



1. The discrete random variable  $X$  has probability distribution

$x$	-4	-2	1	3	5
$P(X=x)$	0.4	$p$	0.05	0.15	$p$

(a) Show that  $p = 0.2$  (2)

Find

(b)  $E(X)$  (2)

(c)  $F(0)$  (1)

(d)  $P(3X + 2 > 5)$  (2)

Given that  $\text{Var}(X) = 13.35$

(e) find the possible values of  $a$  such that  $\text{Var}(aX + 3) = 53.4$  (2)

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2. The discrete random variable  $X$  has probability distribution

$$P(X = x) = \frac{1}{10} \quad x = 1, 2, 3, \dots, 10$$

(a) Write down the name given to this distribution. (1)

(b) Write down the value of

- (i)  $P(X = 10)$
- (ii)  $P(X < 10)$

(2)

The continuous random variable  $Y$  has the normal distribution  $N(10, 2^2)$

(c) Write down the value of

- (i)  $P(Y = 10)$
- (ii)  $P(Y < 10)$

(2)

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Question 2 continued

Lined area for writing the answer to Question 2.

Q2

(Total 5 marks)



3. A large company is analysing how much money it spends on paper in its offices every year. The number of employees,  $x$ , and the amount of money spent on paper,  $p$  (£ hundreds), in 8 randomly selected offices are given in the table below.

$x$	8	9	12	14	7	3	16	19
$p$ (£ hundreds)	40.5	36.1	30.4	39.4	32.6	31.1	43.4	45.7

(You may use  $\sum x^2 = 1160$      $\sum p = 299.2$      $\sum p^2 = 11\,422$      $\sum xp = 3449.5$ )

- (a) Show that  $S_{pp} = 231.92$  and find the value of  $S_{xx}$  and the value of  $S_{xp}$  (5)

- (b) Calculate the product moment correlation coefficient between  $x$  and  $p$ . (2)

The equation of the regression line of  $p$  on  $x$  is given in the form  $p = a + bx$ .

- (c) Show that, to 3 significant figures,  $b = 0.824$  and find the value of  $a$ . (4)

- (d) Estimate the amount of money spent on paper in an office with 10 employees. (2)

- (e) Explain the effect each additional employee has on the amount of money spent on paper. (1)

Later the company realised it had made a mistake in adding up its costs,  $p$ . The true costs were actually half of the values recorded. The product moment correlation coefficient and the equation of the linear regression line are recalculated using this information.

- (f) Write down the new value of
- (i) the product moment correlation coefficient,
  - (ii) the gradient of the regression line. (2)

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4.  $A$  and  $B$  are two events such that

$$P(B) = \frac{1}{2} \quad P(A|B) = \frac{2}{5} \quad P(A \cup B) = \frac{13}{20}$$

(a) Find  $P(A \cap B)$ . **(2)**

(b) Draw a Venn diagram to show the events  $A, B$  and all the associated probabilities. **(3)**

Find

(c)  $P(A)$  **(1)**

(d)  $P(B|A)$  **(2)**

(e)  $P(A' \cap B)$  **(1)**

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**(Total 9 marks)**

Q4



5. The table shows the time, to the nearest minute, spent waiting for a taxi by each of 80 people one Sunday afternoon.

Waiting time (in minutes)	Frequency
2–4	15
5–6	9
7	6
8	24
9–10	14
11–15	12

- (a) Write down the upper class boundary for the 2–4 minute interval. (1)

A histogram is drawn to represent these data. The height of the tallest bar is 6 cm.

- (b) Calculate the height of the second tallest bar. (3)

- (c) Estimate the number of people with a waiting time between 3.5 minutes and 7 minutes. (2)

- (d) Use linear interpolation to estimate the median, the lower quartile and the upper quartile of the waiting times. (4)

- (e) Describe the skewness of these data, giving a reason for your answer. (2)

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6. The time taken, in minutes, by children to complete a mathematical puzzle is assumed to be normally distributed with mean  $\mu$  and standard deviation  $\sigma$ . The puzzle can be completed in less than 24 minutes by 80% of the children. For 5% of the children it takes more than 28 minutes to complete the puzzle.

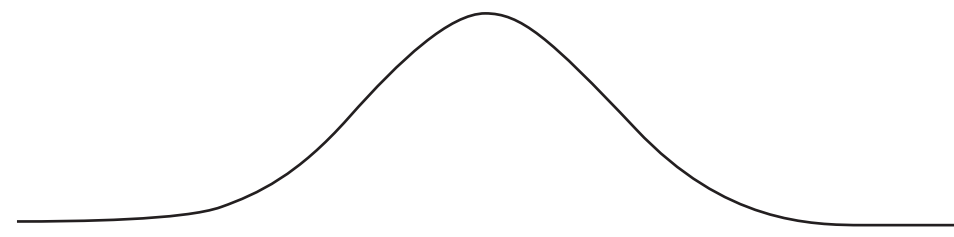
(a) Show this information on the Normal curve below. **(2)**

(b) Write down the percentage of children who take between 24 minutes and 28 minutes to complete the puzzle. **(1)**

(c) (i) Find two equations in  $\mu$  and  $\sigma$ .  
 (ii) Hence find, to 3 significant figures, the value of  $\mu$  and the value of  $\sigma$ . **(7)**

A child is selected at random.

(d) Find the probability that the child takes less than 12 minutes to complete the puzzle. **(3)**




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7. In a large company,

78% of employees are car owners,  
30% of these car owners are also bike owners,  
85% of those who are not car owners are bike owners.

(a) Draw a tree diagram to represent this information.

**(3)**

An employee is selected at random.

(b) Find the probability that the employee is a car owner or a bike owner but not both.

**(2)**

Another employee is selected at random.

Given that this employee is a bike owner,

(c) find the probability that the employee is a car owner.

**(3)**

Two employees are selected at random.

(d) Find the probability that only one of them is a bike owner.

**(3)**





