## Pearson

## Mark Scheme (Results)

## Summer 2017

Pearson Edexcel International A Level in Further Pure Mathematics F1 (WFM01/01)

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## General Marking Guidance

All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.

- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## PEARSON EDEXCEL IAL MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 75
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.


## 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- o.e. - or equivalent (and appropriate)
- d... or dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper or ag- answer given
- $\square$ or d... The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any $A$ or $B$ marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.

## General Principles for Further Pure Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

## Method mark for solving 3 term quadratic:

## 1. Factorisation

$\left(x^{2}+b x+c\right)=(x+p)(x+q)$, where $|p q|=|c|$, leading to $\mathrm{x}=\ldots$
$\left(a x^{2}+b x+c\right)=(m x+p)(n x+q)$, where $|p q|=|c|$ and $|m n|=|a|$, leading to $\mathrm{x}=\ldots$

## 2. Formula

Attempt to use the correct formula (with values for $a, b$ and $c$ ).

## 3. Completing the square

Solving $x^{2}+b x+c=0:\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c=0, q \neq 0$, leading to $\mathrm{x}=\ldots$

## Method marks for differentiation and integration:

## 1. Differentiation

Power of at least one term decreased by 1. $\left(x^{n} \rightarrow x^{n-1}\right)$

## 2. Integration

Power of at least one term increased by 1. $\left(x^{n} \rightarrow x^{n+1}\right)$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

Method mark for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.

Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

May 2017
WFM01 Further Pure Mathematics F1 Mark Scheme



| Question <br> Number | Scheme |  | Notes |  | Marks |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3. | Required to prove by induction the resu | result ${ }_{r=1}^{n} \overline{r(r+1)}$ | $\frac{2}{+1)(r+2)}=\frac{1}{2}$ | $\frac{1}{(n+1)(n+2)}, n \rightarrow$ |  |
| Way 1 | $n=1: \text { LHS }=\frac{1}{3}, \text { RHS }=\frac{1}{2} \quad \frac{1}{(2)(3)}=\frac{1}{3}$ | $=\frac{1}{3} \quad$ and | shows either RH $\mathrm{HS}=\frac{1}{2} \quad \frac{1}{(2)(3)}=$ | $\begin{aligned} & \text { Shows or states LHS }=\frac{1}{3} \\ & \text { SS }=\frac{1}{2} \quad \frac{1}{(1+1)(2+1)}=\frac{1}{3} \\ & =\frac{1}{3} \text { or RHS }=\frac{1}{2} \quad \frac{1}{6}=\frac{1}{3} \end{aligned}$ | B1 |
|  | (Assume the result is true for $n=k$ ) |  |  |  |  |
|  | ${ }_{r=1}^{k+1} \frac{2}{r(r+1)(r+2)}=\frac{1}{2} \quad \frac{1}{(k+1)(k+2)}+\frac{2}{(k+1)(k+1+1)(k+1+2)}$ |  |  | Adds the $(k+1)^{\text {th }}$ term to the sum of $k$ terms | M1 |
|  | $=\frac{1}{2} \frac{1}{(k+1)(k+2)}+\frac{2}{(k+1)(k+2)(k+3)}$ |  |  |  |  |
|  | $=\frac{1}{2} \quad \frac{(k+3)}{(k+1)(k+2)(k+3)}+\frac{2}{(k+1)(k+2)(k+3)}$ <br> or $=\frac{1}{2}\left(\frac{(k+3) 2}{(k+1)(k+2)(k+3)}\right)$ |  | dependent on the previous $M$ mark Makes $(k+1)(k+2)(k+3)$ a common <br> denominator for their second and third fractions |  | dM1 |
|  | $=\frac{1}{2} \quad \frac{1}{(k+2)(k+3)}$ | Obtains $\frac{1}{2} \frac{1}{(k+2)(k+3)}$ or $\frac{1}{2} \frac{1}{(k+1+1)(k+1+2)}$ |  |  | A1 |
|  | If the result is true for $n=k$, then it is true for $n=k+1$. As the result has been shown to be true for $n=1$, then the result is true for all $n$ ( ${ }^{\rightarrow}$ ) |  |  |  | A1 cso |
|  | Final A1 is dependent on all previous marks being scored in that part. It is gained by candidates conveying the ideas of all four underlined points either at the end of their solution or as a narrative in their solution. |  |  |  | (5) |
|  |  |  |  |  | 5 |
| Way 2 | The M1dM1A1 marks for Alternative Way 2 |  |  |  |  |
|  | ${ }_{r=1}^{k+1} \frac{2}{r(r+1)(r+2)}=\frac{1}{2} \quad \frac{1}{(k+1)(k+2)}+\frac{2}{(k+1)(k+1+1)(k+1+2)}$ |  |  | Adds the $(k+1)^{\text {th }}$ term to the sum of $k$ terms | M1 |
|  | $=\frac{(k+1)(k+2)(k+3) 2(k+3)+2(2)}{2(k+1)(k+2)(k+3)}$ |  | dependent on the previous $M$ mark Makes $2(k+1)(k+2)(k+3)$ a common denominator for their three fractions |  | dM1 |
|  | $=\frac{k^{3}+6 k^{2}+9 k+4}{2(k+1)(k+2)(k+3)}=\frac{(k+1)\left(k^{2}+5 k+4\right)}{2(k+1)(k+2)(k+3)}=\frac{k^{2}+5 k+4}{2(k+2)(k+3)}=\frac{(k+2)(k+3) 2}{2(k+2)(k+3)}$ |  |  |  |  |
|  | $=\frac{1}{2} \frac{1}{(k+2)(k+3)}$ | Obtains $\frac{1}{2} \frac{1}{(k+2)(k+3)}$ or $\frac{1}{2} \frac{1}{(k+1+1)(k+1+2)}$ <br> by correct solution only |  |  | A1 |


