# OXFORD CAMBRIDGE AND RSA EXAMINATIONS <br> <br> Advanced Subsidiary General Certificate of Education <br> <br> Advanced Subsidiary General Certificate of Education Advanced General Certificate of Education 

 Advanced General Certificate of Education}

## MATHEMATICS

## 2637

Mechanics 1
Friday 21 JANUARY 2005
Afternoon
1 hour 20 minutes
Additional materials:
Answer booklet
Graph paper
List of Formulae (MF8)

TIME 1 hour 20 minutes

## INSTRUCTIONS TO CANDIDATES

- Write your Name, Centre Number and Candidate Number in the spaces provided on the answer booklet.
- Answer all the questions.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- Where a numerical value for the acceleration due to gravity is needed, use $9.8 \mathrm{~m} \mathrm{~s}^{-2}$.
- You are permitted to use a graphic calculator in this paper.


## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [ ] at the end of each question or part question.
- The total number of marks for this paper is 60 .
- Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.
- You are reminded of the need for clear presentation in your answers.

1 Two small spheres $A$ and $B$, of masses 0.3 kg and 0.2 kg respectively, are moving on a smooth horizontal table and collide. Immediately before the collision $A$ and $B$ are moving directly towards each other with speeds $1.5 \mathrm{~m} \mathrm{~s}^{-1}$ and $2 \mathrm{~m} \mathrm{~s}^{-1}$ respectively. Immediately after the collision $A$ and $B$ move away from each other with speeds of $a \mathrm{~m} \mathrm{~s}^{-1}$ and $b \mathrm{~m} \mathrm{~s}^{-1}$ respectively.
(i) Show that $b=0.25+1.5 a$.

After the collision sphere $A$ travels a distance of 2 m in 4 s .
(ii) Find the values of $a$ and $b$.

2 A block of mass 3 kg is at rest on a rough horizontal plane.
(i) The block is acted on by a horizontal force of magnitude 14.7 N . Given that the block is on the point of sliding, find the coefficient of friction between the block and the plane.
(ii)


The horizontal force is now replaced by a force of magnitude $P \mathrm{~N}$ acting downwards at $30^{\circ}$ to the horizontal (see diagram). Given that the block is again on the point of sliding, find the value of $P$.


The diagram shows the magnitudes and directions of three coplanar forces which act at a point.
(i) Find the value of $P$ and the value of $x$ in degrees for which the forces are in equilibrium.
(ii) Find the magnitude of the resultant of the forces when $P=12$ and $x=45^{\circ}$.

4 A particle moves in a straight line. At time $t \mathrm{~s}$ the acceleration of the particle is $3 t^{\frac{1}{2}} \mathrm{~m} \mathrm{~s}^{-2}$. When $t=0$ the particle is at the point $O$, and when $t=9$ the particle is at the point $P$ and is moving with velocity $60 \mathrm{~m} \mathrm{~s}^{-1}$. Find
(i) the velocity of the particle at $O$,
(ii) the distance $O P$.

A cyclist travels along a straight road from the point $O$ to the point $A$ where he immediately turns round and returns directly to $O$. On the outward journey the cyclist starts from rest and accelerates uniformly for 20 s , reaching a speed of $9 \mathrm{~m} \mathrm{~s}^{-1}$. He then cycles at a constant speed of $9 \mathrm{~m} \mathrm{~s}^{-1}$ for 82 s before decelerating uniformly for 8 s , coming to rest instantaneously at $A$. On the return journey the cyclist accelerates at $0.5 \mathrm{~m} \mathrm{~s}^{-2}$ until his speed reaches $8 \mathrm{~m} \mathrm{~s}^{-1}$. He then cycles at a constant speed of $8 \mathrm{~m} \mathrm{~s}^{-1}$ until he reaches $O$.
(i) Sketch the $(t, v)$ graph for the cyclist's whole journey (outward and return).
(ii) Find the distance $O A$.
(iii) Find the total time taken for the whole journey.


A particle $A$ is projected vertically upwards from horizontal ground with speed $15 \mathrm{~m} \mathrm{~s}^{-1}$. At the same instant a particle $B$ is released from rest at a height $H \mathrm{~m}$ above the ground (see diagram).
(i) Find the height of $A$ after 0.8 s .
(ii) Find the value of $H$, given that $A$ and $B$ are at the same height after 0.8 s .
(iii) Show that the time interval between the instant that $B$ reaches the ground and the instant that $A$ returns to the ground is approximately 1.5 s .

## [Question 7 is printed overleaf.]



Particles $A$ and $B$, of masses 0.1 kg and 0.32 kg respectively, are attached to the ends of a light inextensible string. The string passes over a fixed smooth pulley at the top of a rough plane which is inclined at an angle $\alpha$ to the horizontal. It is given that $\sin \alpha=0.6$ and $\cos \alpha=0.8$. Particle $A$ is held in contact with the plane and particle $B$ hangs vertically below the pulley (see diagram). The coefficient of friction between $A$ and the plane is $\frac{1}{4}$. Particle $A$ is released and the system starts to move. Find
(i) the acceleration of $A$,
(ii) the distance travelled by $A$ when its speed has reached $2.8 \mathrm{~m} \mathrm{~s}^{-1}$ (assuming that $A$ has not reached the pulley).

When the speed is $2.8 \mathrm{~m} \mathrm{~s}^{-1}$ the string breaks. Particle $A$ continues to move up the plane without reaching the pulley.
(iii) Find the distance between the initial position of $A$ and the highest point reached by $A$.

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