A (30 marks)

- 1 State the exact value of tan 30°. Write 30° in radians as simply as possible in the form $k\pi$. [3]
- 2 Solve the equation |2x-5| = 13. [3]
- 3 Sketch the graph of $y = \sin x$ for $0^\circ \le x \le 360^\circ$.

Solve the equation
$$\sin x = -0.3$$
 for $0^{\circ} \le x \le 360^{\circ}$. [4]

- 4 Obtain the binomial expansion of $(1 5x)^4$, simplifying the coefficients. [4]
- 5 Find the *x*-coordinates of the points on the curve $y = x^3 4x^2 + 2$ where the gradient is 3. [4]
- 6 The equation $5x^2 + 3x + c = 0$ has a repeated root. Find the value of c and the value of the repeated root. [4]
- 7 A circle of radius 7 cm has a sector of angle 1.6 radians. Calculate the arc length of the sector.

The arc length is measured with a flexible ruler as 10.2 cm. Calculate the relative error in this measurement. Give your answer to 2 significant figures. [4]

8 Given that y = 5x, find $\int_{0}^{3} \pi x^{2} dy$. State clearly what this integral represents. [4]

Section B (30 marks)

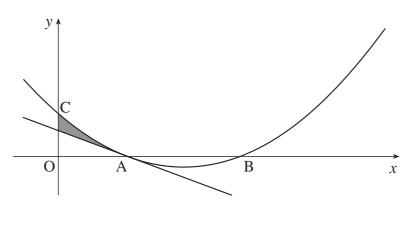


Fig. 9

The curve $y = x^2 - 7x + 10$ cuts the x-axis at A and B and the y-axis at C as shown in Fig. 9.

(i) Write down the coordinates of C.

9

Show that A is (2, 0) and find the coordinates of B.

Hence or otherwise find the coordinates of the turning point of the curve. [5]

[2]

[2]

- (ii) Solve the inequality $x^2 7x + 10 > 0$.
- (iii) Show that the equation of the tangent to the curve at A is y = -3x + 6. [3]
- (iv) Calculate the area of the region bounded by the portion AC of the curve, the tangent at A and the *y*-axis. This region is shown shaded in Fig. 9. [5]
- 10 A circle with centre (2, 4) has equation $x^2 + y^2 4x 8y = 25$.
 - (i) Show that the radius of the circle is $\sqrt{45}$. [3]
 - (ii) Prove that the point (8, 8) is outside the circle.
 - (iii) Find the equation of the line which is perpendicular to the line y + 2x = 8 and which passes through the centre of the circle. [3]
 - (iv) P and Q are the points where the line y + 2x = 8 crosses the circle. Show that PQ is a diameter of the circle and find the coordinates of P and Q. [7]

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