| 3. | Question 3 Notes |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Note | LHS $=$ RHS by itself or LHS $=$ RHS $=\frac{1}{3}$ is not sufficient for the $1^{\text {st }} \mathrm{B} 1$ mark. |  |  |  |  |  |  |  |
|  | Note Way 2 | The $1^{\text {st }} \mathrm{A} 1$ can be obtained by e.g. using algebra to show that ${ }_{r=1}^{k+1} \frac{2}{r(r+1)(r+2)}$ $\frac{\left(k^{2}+5 k+4\right)}{2(k+2)(k+3)}$ and by using algebra to show that $\frac{1}{2} \frac{1}{(k+2)(k+3)}$ also gives |  |  |  |  |  |  | es $\frac{\left.2^{2}+5 k+4\right)}{+2)(k+3)}$ |
|  | Note | Moving from $\frac{1}{2} \frac{1}{(k+1)(k+2)}+\frac{2}{(k+1)(k+2)(k+3)}$ to $\frac{1}{2} \quad \frac{1}{(k+2)(k+3)}$ with no intermediate working is $2^{\text {nd }} \mathrm{M} 01^{\text {st }} \mathrm{A} 02^{\text {nd }} \mathrm{A} 0$. |  |  |  |  |  |  |  |
| Way 3 | The M1dM1A1 marks for Alternative Way 3 |  |  |  |  |  |  |  |  |
|  | ${ }_{r=1}^{k+1} \frac{2}{r(r+1)(r+2)}=\frac{1}{2} \quad \frac{1}{(k+1)(k+2)}+\frac{2}{(k+1)(k+1+1)(k+1+2)}$ |  |  |  |  |  | Adds the to the su | $(k+1)^{\text {th }}$ term <br> of $k$ terms | M1 |
|  | $=\frac{1}{2} \quad \frac{}{(k+1}$ | $\frac{1}{+1)(k+2)}+\frac{1}{(k+1)(k+2)}$ | $\frac{1}{(k+2)(k+3}$ |  | dependent on the previous M mark This step must be seen in Way 3 |  |  |  | dM1 |
|  | $=\frac{1}{2} \quad$ | $\frac{1}{(k+2)(k+3)}$ | Obtains $\frac{1}{2} \frac{1}{(k+2)(k+3)}$ or $\frac{1}{2} \frac{1}{(k+1+1)(k+1+2)} \begin{array}{r}\text { by correct solution only }\end{array}$ |  |  |  |  |  | A1 |


