## edexcel

Mark Scheme (Results)
Summer 2015

Pearson Edexcel International A Level in Decision Mathematics 1
(WDM01/01)

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## PEARSON EDEXCEL I AL MATHEMATI CS

## General Instructions for Marking

1. The total number of marks for the paper is 75
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of $M$ marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- d... or dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper or ag- answer given
- $\square$ or d... The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any $A$ or $B$ marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.


## Notes for Question 1

a1M1: A larger value replaced by a smaller value at least once in the working values at either C or E or F or G or H
a1A1: All values in S, A, B, D and C correct. The working values at C must be in the correct order.
Condone lack of 0 in S's working value
a2A1: All values in F and E correct and the working values in the correct order. Penalise order of labelling only once per question ( F and E must be labelled in that order and F must be labelled after $\mathrm{S}, \mathrm{A}, \mathrm{B}, \mathrm{D}$ and C)
a3A1ft: All values in H and G correct on the follow through and the working values in the correct order. Penalise order of labelling only once per question ( H and G must be labelled in that order and H labelled after all other nodes (excluding G))
a4A1ft: If their answer is not 23 follow through their final value at $G$ (condone lack of units)
a5A1: CAO for the route ( $\mathrm{S}-\mathrm{A}-\mathrm{C}-\mathrm{F}-\mathrm{G}$ )
b1B1ft: If their answer is not 20 follow through their final value at H (condone lack of units)
b2B1: CAO for the route ( $\mathrm{S}-\mathrm{A}-\mathrm{C}-\mathrm{F}-\mathrm{E}-\mathrm{H}$ )


| Question |  |  |
| :---: | :---: | :---: |
| Number | Scheme | Marks |

## Sorting list into ascending order in (c)

- If the candidate sorts the list into ascending order and reverses the list then they can score full marks
- If the list is not reversed then mark as a misread. If the candidate says that the list needs reversing but doesn't actually show the reversed list then remove the final A mark earned
Misreads - if there is a 'misread' of a single number (this could take the form of an extra number, a number missing, or a number changed, for example, 31 rather than 13) before starting the sort in (c) then mark as a misread. If they 'misread' more than one number then M0. If they miscopy one of their own numbers during the sort then this is an accuracy error and loses the corresponding A mark(s)

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 3.(a) | e.g. P-Q - S - P | B1 (1) |
| (b) | As vertex Q appears more than once... ... $\mathrm{P}-\mathrm{Q}-\mathrm{R}-\mathrm{T}-\mathrm{Q}-\mathrm{S}$ is not an example of a path on G | $\begin{align*} & \text { B1 }  \tag{2}\\ & \text { DB1 } \end{align*}$ |
| (c) | PS, ST, SV; QS, QR; RU, TW | $\begin{array}{r} \text { M1; A1; A1 } \\ \text { (3) } \\ \hline \end{array}$ |
| (d) | ST SV PS QS (not QT) QR (not PQ) (not TV) RU TW | M1 A1 A1 |
| (e) |  | B1 (1) |
| (f) | $20<x<31$ | $\begin{aligned} & \begin{array}{l} \mathrm{B} 2,1,0 \quad(2) \\ \text { (12 marks) } \end{array} \end{aligned}$ |
| Notes for Question 3 |  |  |

a1B1: Any closed path on $G$ (must begin and end with the same vertex) - check that no vertex (except the start and end vertex) appears more than once
b1B1: No + attempt at a reason - any mention of cycle/circle/loop etc. or repeated vertex/node/point etc. is sufficient for this mark (condone incorrect technical language) - give bod
b2DB1: No + correct reason - no bod - must refer to vertex Q appearing twice (in the walk - not just that a vertex is repeated) or that it contains the cycle $\mathrm{Q}-\mathrm{R}-\mathrm{T}-\mathrm{Q}$ (not just that it contains a cycle). All technical language must be correct for this mark
c1M1: Prim's - First three arcs correctly chosen in order (PS, ST, SV, ... or weights $13,9,11, \ldots$ ) or first four nodes $\{\mathrm{P}, \mathrm{S}, \mathrm{T}, \mathrm{V}, \ldots\}$ correctly chosen in order. If any rejections seen at some point then M1 (max) only. Order of nodes may be seen at the top of a matrix/table $\{1,-,-, 2,3,-, 4,-\}$
c1A1: First five arcs correctly chosen in order (PS, ST, SV, QS, QR, $\ldots$ or weights $13,9,11,14,16, \ldots$ ) or all eight nodes $\{\mathrm{P}, \mathrm{S}, \mathrm{T}, \mathrm{V}, \mathrm{Q}, \mathrm{R}, \mathrm{U}, \mathrm{W}\}$ correctly chosen in order. Order of nodes may be seen at the top of a matrix so for the first two marks accept $\{1,5,6,2,3,7,4,8\}$ (no missing numbers)
c2A1: CSO - all arcs correctly stated and chosen in the correct order. They must be considering arcs for this final mark (do not accept a list of the weights of each arc, nodes or numbers across the top of the matrix unless the correct list of arcs (in the correct order) is also seen)

