

OXFORD CAMBRIDGE AND RSA EXAMINATIONS

10 JANUARY 2005

Advanced Subsidiary General Certificate of Education Advanced General Certificate of Education

MATHEMATICS

Core Mathematics 2

Monday

Afternoon

1 hour 30 minutes

4722

Additional materials: Answer booklet Graph paper List of Formulae (MF1)

TIME 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer all the questions.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- You are permitted to use a graphical calculator in this paper.

INFORMATION FOR CANDIDATES

- . The number of marks is given in brackets [] at the end of each question or part question.
- The total number of marks for this paper is 72.
- . Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.
- You are reminded of the need for clear presentation in your answers.

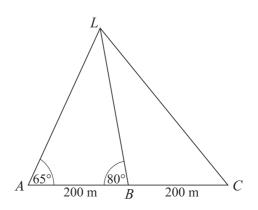
1	Simplify $(3 + 2x)^3 - (3 - 2x)^3$.	[5]
		L- 1

2 A sequence u_1, u_2, u_3, \ldots is defined by

$$u_1 = 2$$
 and $u_{n+1} = \frac{1}{1 - u_n}$ for $n \ge 1$.

- (i) Write down the values of u_2 , u_3 , u_4 and u_5 . [3]
- (ii) Deduce the value of u_{200} , showing your reasoning.

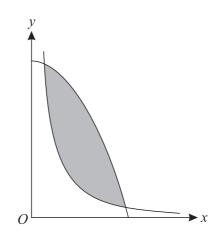




A landmark *L* is observed by a surveyor from three points *A*, *B* and *C* on a straight horizontal road, where AB = BC = 200 m. Angles *LAB* and *LBA* are 65° and 80° respectively (see diagram). Calculate

- (i) the shortest distance from L to the road,
- (ii) the distance LC.

4



The diagram shows a sketch of parts of the curves $y = \frac{16}{x^2}$ and $y = 17 - x^2$.

- (i) Verify that these curves intersect at the points (1, 16) and (4, 1).
- (ii) Calculate the exact area of the shaded region between the curves.

[1]

[7]

[4]

[3]

[4]

5 (i) Prove that the equation

 $\sin\theta\tan\theta = \cos\theta + 1$

can be expressed in the form

$$2\cos^2\theta + \cos\theta - 1 = 0.$$
 [3]

(ii) Hence solve the equation

$$\sin\theta\tan\theta = \cos\theta + 1,$$

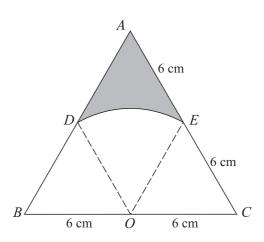
giving all values of θ between 0° and 360°.

6 (a) Find
$$\int x(x^2+2) dx$$
. [3]

(b) (i) Find
$$\int \frac{1}{\sqrt{x}} dx.$$
 [3]

(ii) The gradient of a curve is given by $\frac{dy}{dx} = \frac{1}{\sqrt{x}}$. Find the equation of the curve, given that it passes through the point (4, 0). [3]





The diagram shows an equilateral triangle ABC with sides of length 12 cm. The mid-point of BC is O, and a circular arc with centre O joins D and E, the mid-points of AB and AC.

- (i) Find the length of the arc *DE*, and show that the area of the sector *ODE* is 6π cm². [4]
- (ii) Find the exact area of the shaded region.

[Questions 8 and 9 are printed overleaf.]

[4]

[5]

- 8 (i) On a single diagram, sketch the curves with the following equations. In each case state the coordinates of any points of intersection with the axes.
 - (a) $y = a^x$, where *a* is a constant such that a > 1. [2]
 - (b) $y = 2b^x$, where b is a constant such that 0 < b < 1. [2]
 - (ii) The curves in part (i) intersect at the point P. Prove that the x-coordinate of P is

$$\frac{1}{\log_2 a - \log_2 b}.$$
[5]

9 A geometric progression has first term *a*, where $a \neq 0$, and common ratio *r*, where $r \neq 1$. The difference between the fourth term and the first term is equal to four times the difference between the third term and the second term.

(i) Show that
$$r^3 - 4r^2 + 4r - 1 = 0.$$
 [2]

- (ii) Show that r 1 is a factor of $r^3 4r^2 + 4r 1$. Hence factorise $r^3 4r^2 + 4r 1$. [3]
- (iii) Hence find the two possible values for the ratio of the geometric progression. Give your answers in an exact form. [2]
- (iv) For the value of r for which the progression is convergent, prove that the sum to infinity is $\frac{1}{2}a(1+\sqrt{5})$. [4]

BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (OCR) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

OCR is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.