| Question <br> Number | Scheme | Notes |  | Marks |
| :---: | :---: | :---: | :---: | :---: |
| 4. (a) <br> Way 1 | $\left\{x=4 t, y=\frac{4}{t} \Rightarrow\right\} 3\left(\frac{4}{t}\right) \quad 2(4 t)=10$ | Substitutes $x=4 t$ and $y=\frac{4}{t}$ into the printed equation to obtain an equation in $t$ only |  | M1 |
|  | $\begin{array}{cc} 8 t^{2}+10 t \quad 12=0 \text { or } 4 t^{2}+5 t \quad 6=0 \\ & (\text { can be implied }) \end{array}$ | A correct 3 term quadratic <br> Note: E.g. $12 \quad 8 t^{2}=10 t, 8 t^{2}+10 t \quad 12\{=0\}$ or $8 t^{2}+10 t=12$ are acceptable for this mark |  | A1 |
|  | $\begin{array}{ll} \left.\quad \begin{array}{ll} 8 t & 6 \end{array}\right)(t+2)=0 & t=\ldots \\ \text { or }\left(\begin{array}{ll} 4 t & 3 \end{array}\right)(2 t+4)=0 & t=\ldots \\ \text { or }\left(\begin{array}{ll} 4 t & 3 \end{array}\right)(t+2)=0 & t=\ldots \end{array}$ | dependent on the previous M mark Correct method (e.g. factorising, completing the square or applying the quadratic formula) of solving a 3 TQ to find $t=\ldots$ |  | dM1 |
|  | - $x=4\left(\frac{3}{4}\right)=3$ and $y=\frac{4}{\left(\frac{3}{4}\right)}=\frac{16}{3}$ <br> - $x=4(2)=8$ and $y=\frac{4}{(2)}=2$ | dependent on both the previous $M$ marks Correct substitution at least one of their values for $t$ into the given parametric equations and obtains two sets of corresponding values for $x=\ldots$ and $y=\ldots$ |  | ddM1 |
|  | $A\left(3, \frac{16}{3}\right), B(8,2)$ or $A: x=3, y=\frac{16}{3}$ and $B: x=8, y=2$ ( $\begin{array}{r}\text { Identifies the correct } \\ \text { coordinates for } A \text { and } B\end{array}$ |  |  | A1 cao |
|  |  |  |  | (5) |
| (a) Way 2 | $\left.\begin{array}{l\|l}x\left(\frac{10+2 x}{3}\right)=16 & \left(\frac{3 y}{2} 10\right. \\ \hline\end{array}\right) y=16$ | Either substitutes their rearranged <br> $3 y \quad 2 x=10$ into $x y=k$ or substitutes either $y=\frac{k}{x} \text { or } x=\frac{k}{y}, k \quad 0, \text { into } 3 y \quad 2 x=10$ <br> to form an equation in either $x$ only or $y$ only |  | M1 |
|  | $\left.\begin{array}{lll} 2 x^{2}+10 x & 48=0 \text { or } x^{2}+5 x & 24=0 \text { or } \\ \frac{2}{3} x^{2}+\frac{10}{3} x & 16=0 \text { or } \frac{3}{2} y^{2} & 5 y \end{array} \quad 16=00 \text { (can be implied }\right) \text { }$ | A correct 3 term quadratic <br> Note: $10 x+2 x^{2}=48,3 y^{2} \quad 10 y=32$ or $x^{2}+5 x \quad 24\{=0\}$ are acceptable for this mark |  | A1 |
|  |  | dependent on the previous M mark Correct method (e.g. factorising, completing the square or applying the quadratic formula) of solving a 3TQ to find either $x=\ldots$ or $y=\ldots$ |  | dM1 |
|  | E.g. $\quad x=3 \quad y=\frac{16}{3}$ dependent on both the previous M marks. Correct substitution <br> of at least one of their values for $x$ or $y$ into either $3 y \quad 2 x=10$ or <br> $x=8 \quad y=\frac{16}{8}=2$ their rearranged $3 y \quad 2 x=10$ or $y=\frac{k}{x}$ or $x=\frac{k}{y}, k \quad 0$, and <br> obtains two sets of corresponding values for $x=\ldots$ and $y=\ldots$ |  |  | ddM1 |
|  | $A\left(3, \frac{16}{3}\right), B(8,2)$ or $A: x=3, y=\frac{16}{3}$ and $B: x=8, y=2$ ( $\begin{array}{r}\text { Identifies the correct } \\ \text { coordinates for } A \text { and } B\end{array}$ |  |  | A1 cao |
|  |  |  |  | (5) |
| (b) | $\left(\frac{3+(8)}{2}, \frac{\frac{16}{3}+(2)}{2}\right) ;=\left(\frac{5}{2}, \frac{5}{3}\right)$ | Uses their $\left(x_{1}, y_{1}\right)$ and $\left(x_{2}, y_{2}\right)$ from part (a) to apply $\left(\frac{x_{1}+x_{2}}{2}, \frac{y_{1}+y_{2}}{2}\right)$ o.e. <br> Correct answer |  | M1; |
|  |  |  |  | A1 |
|  |  |  |  | (2) |
|  |  |  |  | 7 |