Misread: Starting at a node other than P scores M1 only - must have the first three arcs (or four nodes or numbers) correct (and in the correct order) - condone rejections seen for this mark

| Question |  |  |
| :--- | :---: | :---: |
| Number | Scheme | Marks |
| d1M1: K. |  |  |

d1M1: Kruskal's - first four arcs (ST, SV, PS, QS, ... or weights $9,11,13,14, \ldots$ ) chosen correctly in order and at least one rejection seen at some point
d1A1: All seven arcs (ST, SV, PS, QS, QR, RU, TW or weights $9,11,13,14,16,20,24$ ) chosen correctly in order and no additional arcs
d2A1: CSO - all selections and rejections correct (in correct order and at the correct time) - do not accept weights only for this mark

- Listing all the arcs in order and then listing those arcs in the tree in the correct order is fine for full marks (this implies that rejections are correct and at the correct time)
- Listing all the arcs in order and just drawing the MST is M0
e1B1: CAO (condone lack of/incorrect weights on arcs)
f1B1: $x<31$ or $x \leq 31$ or $x<30$ or $x \leq 30$
f2B1: Either $20<x<31$ or $21 \leq x \leq 30$

| Question Number | Scheme |  |  |  |  |  | Marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4.(a) | A path from an unmatched vertex in one set to an unmatched vertex in the other set... <br> ...which alternately uses arcs not in/in the matching |  |  |  |  |  | $\begin{aligned} & \mathrm{B} 1 \\ & \mathrm{~B} 1 \end{aligned}$ |
| (b) | Initial matching: $\mathrm{A}=3, \mathrm{~B}=2, \mathrm{D}=4$ (C and E unmatched) Improved matching: $A=4, B=3, D=1, E=2$ ( $C$ unmatched) |  |  |  |  |  | $\begin{array}{ll} \hline \text { B1 } \\ \text { B1 } & \text { (2) } \\ \hline \end{array}$ |
| (c) | e.g. (see below for alternatives) <br> Alternating path: $\mathrm{C}-3=\mathrm{B}-2=\mathrm{E}-5$ <br> Change status to give: $\mathrm{C}=3-\mathrm{B}=2-\mathrm{E}=5$ <br> Complete matching: $\mathrm{A}=4, \mathrm{~B}=2, \mathrm{C}=3, \mathrm{D}=1, \mathrm{E}=5$ |  |  |  |  |  | M1 <br> A1 <br> A1 <br> (3) <br> (7 marks) |
| Notes for Question 4 |  |  |  |  |  |  |  |
|  | Possible paths | A | B | C | D | E |  |
|  | C-3-B-2-E-5 | 4 | 2 | 3 | 1 | 5 |  |
|  | $\mathrm{C}-4-\mathrm{A}-1-\mathrm{D}-5$ | 1 | 3 | 4 | 5 | 2 |  |
|  | $\mathrm{C}-4-\mathrm{A}-3-\mathrm{B}-2-\mathrm{E}-5$ | 3 | 2 | 4 | 1 | 5 |  |

a1B1: Unmatched to unmatched (vertex/node may be implied but do not accept arc) - technical language (if used) must be correct
a2B1: (Alternate) arcs not in/in (arc(s) (not vertices/nodes) must be explicitly mentioned)
In (b) ignore the candidates labelling in this part - for example, give bod on candidates who call the initial matching the improved matching (and vice-versa) or those that state the initial matching under (ii). Condone lack of unmatched vertices stated. Both the initial and improved matching may be stated or drawn - do check carefully the top of the second page for these drawn there. Only accept a clear diagram with exactly three or four arcs
b1B1: CAO ( $\mathrm{A}=3, \mathrm{~B}=2, \mathrm{D}=4$ )
b2B1: $\mathrm{CAO}(\mathrm{A}=4, \mathrm{~B}=3, \mathrm{D}=1, \mathrm{E}=2)$
c1M1: An alternating path from C to 5 (or vice - versa)
c1A1: CAO - a correct path including change status either stated or shown. Chosen path clear
c2A1: CAO - must follow from correct stated path. Accept on a clear diagram (with five arcs only).

