

6. The circle C , with centre A , has equation

$$x^2 + y^2 - 6x + 4y - 12 = 0.$$

(a) Find the coordinates of A . (2)

(b) Show that the radius of C is 5. (2)

The points P , Q and R lie on C . The length of PQ is 10 and the length of PR is 3.

(c) Find the length of QR , giving your answer to 1 decimal place. (3)

10.

Figure 2

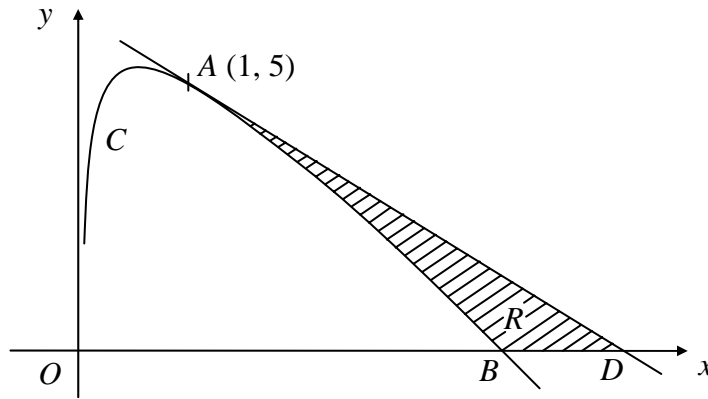


Figure 2 shows part of the curve C with equation

$$y = 9 - 2x - \frac{2}{\sqrt{x}}, \quad x > 0.$$

The point $A(1, 5)$ lies on C and the curve crosses the x -axis at $B(b, 0)$, where b is a constant and $b > 0$.

(a) Verify that $b = 4$. (1)

The tangent to C at the point A cuts the x -axis at the point D , as shown in Fig. 2.

(b) Show that an equation of the tangent to C at A is $y + x = 6$. (4)

(c) Find the coordinates of the point D . (1)

The shaded region R , shown in Fig. 2, is bounded by C , the line AD and the x -axis.

(d) Use integration to find the area of R . (6)