|  | Question 4 Notes |  |
| :---: | :---: | :---: |
| 4. (a) | SC | If the two previous M marks have been gained then award Special Case ddM1 for finding their correct points by writing either $x=3, y=\frac{16}{3}$ or $x=8, y=2$ or $\left(3, \frac{16}{3}\right)$ or $(8,2)$ |
|  | Note | A decimal answer of e.g. $A(3,5.33), B(8,2)$ (without a correct exact answer) is $2^{\text {nd }} \mathrm{A} 0$ |
|  | Note | Writing coordinates the wrong way round E.g. writing $x=3, y=\frac{16}{3}$ and $x=8, y=2$ followed by $A\left(\frac{16}{3}, 3\right), B(8,2)$ is $2^{\text {nd }} \mathrm{A} 0$ |
|  | Note | Imply the dM 1 mark for writing down the correct roots for their quadratic equation. E.g. <br> - $2 x^{2}+10 x \quad 48=0$ or $x^{2}+5 x \quad 24=0$ or $\frac{2}{3} x^{2}+\frac{10}{3} x=16 \rightarrow x=3,8$ <br> - $\frac{3}{2} y^{2} \quad 5 y \quad 16=0$ or $3 y^{2} \quad 10 y \quad 32=0 \rightarrow y=\frac{16}{3}, 2$ <br> - $8 t^{2}+10 t=12$ or $4 t^{2}+5 t \quad 6=0 \rightarrow t=\frac{3}{4}, \quad 2$ |
|  | Note | For example, give dM0 for <br> - $8 t^{2}+10 t=12$ or $4 t^{2}+5 t \quad 6=0 \rightarrow t=\frac{1}{4}, \quad 2$ [incorrect solution] with no intermediate working. |
|  | Note | You can also imply the $1^{\text {st }} \mathrm{A} 1 \mathrm{dM} 1$ marks for either <br> - $x\left(\frac{10+2 x}{3}\right)=16$ or $3\left(\frac{16}{x}\right) \quad 2 x=10 \rightarrow x=3,8$ <br> - $\left(\frac{3 y 10}{2}\right) y=16$ or $3 y \quad 2\left(\frac{16}{y}\right)=10 \rightarrow y=\frac{16}{3}, 2$ <br> - $3\left(\frac{4}{t}\right) \quad 2(4 t)=10 \rightarrow x=3,8$ <br> - $3\left(\frac{4}{t}\right) \quad 2(4 t)=10 \rightarrow y=\frac{16}{3}, 2$ <br> with no intermediate working. |
|  | Note | You can imply the $1^{\text {st }} \mathrm{A} 1 \mathrm{dM} 1$ ddM1 marks for either <br> - $x\left(\frac{10+2 x}{3}\right)=16$ or $3\left(\frac{16}{x}\right) \quad 2 x=10 \rightarrow x=3,8$ and $y=\frac{16}{3}, \quad 2$ <br> - $3\left(\frac{4}{t}\right) \quad 2(4 t)=10 \rightarrow x=3,8$ and $y=\frac{16}{3}, 2$ <br> with no intermediate working. <br> You can then imply the final A1 mark if they correctly identify the correct pairs of values or coordinates which relate to the point $A$ and the point $B$. |
|  | Note | Give $2^{\text {nd }} \mathrm{A} 0$ for a final answer of both $A\left(3, \frac{16}{3}\right), B(8,2)$ and $A(8,2), B\left(3, \frac{16}{3}\right)$, |
| (b) | Note | A decimal answer of e.g. ( $2.5,1.67$ ) (without a correct exact answer) is A0 |
|  | Note | Allow A1 for $\left(\frac{5}{2}, \frac{10}{6}\right)$ or $\left(2 \frac{1}{2}, 1 \frac{2}{3}\right)$ or exact equivalent. |