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 5.(a) | $\mathrm{A}(\mathrm{BC}) \mathrm{E}+\mathrm{H}(\mathrm{F}) \mathrm{G}=15+13=28^{*}$ <br> $\mathrm{A}(\mathrm{BDF}) \mathrm{H}+\mathrm{E}(\mathrm{F}) \mathrm{G}=30+7=37$ <br> $\mathrm{A}(\mathrm{BDF}) \mathrm{G}+\mathrm{E}(\mathrm{F}) \mathrm{H}=21+16=37$ <br> Repeat arcs: AB, BC, CE, HF, FG <br> Length: $214+28=242(\mathrm{~km})$ | M1 <br> A1 A1 A1 <br> A1 <br> A1ft <br> (6) |
| (b) | 4 | B1 (1) |
| (c) | EG (7) is the shortest link between two odd nodes excluding H Repeat EG (7) since this is the shortest path excluding H We finish at A Length of route $=214+7=221(\mathrm{~km})$ | M1 <br> A1 <br> A1 <br> (3) <br> (10 marks) |
| Notes for Question 5 |  |  |
| a1M1: Three distinct pairings of the correct four odd nodes <br> a1A1: One row correct including pairings and totals <br> a2A1: Two rows correct including pairings and totals <br> a3A1: All three rows correct including pairings and totals <br> a4A1: The smallest repeat arcs (accept ABCE, HFG but not AE, HG) <br> a5A1ft: Correct answer of 242 or 214 + their least |  |  |

b1B1: CAO (4)
c1M1: Identifies the need to repeat one path of the three (AE, EG, AG) which does not include H (maybe implicit) or listing of only these possible repeats - this mark is dependent on either scoring the M mark in (a) or stating all three posssible paths c1A1: Identifies EG as the least and A as the finishing point. They have to explicitly state the EG is the least path (but they do not need to include that it is the least of those that do not include H as this is the least of all six possible paths)
c2A1: CAO (221)

| Question <br> Number | Scheme |  |  |  |  |  | Marks |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6.(a) | Activit | Immediately preceded by | Activity | Immediate preceded by | Activity | Immediately preceded by | B2,1,0 | (2) |
|  | A | - | G | C | M | I |  |  |
|  | B | - | H | C | N | D E F J |  |  |
|  | C | - | I | D E | P | D E F J |  |  |
|  | D | A | J | G | Q | K P |  |  |
|  | E | B C | K | G | R | K P |  |  |
|  | F | B C | L | G H |  |  |  |  |
| (b) |  |  |  |  |  |  | M1 <br> A1 <br> M1 <br> A1 | (4) |
| (c) | Float on D $=21-5-8=8$ |  |  |  |  |  | B1 | (1) |
| (d) | Lower bound is $\frac{142}{42}=3.38 \ldots=4$ |  |  |  |  |  | B1 | (1) |
| (e) | e.g. |  |  |  |  |  | M1 <br> A1 <br> A1 <br> A1 <br> (12 ma | (4) |


| Question <br> Number | Scheme | Marks |
| :---: | :---: | :---: |

## Notes for Question 6

a1B1: Any four rows correct
a2B1: All eight rows correct
b1M1: All top boxes complete, values generally increasing in the direction of the arrows ('left to right'), condone one rogue
b1A1: CAO
b2M1: All bottom boxes complete, values generally decreasing in the opposite direction of the arrows ('right to left'), condone one rogue.
b2A1: CAO
c1B1: CAO - correct calculation seen
d1B1: CAO - either a correct calculation seen or awrt 3.4 then 4 . An answer of 4 with no working scores B0
e1M1: Not a cascade chart. 5 workers used at most, at least 8 new (14 in total) activities placed e1A1: 4 workers. All 11 new ( 17 in total) activities present (just once). Condone two errors either precedence or time interval or activity length
e2A1: 4 workers. All 11 new (17 in total) activities present (just once). Condone one error either precedence or time interval or activity length
e3A1: CAO

