GCE Examinations

Advanced Subsidiary / Advanced Level

Statistics
Module S1

Paper F

MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.

S1 Paper F – Marking Guide

1. *(a)* mean = $\frac{1145.3}{15}$ = 76.4 kg   M1 A1

variance = $\frac{88042.14}{15} - 76.353^2 = 39.6$ kg^2 M2 A1

(b) mean lower as replacement weighs less   B2

variance higher as replacement's weight further from mean   B2   **(9)**

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2. *(a)* $a + b + \frac{1}{4} + 2a + \frac{1}{8} = 1$ M1

$3a + b = \frac{5}{8}$; $b = \frac{5}{8} - 3a$ M1 A1

(b) $\sum x\text{P}(x) = a + 2b + \frac{3}{4} + 8a + \frac{5}{8}$ M1

$= 9a + 2(\frac{5}{8} - 3a) + \frac{11}{8} = 3a + \frac{21}{8}$ M1 A1

(c) $3a + \frac{21}{8} = \frac{45}{16}$ M1

$3a = \frac{45}{16} - \frac{21}{8} = \frac{3}{16}$ M1

$a = \frac{1}{16}$, $b = \frac{7}{16}$ A2   **(10)**

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3. *(a)* $\text{P}(Z < \frac{25 - 21.5}{2.2}) = \text{P}(Z < 1.59) = 0.9441$ M2 A1

(b) $\text{P}(Z > \frac{19 - 21.5}{2.2}) = \text{P}(Z > {}^-1.14) = 0.8729$ ∴ 87.3%   M2 A1

(c) $\text{P}(Z < \frac{20 - 21.5}{2.2}) = \text{P}(Z < {}^-0.68) = 0.2483$ M1 A1

P(2 of 3 < 20) = $3 \times 0.2483^2 \times 0.7517 = 0.139$ M2 A1   **(11)**

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4. *(a)* $0.76 = 0.5 + 0.42 - \text{P}(A \cap B)$ M1

$\text{P}(A \cap B) = 0.92 - 0.76 = 0.16$ M1 A1

(b) $(1 - 0.5) + 0.16 = 0.66$ M2 A1

(c) $= \frac{\text{P}(B \cap A')}{\text{P}(A')} = \frac{0.42 - 0.16}{1 - 0.5} = 0.52$ M2 A1

(d) $\text{P}(A) \times \text{P}(B) = 0.5 \times 0.42 = 0.21$ M1 A1

$\neq \text{P}(A \cap B)$ ∴ not independent   A1   **(12)**

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5. (a) $n = 31$, median $= 29$ A1
$Q_1 = 23$ A1
$Q_3 = 34$ A1
IQR $= Q_3 - Q_1 = 34 - 23 = 11$ M1 A1

(b) $Q_2 - Q_1 = 6$; $Q_3 - Q_2 = 5$ M1
$\therefore Q_2 - Q_1 > Q_3 - Q_2$ $\therefore$ slight +ve skew   M1 A1

(c) e.g. recommend mean and std. dev. as they take account of all
    values and there is little skew / few extreme values   B2

(d) $Q_1 - 2s = 2.4$; $Q_3 + 2s = 54.6$ $\therefore$ outliers are 0, 2   M1 A1

        B4   **(16)**

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6. (a)
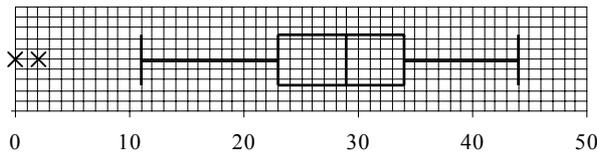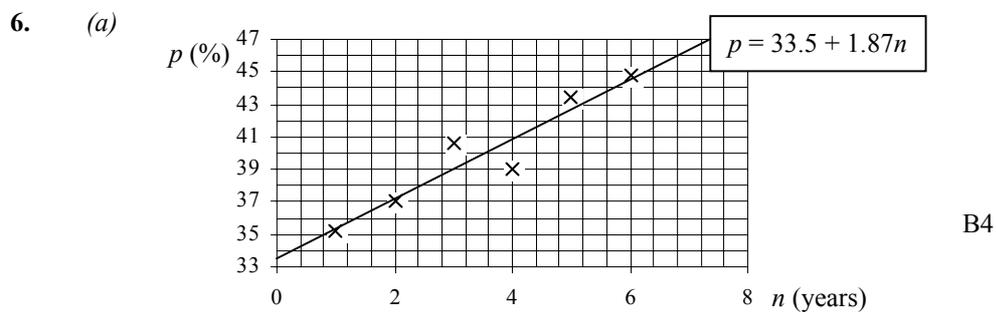
$p = 33.5 + 1.87n$

        B4

(b) $S_{np} = 873 - \dfrac{21 \times 240.1}{6} = 32.65$ M1

$S_{nn} = 91 - \dfrac{21^2}{6} = 17.5$ M1

$b = \dfrac{32.65}{17.5} = 1.8657$ M1 A1

$a = \dfrac{240.1}{6} - 1.8657 \times \dfrac{21}{6} = 33.4867$ M1 A1
$p = 33.5 + 1.87n$ A1
line on graph above   B2

(c) $S_{pp} = 9675.41 - \dfrac{240.1^2}{6} = 67.4083$ M1

$r = \dfrac{32.65}{\sqrt{17.5 \times 67.4083}} = 0.9506$ M1 A1

r strongly +ve supporting linear model   B1   **(17)**

Total   **(75)**

Performance Record – S1 Paper F

Question no.	1	2	3	4	5	6	Total
Topic(s)	mean, variance	discrete r. v.	normal dist.	probability	stem & leaf, quartiles, boxplot	scatter diagram, regression, pmcc	
Marks	9	10	11	12	16	17	75
Student							