|  |  | Question 5 Notes Continued |
| :---: | :---: | :---: |
| 5. (b) | Note | Incorrect differentiation followed by their estimate of with no evidence of applying the NR formula is final dM0A0. |
|  | Final <br> dM1 | This mark can be implied by applying at least one correct value of either f(2) or f (2) in $2 \frac{f(2)}{f(2)}$. So just $2 \frac{f(2)}{f(2)}$ with an incorrect answer and no other evidence scores final dM0A0. |
|  | Note | You can imply the M1A1A1 marks for algebraic differentiation for either <br> - $\mathrm{f}(2)=\frac{7}{2}(2)^{\frac{3}{2}} 5(2)^{4}$ <br> - f (2)applied correctly in $\alpha \simeq 2-\frac{30-7(2)^{-\frac{1}{2}}-(2)^{5}}{-\frac{7}{2}(2)^{-\frac{3}{2}}-5(2)^{4}}$ |
|  | Note | Differentiating INCORRECTLY to give $\mathrm{f}(x)=\frac{7}{2} x^{2} \quad 5 x^{4}$ leads to $\alpha \simeq 2-\frac{2.949747468 \ldots}{-81.75}=2.036082538 \ldots=2.04(2 \mathrm{dp})$ <br> This response should be awarded M1A1A0M1A0 |


| Question Number | Scheme | Notes | Marks |
| :---: | :---: | :---: | :---: |
| 6. (a) | ${ }_{r=1}^{n} r^{2}(r+1)={ }_{r=1}^{n} r^{3}+{ }_{r=1}^{n} r^{2}$ | $\left\{\right.$ Note: Let $\mathrm{f}(n)=\frac{1}{12} n(n+1)(n+2)(3 n+1)$ or their answer to part (a).\} |  |
|  | $=\frac{1}{4} n^{2}(n+1)^{2}+\frac{1}{6} n(n+1)(2 n+1)$ | Attempts to expand $r^{2}(r+1)$ and attempts to substitute at least one correct standard formula into their resulting expression. | M1 |
|  |  | Correct expression (or equivalent) | A1 |
|  | $=\frac{1}{12} n(n+1)[3 n(n+1)+2(2 n+1)] \quad$ At | dependent on the previous $M$ mark Attempt to factorise at least $n(n+1)$ having attempted to substitute both standard formulae. | dM1 |
|  | $=\frac{1}{12} n(n+1)\left[3 n^{2}+7 n+2\right]$ | \{this step does not have to be written\} |  |
|  | $=\frac{1}{12} n(n+1)(n+2)(3 n+1)$ | Correct completion with no errors. <br> Note: $a=12, b=1$ | A1 cso |
|  |  |  | (4) |
| $\begin{gathered} (\mathrm{b}) \\ \text { Way } 1 \end{gathered}$ | $\begin{aligned} & \left\{\sum_{r=25}^{49} r^{2}(r+1)\right\} \\ & =\left(\frac{1}{12}(49)(50)(51)(148)\right) \quad\left(\frac{1}{12}(24)(25)(26)(73)\right) \\ & \{=1541050 \quad 94900=1446150\} \end{aligned}$ | Attempts to find either <br> $f(49) \quad f(24)$ or $f(49) \quad f(25)$. <br> This mark can be implied. | M1 |
|  |  | Correct numerical expression for $f(49) \quad f(24)$ which can be simplified or un-simplified. Note: This mark can be implied by seeing 1446150 | A1 |
|  | $\begin{aligned} & \left\{\sum_{r=25}^{49}\left(r^{2}(r+1)+2\right)\right\}^{\prime 2} \\ & =" 1446150 "+25(2) ;=1446200 \end{aligned}$ | Adds 25(2) or equivalent to their ${ }_{r=25}^{r^{2}(r+1)}$ or clear evidence that ${ }_{r=25}^{49} 2=2(49)$ $2(24)$ or 50 | M1 |
|  |  | 1446200 | A1 cao |
|  |  |  | (4) |
| (b) <br> Way 2 | $\left.\begin{array}{rl} \left\{\sum_{r=25}^{49}\left(r^{2}(r+1)+2\right)\right\} & =\left(\underline{\underline{\frac{1}{12}}(49)(50)(51)(148)}+\underline{2(49)}\right) \quad(\underline{\underline{1}}(24)(25)(26)(73) \end{array}+\underline{2(24)}\right)$ |  |  |
|  | Attempts to find either $\underline{\underline{f(49)}} \mathrm{f}(24)$ or $\underline{\underline{f(49)} \mathrm{f}(25)}$ |  | M1 |
|  | Correct numerical expression for $f(49) \quad f(24)$ which can be simplified or un-simplified. <br> Note: This mark can be implied by ( $\underline{\underline{1541050}+\ldots) \quad(\underline{\underline{94900}}+\ldots) \text { or } 154114894948) ~}$ |  | A1 |
|  | Adds 50 or equivalent to their ${ }_{r=25}^{49} r^{2}(r+1)$ or clear evidence that ${ }_{r=25}^{49} 2=2(49) \quad 2(24)$ or 50 <br> Note: This mark can be implied by ( $\ldots+2(49)$ ) (... $+2(24))$ or 154114894948 |  | M1 |
|  | 1446200 |  | A1 cao |
|  |  |  | (4) |
|  |  |  | 8 |