| Activity | Duration | Time interval | IPA |
| :--- | :--- | :--- | :--- |
| D | 8 | $5-21$ | A |
| E | 4 | $10-21$ | B, C |
| F | 3 | $10-23$ | B, C |
| H | 14 | $10-32$ | C |
| I | 11 | $14-32$ | D, E |
| K | 5 | $15-35$ | G |
| L | 10 | $24-42$ | G, H |
| M | 10 | $25-42$ | I |
| P | 11 | $23-35$ | D, E, F, J |
| Q | 7 | $34-42$ | K, P |
| R | 5 | $34-42$ | K, P |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 7.(a) | $\begin{aligned} & 60 x+35 y \geq 840 \text { or } x+\frac{7}{12} y \geq 14 \Rightarrow 12 x+7 y \geq 168 \\ & 15 x+24 y \leq 480 \text { or } \frac{1}{4} x+\frac{2}{5} y \leq 8 \Rightarrow 5 x+8 y \leq 160 \end{aligned}$ | M1 A1 <br> M1 A1 <br> (4) |
| (b) | $2 y \geq x$ | M1 A1 (2) |
| (c) |  | $\begin{aligned} & \text { B1 } \\ & 12 x+7 y=168 \\ & \text { B1 } \\ & 5 x+8 y=160 \\ & \text { B1 } \\ & 2 y=x \\ & \text { B1 } \\ & \text { R correct (4) } \end{aligned}$ |
| $\begin{aligned} & \text { (d)(i) } \\ & \text { (d)(ii) } \end{aligned}$ | Objective line correctly drawn (and labelled) Optimal vertex labelled $V\left(\frac{160}{9}, \frac{80}{9}\right)$ | B1 <br> DB1 <br> M1 A1 <br> (4) |
| (e) | Make 17 hardbacks and 9 paperbacks, expected profit (£)1344 | $\begin{aligned} & \text { B1 B1 (2) } \\ & \text { (16 marks) } \end{aligned}$ |


| Question |
| :---: |
| Number |

Scheme

## Notes for Question 7

a1M1: Two of three coefficients correct with correct inequality sign in unsimplfied form or all three coefficients correct with any sign ( $=,<,>, \leq, \geq$ )
a1A1: CAO (the correct answer with no working can imply M1 only)
a2M1: Two of the three coefficients correct with correct inequality sign in either unsimplified or simplified form or all three coefficients correct with any sign ( $=,<,>, \leq, \geq$ )
a2A1: CAO (the correct answer with no working can imply M1A1)
b1M1: Either both coefficients correct (accept $=,<,>, \leq, \geq$ here) or $y \geq 2 x$
b1A1: CAO
c1B1: $12 x+7 y=168$ drawn correctly, does not pass outside of a small square of $(0,24)$ and $(14,0)$. Ignore shading
c2B1: $5 x+8 y=160$ drawn correctly, does not pass outside of a small square of $(0,20)$ and $(32,0)$. Ignore shading
c3B1: $2 y=x$ drawn correctly, does not pass outside of a small square of $(0,0),(16,8)$ and sufficiently long enough to define the feasible region. Ignore shading
c4B1: R labelled correct (not just implied by shading) - must have earned all previous marks in this part
di1B1: Drawing the correct objective line on the graph, use line drawing tool to check if necessary. Line must not pass outside of a small square if extended from axis to axis
di2DB1: V labelled clearly on their graph. This mark is dependent on both the correct three line segments that define the boundary of the feasible region and the correct objective line
dii1M1: The simultaneous equations $5 x+8 y=160$ and $x=2 y$ being used in an attempt to find V - must get to $\mathrm{x}=\cdots$ or $\mathrm{y}=\cdots$ (condone one error in the solving of the simultaneous equations) dii1A1: CAO $\left(\frac{160}{9}, \frac{80}{9}\right)$ or $\left(17 \frac{7}{9}, 8 \frac{8}{9}\right)$ (coordinates must be exact) - the correct answer with no working can imply M1A1
e1B1: CAO $(17,9)-$ accept $x=17, y=9$
e2B1: CAO ((£)1344)

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