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Turn over

1. Use integration by parts to find the exact value of $\int_{1}^{3} x^{2} \ln x \, dx$.

(6)

- 2. Fluid flows out of a cylindrical tank with constant cross section. At time t minutes, $t \ge 0$, the volume of fluid remaining in the tank is V m³. The rate at which the fluid flows, in m³ min⁻¹, is proportional to the square root of V.
 - (a) Show that the depth h metres of fluid in the tank satisfies the differential equation

$$\frac{\mathrm{d}h}{\mathrm{d}t} = -k\sqrt{h}, \qquad \text{where } k \text{ is a positive constant.}$$
(3)

(b) Show that the general solution of the differential equation may be written as

$$h = (A - Bt)^2$$
, where A and B are constants. (4)

Given that at time t = 0 the depth of fluid in the tank is 1 m, and that 5 minutes later the depth of fluid has reduced to 0.5 m,

(c) find the time, T minutes, which it takes for the tank to empty.

(3)

(d) Find the depth of water in the tank at time 0.5T minutes.

(2)

- 3. (a) Use the identity for $\cos (A + B)$ to prove that $\cos 2A = 2 \cos^2 A 1$. (2)
 - (b) Use the substitution $x = 2\sqrt{2} \sin \theta$ to prove that

$$\int_{2}^{\sqrt{6}} \sqrt{(8-x^2)} \, dx = \frac{1}{3}(\pi + 3\sqrt{3} - 6).$$
 (7)

A curve is given by the parametric equations

$$x = \sec \theta$$
, $y = \ln(1 + \cos 2\theta)$, $0 \le \theta < \frac{\pi}{2}$.

(c) Find an equation of the tangent to the curve at the point where $\theta = \frac{\pi}{3}$.

(5)

4. Figure 2

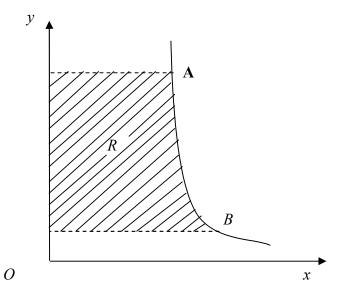


Figure 2 shows a sketch of the curve C with equation $y = \frac{4}{x-3}$, $x \ne 3$.

The points *A* and *B* on the curve have *x*-coordinates 3.25 and 5 respectively.

(a) Write down the y-coordinates of A and B.

(1)

(b) Show that an equation of C is
$$\frac{3y+4}{y}$$
, $y \neq 0$.

(1)

The shaded region R is bounded by C, the y-axis and the lines through A and B parallel to the x-axis. The region R is rotated through 360° about the y-axis to form a solid shape S.

(c) Find the volume of S, giving your answer in the form $\pi(a + b \ln c)$, where a, b and c are integers.

(7)

The solid shape S is used to model a cooling tower. Given that 1 unit on each axis represents 3 metres,

(d) show that the volume of the tower is approximately 15500 m^3 .

(2)

5.	Relative to a fixed origin O , the point A has position vector $3\mathbf{i} + 2\mathbf{j} - \mathbf{k}$, the point B has position vector $5\mathbf{i} + \mathbf{j} + \mathbf{k}$, and the point C has position vector $7\mathbf{i} - \mathbf{j}$.							
	(a) Find the cosine of angle ABC.	(4)						
	(b) Find the exact value of the area of triangle ABC.	(4)						
	The point D has position vector $7\mathbf{i} + 3\mathbf{k}$.							
	(c) Show that AC is perpendicular to CD.	(2)						
	(d) Find the ratio AD:DB.	(2)						

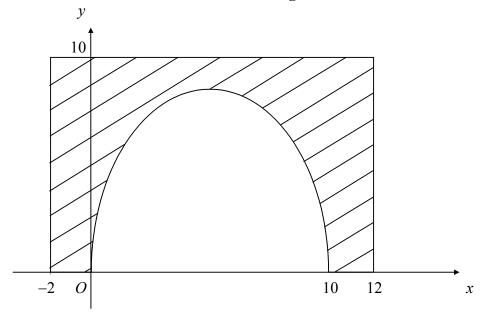


Figure 2 shows the cross-section of a road tunnel and its concrete surround. The curved section of the tunnel is modelled by the curve with equation $y = 8\sqrt{\sin\frac{\pi x}{10}}$, in the interval $0 \le x \le 1$

10. The concrete surround is represented by the shaded area bounded by the curve, the x-axis and the lines x = -2, x = 12 and y = 10. The units on both axes are metres.

(a) Using this model, copy and complete the table below, giving the values of y to 2 decimal places.

х	0	2	4	6	8	10
y	0	6.13				0

(2)

The area of the cross-section of the tunnel is given by $\int_{0}^{10} y \, dx$.

(b) Estimate this area, using the trapezium rule with all the values from your table.

(4)

(c) Deduce an estimate of the cross-sectional area of the concrete surround.

(1)

(d) State, with a reason, whether your answer in part (c) over-estimates or under-estimates the true value.

(2)

7. $f(x) = \frac{25}{(3+2x)^2(1-x)}, |x| < 1.$

(a) Express f(x) as a sum of partial fractions. (4)

(b) Hence find $\int f(x) dx$.

(5)

(c) Find the series expansion of f(x) in ascending powers of x up to and including the term in x^2 . Give each coefficient as a simplified fraction.

(7)

END