|  | Question 6 Notes Continued |  |
| :---: | :---: | :---: |
| 6. (b) | Note | Give $1^{\text {st }} \mathrm{M} 11^{\text {st }}$ A0 for applying $\mathrm{f}(49) \quad \mathrm{f}(25)$. i.e. $1541050 \quad 111150\{=1429900\}$ |
|  | Note | You cannot follow through their incorrect answer from part (a) for the $1^{\text {st }} \mathrm{A} 1$ mark. |
|  | Note | $\begin{aligned} & \text { Give M1A0M1A0 for applying }[\mathrm{f}(49)+2(49)][\mathrm{f}(25)+2(24)] \\ & \text { i.e. } 1541148 \quad 111198\{=1429950\} \end{aligned}$ |
|  | Note | $\begin{aligned} & \text { Give M1A0M0A0 for applying }[\mathrm{f}(49)+2(49)] \quad[\mathrm{f}(25)+2(25)] \\ & \text { i.e. } 1541148 \quad 111200\{=1429948\} \end{aligned}$ |
|  | Note | Give $1^{\text {st }} \mathrm{M} 01^{\text {st }} \mathrm{A} 0$ for applying (49) ${ }^{2}(50) \quad(24)^{2}(25)=120050 \quad 14400=105650$ |
|  | Note | Give $1^{\text {st }} \mathrm{M} 01^{\text {st }} \mathrm{A} 0$ for applying $(49)^{2}(50) \quad(25)^{2}(26)=120050 \quad 16250=103800$ |
|  | Note | Give M0A0M0A0 for listing individual terms. $\text { e.g. } 16250+18252+\ldots+112896+120050=1446200$ |
|  | Note | Give $2^{\text {nd }} \mathrm{M} 0$ for lack of bracketing in $\frac{1}{12}(49)(50)(51)(148)+2(49) \quad \frac{1}{12}(24)(25)(26)(73)+2(24) \text { unless recovered }$ |
|  | Note | Give M0A0M0A0 for writing down 1446200 without any working. |
|  | Note | Applying f(49) $\mathrm{f}(24)$ for $\frac{1}{4} n(n+1)(n+2)(3 n+1)$ is $4623150 \quad 284700=4338450$ is $1^{\text {st }} \mathrm{M} 11^{\text {st }} \mathrm{A} 0$ |
|  |  |  |
|  |  |  |





|  | Question 9 Notes |  |  |
| :---: | :---: | :--- | :---: |
| 9. (a) | Note | M1 can be implied by awrt 0.45 or a truncated 0.44 |  |
|  | Note | Give A0 for $0.4472 \ldots$ without reference to $\frac{\sqrt{5}}{5}$ or $\frac{1}{\sqrt{5}}$ or $\sqrt{\frac{1}{5}}$ |  |
|  | Note | Give B0 for 1.11 followed by a final answer of 1.11 |  |
| (b) | Note | Be aware that $\frac{1}{\left(\frac{1}{5} \frac{2}{5} \mathrm{i}\right)}=1+2 \mathrm{i}$ |  |



